# The Longitudinal Characteristics of Three Slender 'Mild Ogee' Wings at Mach Numbers from 0.4 to 2.0 

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## THE LONGITUDINAL CHARACTERISTICS OF THREE SLENDER "MILD OGRE" WINGS AT MACH NUMBERS FROM 0.4 TO 2.0

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## SUMMARY

Wind tunnel measurements of lift, pitching moment and drag on one plane and two cambered wings of "mild ogee" planform ( $p=8 / 15$ ) are reported. These measurements are supplemented by vapour screen and oil flow observations.

The wings were designed by slender wing theory for attached flow along the leading-edge at particular values of lift and pitching moment. The design and measured attachment conditions agreed fairly well. The non-linear luft developed could be related with the type of vortex development above the attachment incidence.

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## INTRODUCTION

To assist the design of slender wings for flight at supersonce speeds three "mild ogee" wings were tested in the $3 \times 3 \mathrm{ft}$ wand tunnel over the Mach number range from $M=0.40$ to 2.00 m January 1961. These wings had a common planform, with a value of planform parameter $p=0.533$ intermediate between the high value of wings tested by Squire ${ }^{1,2,3}$ and the low value of wings tested by Courtney ${ }^{4}$ and Taylor ${ }^{5}$. The tests were intended to provide more data on the effects of $p$ on camber design and lift dependent drag.

This paper compares the measured and calculated forces and moments on the wings and describes the types of flow observed at off-design conditions.

## 2 EXPERTMENTAL DETAMS

2.1 Model design

The three wings had a common planform (Fig. 1 and Table 1); as they followed the eight wings discussed in Refs.1, 2 and 3 they were designated wings 9, 10 and 11.

Wing 9 was uncambered. The cambered wangs were designed by slender wing theory for attached flow at the leading-edge with a given load distribution. The method of camber desagn was outlined by Weber ${ }^{5}$. For both wangs the spanwise camber was restricted to a region outboard of a "shoulder position" defined by $y=(0.5+0.25 x)(S x)$. Wang 10 was designed for flow attachment at a lift coefficient of 0.05 with the centre of pressure at $0.547 \mathrm{c}_{0}$. This was $0.07 \mathrm{c}_{0}$ forward of the slender wang aerodynamic centre position, $0.617 \mathrm{c}_{0}$. The patching moment increment $\Delta \mathrm{C}_{\mathrm{m}}$ was thus 0.0035 on $\mathrm{c}_{0}$ (or 0.0053 on $\overline{\bar{c}}$ ). The design of this wing was discussed in Ref. 7 and details of the design loading and the camber shapes are given an Figs. 2 and 3 and Table 1. Wing 11 was designed for the same patching moment increment as wing $10\left(\Delta C_{m}=0.0053\right.$ on $\left.\overline{\bar{c}}\right)$ at zero lift coefficient. The design load distribution for Wing 11 was that of Wing 10 less the slender wing load distribution on an uncambered wing with $C_{L}=0.05$. Details of Wing $11^{*}$ are given in Figs. 2 and 3 of Table 1.

The thickness was added to the camber surface as an earlier wings of this series ${ }^{1,2,3}$. The diamond shaped thickness distribution was added to the

[^1]camber surfaces so that areas of spanwise stations were the same for all three wings. Typical cross-sections are shown in Fig. 2.

A small body was added to the rear of the model to shield the balance and sting support. On the cambered models this shield was not quite symmetric, however, the estimated errors caused by this asymmetry on the wing pitching moment are small.

Wing 9 was made completely of steel but Wings 10 and 11 were made of glass-cloth and araldite on a steel core. The models were given a matt black paint finish to facilltate flow visualization.

### 2.2 Test range

The tests were made in the transonic and supersonic sections of the $3 \times 3 f t$ tunnel at R.A.E. Bedford. The lift, pitching moment and drag were measured in the nomnal incidence* range $-2^{\circ}$ to $+13^{\circ}$ (one degree steps) at Mach numbers of $0.40,0.70,0.85,0.90,0.94,0.98,1.02,1.42,1.61,1.82$ and 2.00. In addition, surface oil flow and vapour screen patterns were obtanned at selected conditions where changes in types of flow were expected.

The test Reynolds number was $1.6 \times 10^{6}$ per foot, except at $M=2.0$ when it was reduced to $1.35 \times 10^{6}$ per foot because of a tunnel power limitation.

In all force tests bands of distributed roughness were applied to fix transition of the boundary layer on both surfaces of the wing. The roughness bands consisted of a mixture of carborundum grains and thin aluminium paint applıed so that closely spaced indıvidual grains projected from a paint base about 0.001 inch thick. The height of the particles was 0.003 inch at speeds up to 1.02 and 0.007 inch at hagher speeds. The roughness bands were half an inch wide (normal to the leading-edge) and started an eighth of an inch inboard of the edge.

This roughness distrıbution did fix transition on other wings of this series ${ }^{3}$ except possibly at $M=1.02$ and 2.00 for a small incidence range. However, the drag results on Wing 9 at $M=1.8$ and 2.0 revealed a "bucket" of the type previously associated ${ }^{8}$ with laminar flow as shown in Fig. 40 An investigation of the boundary layer state using azobenzene did, in fact, reveal large areas of laminar flow (Fig.5). The minimum height of roughness

[^2]needed to fix transition at the comparatively low Reynolds numbers then available in the $3 f t$ tunnel was subsequently determined and was reported in Ref.9. This investigation included drag measurements on Wing 9 with different roughness distributions over a wide range of Reynolds number but for consistenoy with wings 10 and 11 , only data with roughness particles 0.007 inch high were quoted here.

### 2.3 Accuraoy

The balance results have been corrected for interaction effects and sting deflection before being reduced to coefficient forms; for all wings these coefficients are based on the dimensions of the common planform. Moments (based on $\overline{\overline{0}}$ ) are referred to the $48.5 \%$ point of the aerodynamic mean chord ( $66 \%$ of the root chord) so that the change of aerodynamic centre position with Mach number is emphasised (Figs.10-12). The drag has been corrected to a base pressure equal to free stream static pressure. No corrections have been applied to the measured pitching moment or drag for the small distortion caused by the sting shield.

The incidence and pitching moment have been corrected for flow deflection and curvature in the tunnel stream. The flow corrections were found for the uncambered wing and the same corrections applied to all the cambered wings: the maxinum carrections were $\Delta \alpha=0.2^{\circ}$ and $\Delta C_{m}=0.0010$. Previous tests in this series ${ }^{3}$ have justified this procedure.

No corrections have been applied for tunnel interference; this interference is, of course, absent at supersonic speeds when the bow shock wave is reflected clear of the model ( $M>1.3$ ). There is, however, some interference at subsonic and transonic speeds. Previous tests have shown that these effects are small except near $M=1.00$. Here the Mach number error may be as large as 0.02 ; the free stream Mach number being less than the quoted tunnel Mach number.

Apart from this tunnel interference it is estimated that the accuracy of the results is as follows

$$
\begin{aligned}
& C_{L} \quad \pm 0.003 \\
& C_{m} \\
& \\
& C_{D} \\
& C_{D} .0006 \\
& \\
& \\
& \\
& \\
& \\
& \\
& \pm 0.0004 \text { at } C_{L}=0 \\
& \pm 0.05^{\circ}
\end{aligned}
$$

## 3 RESUITS

### 3.1 Lift and pitching moment

The variation of lift coefficient with incidence is plotted in Figs.6-8 for Wings 9-11. Appreciable non-linear lift is developed from flow separations at the sharp leading-edges, particularly at subsonic speeds. The oambered wings should have attached flow along the leading-edge at the design condition, which may be compared with the incidence ( $\bar{\alpha}$ ) for minimum lift curve slope near $M=1.0$ (the Mach number appropriate to the slender wing design value $\beta S_{1} / c_{0}=0$ ). Fair agreement is shown in the following table.

Comparison of attachment conditions near $M=1.0$

| Wing | Measured |  | Design |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\bar{\alpha}$ | $\overline{\mathrm{c}}_{\mathrm{L}}$ | $\bar{\alpha}$ | $\overline{\mathrm{C}}_{\mathrm{L}}$ |
| 10 | $4.0^{\circ}$ | 0.075 | $3.2^{\circ}$ | 0.05 |
| 11 | $1.0^{\circ}$ | 0.012 | $0.8^{\circ}$ | 0 |

The lift development for the three wings above the attachment incidence may be compared ${ }^{3}$ by plotting $C_{L}-\bar{C}_{L}$ against $\alpha-\bar{\alpha}$, Fig.9. The lift on Wings 9 and 11 correlates exactly but much more non-linear lift is developed by Wing 10. This is discussed in 3.3 below.

Near the attachment incidence the slopes of the curves do not vary significantly with Mach number and correspond fairly well with the slender wing value appropriate to $M=1.0\left(\mathrm{dC}_{\mathrm{L}} / \mathrm{d} \alpha=\pi \mathrm{A} / 2\right)$, (Fig.9b).

Above the attachment incidence non-linear lift develops; this is considerable at $M=0.40$ (Fig.9a), reaches a maximum near $M=1.0$ but decreases as the Mach number increases to $M=2.0$ (Fig. 9 b ). The non-linear lift measured on Wings 9 and 11 at $M=1.02$ compares favourably with that given by Mangler and $\operatorname{Smith}^{10,11 .}$

The variation of pitching moment coefficient $C_{m}$ with lift coefficient for Wings 9-11 is shown in Figs. 10-12. The curves are fairly smooth and
clearly show the rearward movement of aerodynamic centre, as the Mach number increases from subsonic to supersonic speeds. The aerodynamic centre positions on the root chord $c_{0}$ are given at lift coefficients of $0.05,0.10$,
at $M=2.0$ on some highly swept arrow wings with sharp leading-edges. Fig. 5 of Ref. 12 is particularly relevant to the present tests. Carborundum slightly higher than 0.007 inch was used and the Reynolds number range extended from $R=0.5 \times 10^{6}$ to $404 \times 10^{6}$. Transition was always fixed on the cambered wing but on the plane wing transition occurred from $R=1.3 \times 10^{6}$ to $2.0 \times 10^{6}$ (c.f. the present test Reynolds number $1.35 \times 10^{6}$ with particles only 0.007 inch high).

The measured variation with Mach number of $C_{D_{0}}$ for Wing 9 is plotted in Fig.20. The estimated total drag (the wave drag of the model including the fairing plus skin friction) is also plotted. At subsonic and transonic speeds the measured drag is $10 \%$ higher than the estimated skin friction as in previous tests with a model having the same area distribution ${ }^{3}$ : this difference may be caused by sting interference or it could be form drag. At supersonic speeds there is excellent agreement between the measured and estimated drags at $M=1.42$ and 1.61, the measured $C_{D_{0}}$ being 0.0002 lower than the estimate. However, at 1.82 and 2.00 the measured $C_{D_{0}}$ is lower than the estimate due to the failure to fix transition of the boundary layer. It was assumed in the analysis of the drag due to lift that the plane wing $C_{D_{0}}$ with fixed transition at $M=1.82$ and $2.00, C_{D}^{1}$, is also 0.0002 Iower than the estimate. [If the axial force for $M=1.82$ and 2.00 is plotted against $|\alpha|$ and the laminar bucket faired out the value of axial force at $\alpha=0$, ( $C_{D}$ ), is in fact about 0.0002 below the estimate for both Mach numbers.]

Fig. 21 shows the variation of the drag due to lift factor with lift coefficient and Mach number for the three wings. $C_{D}$ is the measured drag coefficient on the respective wings (with roughness particles 0.007 inch high).

The variation of the drag due to lift factors with slenderness parameter $\beta S_{T} / c_{0}$ at $C_{L}{ }^{\prime} s$ of 0.10 and 0.20 from Fig. 21 are plotted $2 n$ Fig.22. Wings 9 and 11 are nearly identical and lie above Courtney's correlation curve ${ }^{13}$. In contrast Wing 10 lies close to Courtney's curve, although still above the deszgn value ${ }^{7}$ at $\beta S_{T} / c_{0}=0.374$. This improvement in the drag due to lift contributes to the favourable lift-to-drag ratios measured on Wing 10 compared to Wings 9 and 11; the wing lift-to-drag ratios are presented in Fig. 23.

## 3.3 <br> Vortex development

The non-linear laft developed on Wings 9 and 11 above the attachment incidence is nearly the same. In contrast Wing 10 develops considerably more non-linear lift than Wings 9 and 11 when $\alpha-\bar{\alpha}$ is greater than about $3^{\circ}$. These results can be related with the vortex development observed on the wings.

The first useful clue to the vortex development was observed on the tunnel schlieren at $M=2.0$ with carborundum 0.020 nnch high on the wings (during the roughness investigation reported in Ref.9). The shock waves from the particles were then clearly vislble along the leading-edge (c.f. 3.2 above) at the attachment incidence. When the incidence increased these shock waves disappeared as the roughness became immersed in the separated flow from the leading-edge. For Wings 9 and 11 measurements revealed that the region without shock waves increased gradually as incidence increased (Fig. 24). For Wing 10, however, the shock waves seemed to disappear suadenly between $\alpha=7^{\circ}$ to $8^{\circ}\left(\alpha-\bar{\alpha}\right.$ between $3^{\circ}$ and $\left.4^{\circ}\right)$ and it was impossible to measure thas movement.

Observation* of the vortaces using the vapour screen technique ${ }^{14}$ confarmed the close simılarity of the flow on Wings 9 and 11 (Figs.25a and 25c). On Wings 9 and 11 the leading-edge vortex develops approximately conically as incidence increases. On Wing 10, an addition to the leadingedge vortex an array of streanwise vortices seems to develop as incidence increases (Fig.25b). Between $\alpha=7.3^{\circ}$ and $8.3^{\circ}$ the leading-edge vortex and the streamwise vortices suddenly coalescet. The vortex on Wing 10 is then wider than on Wings 9 and 11 (c.f. Fig.25a, $\alpha-\bar{\alpha}=401^{\circ}$ and Fig.25b, $\alpha-\bar{\alpha}=4.2^{\circ}$ ). This wader spanwise extent of the vortex on wing 10 probably produces the larger non-lınear lift (c.f. Fig.9, Wings 10 and 9). The vapour screen on Wing 10 at $M=1.4$ with and without roughness was identical with that at $M=1.8$ so that the boundary layer state could not be determining the vortex development.

[^3]The oil flow photographs now presented illustrate additional details of the vortex development on Wings 9 and 10. Fig. 26 shows some typical oil flow photographs taken on Wing 9. Fig. 26a, at $M=2.0$ and $\alpha=5.1^{\circ}$ shows a similar flow to that on a slender delta wing. The vortex development is nearly conical and is characterised by a strong primary vortex and a secondary separation near the leading edge; the roughness was removed to show this secondary separation. Fig. 26 b at $M=0.40, \alpha=5.1^{\circ}$ is included to recall that if wings are sufficiently slender there is close similarity between the separated flows at subsonic and supersonic speeds although the non-linear lift is larger at subsonic speeds. The vortex is roughly elliptical in section on the vapour screen at supersonic speeds (Fig.25a) and is known to be roughly circular in section at subsonic speeds. The change in width of the vortex can be seen in Fig.26. Here the intersection of the attachment line and the trailing-edge moves outboard from $0.64 \mathrm{~S}_{\mathrm{T}}$ at $\mathrm{M}=2.0$ to $0.77 \mathrm{~S}_{\mathrm{T}}$ at $\mathrm{M}=0.40$.

Fig. 27 shows some typical oil flow photographs taken on Wing 10 at $M=1.4$ without roughness. The flow at $7.3^{\circ}$ shows a complex array of streamwise vortices covering most of the planform (Fig.27a). A similar array of vortices has been observed previously on delta wings and attributed ${ }^{16}$ to the rolling up of the boundary layer vorticity under the influence of the spanwise pressure gradient. The flow at $8.3^{\circ}$ apparently shows only one large vortex but a careful examination reveals a few streamwise vortices inboard of the main vortex (Fig.27b).

## 4 CONCLUSIONS

Tests of three mild ogee wings in the 3ft tunnel at subsonic and supersonic speeds showed that a prescribed type of lift and centre of pressure position ${ }^{6,7}$ was achieved on both cambered wings.

The vortex development on Wings 9 and 11 was approximately conical and similar to that on a slender delta. The vortex development on Wing 10 at supersonic speeds was characterised inctially by what seems to be an array of small streamwise vortices in addition to the leading-edge vortex. The streamwise vortices coalesced suddenly with the leading-edge vortex as incidence was increased. This single vortex extended spanwise further than the vortex on Wings 9 and 11 at comparable incidences; the increase in size probably accounted for the larger non-linear lift increment of Wing 10.

## TABLE 1

## GEOMETRY OF WINGS 9-11

=

Root chord
Aerodynamic mean chord
Wing area
Aspect ratio
Equation of leading edge
Planform parameter
$c_{0}=22$ inches
$\overline{\bar{c}}=37 / 56 \cdot c_{0}=14.545$ inches
$S=16 / 15 \cdot S_{T} c_{0}=129.1$ square
$A=0.9375$
$y=S_{T} x\left(1+x^{3}-x^{4}\right)$
$\mathrm{p}=8 / 15=0.533$
Slenderness factor

$$
S_{T} / c_{0}=0.25
$$

Newby area distribution
where
$A(x)=12 V c_{0}^{2} x^{2}(1-x)$
$V=$ volume $/ c_{0}^{3}$
$\mathrm{V}=0.00584$.

Hence non dimensional volume factor
$\tau=$ wing volume/wing area ${ }^{3 / 2}=0.0424$.

Wing 10 Equation of centre line camber

$$
z=0.0395\left[1.413-\left(x+2.648 x^{2}-3.644 x^{3}+1.409 x^{4}\right)\right] .
$$

## Wing 11 - Table of centre line camber

| $x$ | $z$ |
| :---: | :---: |
| 0.0 | 0.0136 |
| 0.1 | 0.0129 |
| 0.2 | 0.0112 |
| 0.3 | 0.088 |
| 0.4 | 0.0063 |
| 0.5 | 0.0039 |
| 0.6 | 0.0021 |
| 0.7 | 0.0013 |
| 0.8 | 0.0002 |
| 0.9 | 0.0000 |
| 1.0 | 0.0000 |

RESULTS - WING 9

| M | $\alpha$ | $\mathrm{C}_{L}$ | $C_{\text {m }}$ | $C_{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | $\begin{array}{r} -2.04 \\ -1.07 \\ 0 \\ +1.02 \\ 1.99 \\ 3.06 \\ 4.09 \\ 5.11 \\ 6.14 \\ 7.17 \\ 8.20 \\ 9.23 \\ 10.27 \\ 11.30 \\ 12.34 \end{array}$ | $\begin{array}{r} -0.051 \\ -0.026 \\ -0.001 \\ +0.024 \\ 0.048 \\ 0.079 \\ 0.108 \\ 0.141 \\ 0.178 \\ 0.215 \\ 0.256 \\ 0.296 \\ 0.336 \\ 0.378 \\ 0.423 \end{array}$ | $\begin{array}{r} -0.0032 \\ -0.0019 \\ 0 \\ +0.0021 \\ 0.0036 \\ 0.0054 \\ 0.0077 \\ 0.0095 \\ 0.0106 \\ 0.0139 \\ 0.0171 \\ 0.0199 \\ 0.0231 \\ 0.0264 \\ 0.0301 \end{array}$ | 0.0098 0.0090 0.0090 0.0093 0.0105 0.0130 0.0163 0.0212 0.0271 0.0346 0.0440 0.0549 0.0676 0.0816 0.0983 |
| 0.70 | $\begin{array}{r} -2.06 \\ -1.08 \\ 0 \\ +1.03 \\ 2.02 \\ 3.10 \\ 4.14 \\ 5.18 \\ 6.23 \\ 7.27 \\ 8.32 \\ 9.37 \\ 10.43 \\ 11.48 \\ 12.54 \end{array}$ | -0.051 -0.027 -0.002 0.021 0.050 0.079 0.113 0.149 0.186 0.223 0.266 0.307 0.349 0.396 0.440 | $\begin{array}{r} -0.0032 \\ -0.0017 \\ 0 \\ 0.0018 \\ 0.0032 \\ 0.0047 \\ 0.0064 \\ 0.0082 \\ 0.0100 \\ 0.0121 \\ 0.0145 \\ 0.0170 \\ 0.0192 \\ 0.0221 \\ 0.0250 \end{array}$ | $\begin{aligned} & 0.0099 \\ & 0.0091 \\ & 0.0088 \\ & 0.0097 \\ & 0.0106 \\ & 0.0134 \\ & 0.0168 \\ & 0.0218 \\ & 0.0279 \\ & 0.0354 \\ & 0.0457 \\ & 0.0571 \\ & 0.0702 \\ & 0.0863 \\ & 0.1032 \end{aligned}$ |
| 0.85 | $\begin{array}{r} -2.02 \\ -1.09 \\ 0 \\ 1.04 \\ 2.03 \\ 3.12 \\ 4.17 \\ 5.22 \\ 6.28 \\ 7.33 \\ 8.39 \\ 9.45 \\ 10.51 \\ 11.58 \\ 12.64 \end{array}$ | $\begin{aligned} & -0.054 \\ & -0.028 \\ & -0.001 \\ & +0.023 \\ & 0.052 \\ & 0.085 \\ & 0.121 \\ & 0.158 \\ & 0.197 \\ & 0.238 \\ & 0.281 \\ & 0.327 \\ & 0.370 \\ & 0.418 \\ & 0.465 \end{aligned}$ | $\begin{gathered} -0.0033 \\ -0.0017 \\ 0 \\ 0.0015 \\ 0.0025 \\ 0.0039 \\ 0.0053 \\ 0.0066 \\ 0.0083 \\ 0.0093 \\ 0.0112 \\ 0.0124 \\ 0.0143 \\ 0.0158 \\ 0.0175 \end{gathered}$ | $\begin{aligned} & 0.0097 \\ & 0.0093 \\ & 0.0086 \\ & 0.0094 \\ & 0.0104 \\ & 0.0132 \\ & 0.0171 \\ & 0.0225 \\ & 0.0293 \\ & 0.0379 \\ & 0.0482 \\ & 0.0609 \\ & 0.0748 \\ & 0.0917 \\ & 0.1103 \end{aligned}$ |

(Contd.)

TABIE 2 (Contd.)
$=$

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $\mathrm{C}_{\mathrm{D}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.90 | -2.02 | -0.060 | -0.0025 | 0.0098 |
|  | -1.03 | -0.028 | -0.0014 | 0.0091 |
|  | 0 | -0.003 | 0 | 0.0084 |
|  | 1.04 | 0.024 | 0.0012 | 0.0091 |
|  | 2.03 | 0.054 | 0.0028 | 0.0109 |
|  | 3.12 | 0.086 | 0.0036 | 0.0136 |
|  | 4.17 | 0.122 | 0.0050 | 0.0172 |
|  | 5.21 | 0.158 | 0.0060 | 0.0225 |
|  | 6.26 | 0.199 | 0.0071 | 0.0296 |
|  | 7.32 | 0.241 | 0.0081 | 0.0385 |
|  | 8.37 | 0.284 | 0.0093 | 0.0490 |
|  | 9.43 | 0.331 | 0.0102 | 0.0617 |
|  | 10.48 | 0.374 | 0.0116 | 0.0758 |
|  | 11.54 | 0.421 | 0.0130 | 0.0926 |
|  | 12.60 | 0.469 | 0.0140 | 0.1113 |
| 0.94 | -2.02 | -0.056 | -0.0029 | 0.0098 |
|  | -1.08 | -0.029 | -0.0017 | 0.0090 |
|  | 0 | -0.003 | 0 | 0.0086 |
|  | 1.04 | 0.024 | 0.0015 | 0.0092 |
|  | 2.04 | 0.055 | 0.0027 | 0.0108 |
|  | 3.13 | 0.088 | 0.0036 | 0.0134 |
|  | 4.18 | 0.125 | 0.0047 | 0.0175 |
|  | 5.22 | 0.162 | 0.0053 | 0.0228 |
|  | 6.27 | 0.204 | 0.0062 | 0.0302 |
|  | 7.32 | 0.245 | 0.0071 | 0.0390 |
|  | 8.38 | 0.290 | 0.0079 | 0.0499 |
|  | 9.43 | 0.339 | 0.0080 | 0.0635 |
|  | 10.49 | 0.383 | 0.0086 | 0.0782 |
|  | 11.55 | 0.4331 | 0.0094 | 0.0951 |
|  | 12.60 | 0.478 | 0.0100 | 0.1142 |
| 0.98 | -2.02 | -0.059 | -0.0023 | 0.0104 |
|  | -1.03 | -0.029 | -0.0016 | 0.0093 |
|  | +0.01 | -0.003 | 0 | 0.0087 |
|  | 1.05 | 0.025 | 0.0015 | 0.0095 |
|  | 2.04 | 0.055 | 0.0021 | 0.0115 |
|  | 3.13 | 0.091 | 0.0027 | 0.0144 |
|  | 4.18 | 0.129 | 0.0031 | 0.0187 |
|  | 5.22 | 0.167 | 0.0036 | 0.0245 |
|  | 6.32 | 0.211 | 0.0037 | 0.0314 |
|  | 7.32 | 0.257 | 0.0031 | 0.0414 |
|  | 8.37 | 0.300 | 0.0031 | 0.0524 |
|  | 9.42 | 0.351 | 0.0022 | 0.0665 |
|  | 10.47 | 0.397 | 0.0018 | 0.0819 |
|  | 11.51 | 0.445 | 0.0001 | 0.0993 |
|  | 12.56 | 0.497 | -0.0011 | 0.1195 |

(Contd.)

TABLE 2 (Contd.)

| M | $\alpha$ | $\mathrm{C}_{L}$ | $\mathrm{c}_{\text {m }}$ | CD |
| :---: | :---: | :---: | :---: | :---: |
| 1.02 | $\begin{gathered} -2.06 \\ -1.03 \\ 0 \\ 1.04 \\ 2.03 \\ 3.12 \\ 4.16 \\ 5.20 \\ 6.25 \\ 7.29 \\ 8.34 \\ 9.38 \\ 10.44 \\ 11.49 \\ 12.54 \end{gathered}$ | -0.058 -0.029 -0.005 0.024 0.060 0.097 0.134 0.177 0.222 0.262 0.308 0.354 0.403 0.450 0.494 | -0.0002 -0.0011 0 +0.0010 0.0007 0.0004 0 -0.0011 -0.0016 -0.0022 -0.0031 -0.0040 -0.0044 -0.0055 -0.0058 | $\begin{aligned} & 0.0125 \\ & 0.0117 \\ & 0.0111 \\ & 0.0115 \\ & 0.0138 \\ & 0.0166 \\ & 0.0210 \\ & 0.0268 \\ & 0.0351 \\ & 0.0442 \\ & 0.0558 \\ & 0.0692 \\ & 0.0851 \\ & 0.1025 \\ & 0.1211 \end{aligned}$ |
| 1.42 | $\begin{array}{r} -1.96 \\ -0.93 \\ +0.10 \\ +1.14 \\ +2.17 \\ +3.20 \\ +4.24 \\ +5.28 \\ +6.32 \\ +7.36 \\ +8.40 \\ +9.45 \\ +10.49 \\ +11.54 \\ +12.58 \\ +0.09 \end{array}$ | -0.052 -0.023 +0.006 +0.033 +0.062 +0.093 +0.128 +0.163 +0.199 +0.235 +0.272 +0.308 +0.345 +0.381 +0.418 -0.008 | $\begin{aligned} & +0.0007 \\ & +0.0004 \\ & -0.0003 \\ & -0.0007 \\ & -0.0013 \\ & -0.0021 \\ & -0.0029 \\ & -0.0038 \\ & -0.0046 \\ & -0.0052 \\ & -0.0059 \\ & -0.0064 \\ & -0.0069 \\ & -0.0073 \\ & -0.0076 \\ & +0.0002 \end{aligned}$ |  |
| 1.61 | $\begin{array}{r} -1.86 \\ -0.83 \\ +0.19 \\ +1.23 \\ +2.26 \\ +3.20 \\ +4.23 \\ +5.27 \\ +6.41 \\ +7.45 \\ +8.49 \\ +9.53 \\ +10.57 \\ +11.61 \\ +12.66 \\ +0.20 \end{array}$ | $\begin{aligned} & -0.044 \\ & -0.018 \\ & +0.001 \\ & +0.033 \\ & +0.064 \\ & +0.093 \\ & +0.126 \\ & +0.158 \\ & +0.191 \\ & +0.224 \\ & +0.257 \\ & +0.290 \\ & +0.324 \\ & +0.356 \\ & +0.389 \end{aligned}$ | +0.0002 0 0 -0.0007 -0.0014 -0.021 -0.0028 -0.0035 -0.0041 -0.0047 -0.0051 -0.0055 -0.0059 -0.0061 -0.0063 -0.0002 |  |

(Conta.)

TABIE 2 (Contd.)

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.82 | -2.06 | -0.050 | +0.0009 | +0.0115 |
|  | -1.03 | -0.023 | $+0.0003$ | +0.0103 |
|  | 0 | $+0.001$ | 0 | +0.0095 |
|  | +1.02 | $+0.024$ | -0.0002 | +0.0106 |
|  | +2.06 | $+0.054$ | -0.0010 | +0.0122 |
|  | +3.09 | $+0.081$ | -0.0015 | +0.0145 |
|  | +4. 12 | +0.112 | -0.0022 | +0.0181 |
|  | +5.16 | +0.142 | -0.0027 | +0.0227 |
|  | +6.19 | +0.173 | -0.0032 | +0.0285 |
|  | +7.23 | $+0.203$ | -0.0036 | +0.0355 |
|  | +8.27 | +0.234 | -0.0038 | +0.0431 |
|  | +9.31 | +0.265 | -0.0041 | +0.0531 |
|  | +10.35 | +0.294 | -0.0043 | +0.0635 |
|  | +11.39 | +0.324 | -0.0044 | +0.0750 |
|  | +12.43 | +0.354 | -0.0045 | +0.0877 |
|  | 0 | $+0.001$ | -0.0001 | +0.0092 |
|  | -1.08 | -0.024 | $+0.0004$ | +0.0103 |
|  | -0.82 | -0.016 | +0.0002 | +0.0100 |
|  | -0.63 | -0.018 | $+0.0004$ | +0.0101 |
|  | -0.42 | -0.011 | +0.0003 | +0.0094 |
|  | -0.21 | -0.004 | +0.0002 | +0.0094 |
|  | 0 | +0.001 | +0.0001 | +0.0092 |
|  | +0.20 | +0.005 | +0.0001 | +0.0093 |
|  | +0.41 | +0.011 | +0.0000 | +0.0096 |
|  | +0.61 | +0.015 | +0.0001 | +0.0101 |
|  | +0.82 | +0.020 | 0 | +0.0106 |
|  | +1.03 | +0.027 | -0.0002 | +0.0107 |
|  | +1.23 | +0.031 | -0.0003 | +0.0111 |
| 2.00 | -2.05 | -0.046 | +0.0006 | +0.0105 |
|  | -1.08 | -0.022 | +0.0001 | +0.0086 |
|  | 0 | +0.001 | 0 | +0.0079 |
|  | +1.03 | $+0.027$ | -0.0002 | +0.0089 |
|  | +2.05 | +0.049 | -0.0006 | +0.0110 |
|  | +3.07 | +0.077 | -0.0013 | +0.0136 |
|  | +4. 10 | $+0.103$ | -0.0018 | +0.0171 |
|  | +5.13 | $+0.131$ | -0.0022 | +0.0211 |
|  | +6.16 | +0.160 | -0.0026 | +0.0264 |
|  | +7.19 | +0.189 | -0.0029 | +0.0328 |
|  | +8.22 | +0.216 | -0.0030 | +0.0401 |
|  | +9.25 | +0.243 | -0.0031 | +0.0489 |
|  | +10.28 | +0.271 | -0.0032 | +0.0585 |
|  | +11.31 | +0.298 | -0.0032 | +0.0693 |
|  | +12.34 | +0.325 | -0.0033 | +0.0810 |
|  | -4. 10 | -0.105 | +0.0018 | +0.0160 |
|  | $-4.10$ | -0.104 | +0.0018 | +0.0159 |
|  | -3.08 | -0.076 | +0.0013 | +0.0130 |
|  | -2.05 | -0.049 | +0.0007 | +0.0105 |
|  | -1.04 | -0.042 | +0.0009 | +0.0091 |
|  | 0 | -0.001 | 0 | +0.0081 |

## RESULTS - WING 10

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | -2.00 | -0.099 | -0.0003 | 0.0170 |
|  | -1.08 | -0.072 | +0.0012 | 0.0143 |
|  | -0.01 | -0.041 | 0.0028 | 0.0123 |
|  | 1.01 | -0.012 | 0.0043 | 0.0108 |
|  | 1.98 | $+0.017$ | 0.0062 | 0.0106 |
|  | 3.05 | 0.042 | 0.0078 | 0.0105 |
|  | 4.07 | 0.063 | 0.0098 | 0.0111 |
|  | 5.09 | 0.084 | 0.0121 | 0.0126 |
|  | 6.12 | 0.117 | 0.0145 | 0.0157 |
|  | 7.14 | 0.152 | 0.0165 | 0.0200 |
|  | 8.17 | 0.185 | 0.0190 | 0.0259 |
|  | 9.20 | 0.224 | 0.0216 | 0.0338 |
|  | 10.23 | 0.264 | 0.0252 | 0.0438 |
|  | 11.27 | 0.307 | 0.0293 | 0.0555 |
|  | 12.31 | 0.351 | 0.0333 | 0.0695 |
| 0.70 | -2.03 | -0.103 | 0.0003 | 0.0175 |
|  | -1.05 | -0.073 | 0.0017 | 0.0148 |
|  | -0.01 | -0.041 | 0.0032 | 0.0128 |
|  | 1.02 | -0.012 | 0.0047 | 0.0108 |
|  | 2.00 | +0.016 | 0.0061 | 0.0103 |
|  | 3.09 | 0.044 | 0.0074 | 0.0105 |
|  | 4.12 | 0.068 | 0.0095 | 0.0116 |
|  | 5.15 | 0.093 | 0.0117 | 0.0137 |
|  | 6.19 | 0.122 | 0.0139 | 0.0167 |
|  | 7.23 | 0.157 | 0.0159 | 0.0219 |
|  | 8.28 | 0.194 | 0.0180 | 0.0275 |
|  | 9.33 | 0.236 | 0.0207 | 0.0360 |
|  | 10.39 | 0.277 | 0.0238 | 0.0473 |
|  | 11.45 | 0.321 | 0.0274 | 0.0600 |
|  | 12.50 | 0.367 | 0.0298 | 0.0745 |
| 0.85 | -2. 10 | -0.108 | 0.0019 | 0.0179 |
|  | -1.11 | -0.078 | 0.0030 | 0.0146 |
|  | -0.01 | -0.034 | 0.0036 | 0.0121 |
|  | 1.03 | -0.013 | 0.0054 | 0.0113 |
|  | 2.02 | 0.016 | 0.0065 | 0.0112 |
|  | 3.11 | 0.044 | 0.0078 | 0.0121 |
|  | 4.15 | 0.069 | 0.0098 | 0.0130 |
|  | 5.19 | 0.096 | 0.0118 | 0.0134 |
|  | 6.24 | 0.128 | 0.0139 | 0.0165 |
|  | 7.29 | 0.164 | 0.0157 | 0.0214 |
|  | 8.35 | 0.205 | 0.0172 | 0.0288 |
|  | 9.41 | 0.249 | 0.0193 | 0.0385 |
|  | 10.48 | 0.295 | 0.0219 | 0.0503 |
|  | 11.55 | 0.341 | 0.0246 | 0.0638 |
|  | 12.62 | 0.389 | 0.0270 | 0.0803 |

(Conta.)

TABTE 3 (Contd.)

| M | $\alpha$ | $\mathrm{C}_{\mathrm{L}}$ | $\mathrm{C}_{\mathrm{m}}$ | $\mathrm{C}_{\text {D }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.90 | -2.09 | -0.111 | 0.0027 | 0.0179 |
|  | -1.05 | -0.079 | 0.0036 | 0.0146 |
|  | -0.01 | -0.045 | 0.0045 | 0.0123 |
|  | 1.03 | -0.012 | 0.0058 | 0.0107 |
|  | 2.02 | +0.014 | 0.0068 | 0.0101 |
|  | 3.11 | 0.044 | 0.0078 | 0.0104 |
|  | 4.14 | 0.066 | 0.0101 | 0.0114 |
|  | 5.19 | 0.098 | 0.0116 | 0.0136 |
|  | 6.23 | 0.129 | 0.0136 | 0.0167 |
|  | 7.28 | 0.164 | 0.0154 | 0.0214 |
|  | 8.34 | 0.207 | 0.0171 | 0.0290 |
|  | 9.40 | 0.251 | 0.0186 | 0.0387 |
|  | 10.46 | 0.298 | 0.0207 | 0.0506 |
|  | 11.53 | 0.346 | 0.0227 | 0.0651 |
|  | 12.59 | 0.394 | 0.0246 | 0.0814 |
| 0.94 | -2.09 | -0.114 | 0.0032 | 0.0182 |
|  | -1.05 | -0.082 | 0.0039 | 0.0148 |
|  | -0.01 | -0.047 | 0.0047 | 0.0122 |
|  | 1.03 | -0.014 | 0.0058 | 0.0107 |
|  | 2.02 | +0.014 | 0.0065 | 0.0102 |
|  | 3.11 | 0.044 | 0.0079 | 0.0106 |
|  | 4.15 | 0.071 | 0.0095 | 0.0118 |
|  | 5.19 | 0.099 | 0.0114 | 0.0139 |
|  | 6.24 | 0.130 | 0.0135 | 0.0169 |
|  | 7.29 | 0.169 | 0.0147 | 0.0220 |
|  | 8.35 | 0.212 | 0.0159 | 0.0298 |
|  | 9.41 | 0.258 | 0.0176 | 0.0398 |
|  | 10.47 | 0.304 | 0.0189 | 0.0520 |
|  | 11.54 | 0.356 | 0.0203 | 0.0672 |
|  | 12.60 | 0.404 | 0.0217 | 0.0837 |
| 0.98 | -2.09 | -0.122 | 0.0048 | 0.0190 |
|  | -1.10 | -0.085 | 0.0050 | 0.0152 |
|  | 0 | -0.048 | 0.0054 | 0.0126 |
|  | 1.03 | -0.015 | 0.0056 | 0.0112 |
|  | 2.03 | 0.016 | 0.0071 | 0.0107 |
|  | 3.12 | 0.044 | 0.0081 | 0.0109 |
|  | 4.16 | 0.072 | 0.0101 | 0.0121 |
|  | 5.20 | 0.099 | 0.0118 | 0.0141 |
|  | 6.25 | 0.133 | 0.0136 | 0.0175 |
|  | 7.30 | 0.170 | 0.0145 | 0.0228 |
|  | 8.31 | 0.218 | 0.0146 | 0.0309 |
|  | 9.41 | 0.264 | 0.0148 | 0.0415 |
|  | 10.47 | 0.312 | 0.0156 | 0.0540 |
|  | 11.53 | 0.362 | 0.0157 | 0.0693 |
|  | 12.59 | 0.409 | 0.0166 | 0.0856 |

(Contd.)

TABLE 3 (Contd.)

| M | $\alpha$ | ${ }^{\text {c }}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{\text {D }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.02 | $\begin{array}{r} -2.07 \\ -1.08 \\ 0 \\ 1.04 \\ 2.03 \\ 2.03 \\ 3.12 \\ 4.16 \\ 5.20 \\ 6.24 \\ 7.29 \\ 8.33 \\ 9.38 \\ 10.44 \\ 11.50 \\ 12.55 \end{array}$ | -0.121 -0.086 -0.050 -0.015 0.017 0.017 0.048 0.076 0.108 0.140 0.184 0.228 0.275 0.326 0.370 0.422 | 0.0080 0.0077 0.0071 0.0071 0.0071 0.0072 0.0074 0.0087 0.0090 0.0106 0.0093 0.0090 0.0084 0.0078 0.0077 0.0084 |  |
| 1.42 | $\begin{array}{r} -1.95 \\ -0.97 \\ +0.12 \\ +1.15 \\ +2.18 \\ +3.22 \\ +4.25 \\ +5.29 \\ +6.33 \\ +7.37 \\ +8.41 \\ +9.46 \\ +10.51 \\ +11.56 \\ +12.61 \\ +0.12 \end{array}$ | $\begin{aligned} & -0.098 \\ & -0.066 \\ & -0.034 \\ & -0.003 \\ & +0.027 \\ & +0.055 \\ & +0.083 \\ & +0.112 \\ & +0.144 \\ & +0.179 \\ & +0.217 \\ & +0.257 \\ & +0.296 \\ & +0.334 \\ & +0.372 \\ & -0.034 \end{aligned}$ |  |  |
| 1.61 | $\begin{array}{r} -1.85 \\ -0.87 \\ +0.22 \\ +1.25 \\ +2.28 \\ +3.31 \\ +4.35 \\ +5.38 \\ +6.32 \\ +7.45 \\ +8.49 \\ +9.54 \\ +10.59 \\ +11.64 \\ +12.69 \\ +0.22 \end{array}$ | $\begin{aligned} & -0.083 \\ & -0.052 \\ & -0.022 \\ & +0.007 \\ & +0.034 \\ & +0.062 \\ & +0.087 \\ & +0.115 \\ & +0.145 \\ & +0.176 \\ & +0.212 \\ & +0.248 \\ & +0.285 \\ & +0.318 \\ & +0.353 \\ & -0.023 \end{aligned}$ |  |  |

(Contd.)

TABLE 3 (Contd.)

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{\text {D }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.82 | -2.05 | -0.080 | +0.0070 | +0.0164 |
|  | -1.07 | -0.055 | +0.0065 | $+0.0138$ |
|  | +0.01 | -0.025 | +0.0059 | +0.0122 |
|  | +1.04 | +0.001 | +0.0055 | +0.0114 |
|  | +2.07 | +0.029 | +0.0050 | +0.0114 |
|  | +3.10 | +0.056 | +0.0045 | +0.0122 |
|  | +4.13 | +0.080 | +0.0043 | +0.0137 |
|  | +5.17 | +0. 107 | $+0.0040$ | +0.0165 |
|  | +6.20 | +0.134 | +0.0038 | +0.0200 |
|  | +7.24 | +0.164 | +0.0035 | +0.0245 |
|  | +8.28 | +0.196 | +0.0032 | +0.0307 |
|  | +9.32 | +0.229 | +0.0030 | +0.0391 |
|  | +10.36 | +0.261 | +0.0032 | +0.0486 |
|  | +11.41 | +0.293 | +0.0034 | +0.0592 |
|  | +12.45 | +0.324 | +0.0038 | +0.0711 |
|  | $+4.13$ | +0.079 | +0.0044 | $+0.0136$ |
|  | +4.34 | +0.084 | $+0.0044$ | +0.0142 |
|  | +4.55 | +0.090 | $+0.0043$ | +0.0148 |
|  | +4.75 | +0.095 | $+0.0043$ | +0.0153 |
|  | +4.96 | +0.101 | +0.0042 | +0.0158 |
|  | +5.17 | +0.106 | +0.0041 | +0.0164 |
|  | +0.01 | -0.028 | +0.0063 | +0.0123 |
| 2.00 | -2.04 | -0.079 | +0.0066 | +0.0157 |
|  | -1.07 | -0.053 | +0.0061 | +0.0135 |
|  | +0.01 | -0.026 | +0.0056 | +0.0116 |
|  | +1.04 | +0 | +0.0051 | +0.0106 |
|  | +2.06 | +0.026 | $+0.0046$ | +0.0104 |
|  | +3.08 | +0.051 | +0.0043 | +0.0109 |
|  | +4.11 | +0.074 | +0.0040 | +0.0129 |
|  | +5.13 | +0.099 | +0.0038 | +0.0156 |
|  | +6.16 | +0.125 | +0.0035 | +0.0188 |
|  | +7.19 | +0.153 | +0.0032 | +0.0233 |
|  | +8.22 | +0.183 | +0.0030 | +0.0289 |
|  | +9.25 | +0.211 | +0.0031 | +0.0360 |
|  | +10.29 | +0.241 | +0.0032 | +0.0450 |
|  | +11.32 | +0.270 | +0.0037 | +0.0547 |
|  | +12.36 | +0.298 | +0.0039 | +0.0655 |
|  | +4. 11 | +0.076 | +0.0041 | +0.0127 |
|  | +4.11 | +0.074 | +0.0041 | +0.0122 |
|  | +4.62 | +0.087 | +0.0039 | +0.0139 |
|  | +5.13 | +0.100 | +0.0038 | +0.0155 |
|  | +5.65 | +0.113 | +0.0036 | +0.0173 |
|  | +3.60 | +0.063 | +0.0041 | $+0.0116$ |
|  | +0.01 | -0.027 | +0.0057 | +0.0116 |

TABLE 4

## RESUTMS - WING 11

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | $\begin{array}{r} -2.04 \\ -1.52 \\ 0 \\ 1.02 \\ 1.99 \\ 3.06 \\ 4.08 \\ 5.11 \\ 6.13 \\ 7.16 \\ 8.19 \\ 9.22 \\ 10.26 \\ 11.30 \\ 12.33 \end{array}$ | $\begin{array}{r} -0.063 \\ -0.036 \\ -0.009 \\ +0.013 \\ 0.028 \\ 0.057 \\ 0.092 \\ 0.125 \\ 0.156 \\ 0.193 \\ 0.224 \\ 0.264 \\ 0.309 \\ 0.355 \\ 0.394 \end{array}$ | $\begin{array}{r} -0.0022 \\ -0.0006 \\ 0.0012 \\ 0.0031 \\ 0.0053 \\ 0.0069 \\ 0.0087 \\ 0.0102 \\ 0.0133 \\ 0.0155 \\ 0.0189 \\ 0.0219 \\ 0.0246 \\ 0.0286 \\ 0.0328 \end{array}$ | 0.0118 0.0105 0.0095 0.0098 0.0105 0.0122 0.0145 0.0185 0.0234 0.0303 0.0372 0.0472 0.0592 0.0737 0.0882 |
| 0.70 | $\begin{array}{r} -2.07 \\ -1.08 \\ 0 \\ 1.03 \\ 2.01 \\ 3.10 \\ 4.14 \\ 5.18 \\ 6.22 \\ 7.26 \\ 8.31 \\ 9.37 \\ 10.42 \\ 11.48 \\ 12.54 \end{array}$ | -0.068 -0.041 -0.013 0.011 0.034 0.063 0.094 0.127 0.163 0.200 0.233 0.282 0.324 0.368 0.415 | $\begin{array}{r} -0.0018 \\ -0.0001 \\ 0.0016 \\ 0.0032 \\ 0.0049 \\ 0.0065 \\ 0.0086 \\ 0.0105 \\ 0.0129 \\ 0.0147 \\ 0.0174 \\ 0.0198 \\ 0.0229 \\ 0.0260 \\ 0.0282 \end{array}$ | 0.0121 0.0106 0.0097 0.0097 0.0104 0.0125 0.0154 0.0184 0.0237 0.0313 0.0386 0.0502 0.0628 0.0770 0.0938 |
| 0.85 | $\begin{array}{r} -2.09 \\ -1.09 \\ 0 \\ 1.04 \\ 2.03 \\ 3.12 \\ 4.17 \\ 5.22 \\ 6.27 \\ 7.33 \\ 8.39 \\ 9.45 \\ 10.51 \\ 11.58 \\ 12.65 \end{array}$ | $\begin{aligned} & -0.072 \\ & -0.043 \\ & -0.014 \\ & 0.011 \\ & 0.037 \\ & 0.065 \\ & 0.098 \\ & 0.133 \\ & 0.171 \\ & 0.211 \\ & 0.252 \\ & 0.296 \\ & 0.340 \\ & 0.387 \\ & 0.432 \end{aligned}$ | $\begin{array}{r} -0.0011 \\ 0.0003 \\ 0.0016 \\ 0.0034 \\ 0.0050 \\ 0.0066 \\ 0.0081 \\ 0.0098 \\ 0.0115 \\ 0.0133 \\ 0.0141 \\ 0.0172 \\ 0.0193 \\ 0.0214 \\ 0.0260 \end{array}$ | 0.0125 0.0107 0.0097 0.0099 0.0104 0.0122 0.0147 0.0189 0.0246 0.0326 0.0416 0.0531 0.0661 0.0815 0.0986 |

(Contd.)

TABLE 4 (Contd. $)$

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.90 | -2.08 | -0.073 | -0.0010 | 0.0125 |
|  | -1.09 | -0.043 | +0.0003 | 0.0106 |
|  | 0 | -0.015 | 0.0019 | 0.0098 |
|  | 1.04 | 0.011 | 0.0033 | 0.0095 |
|  | 2.03 | 0.036 | 0.0051 | 0.0107 |
|  | 3.12 | 0.066 | 0.0066 | 0.0119 |
|  | 4.16 | 0.099 | 0.0080 | 0.0147 |
|  | 5.21 | 0.134 | 0.0093 | 0.0189 |
|  | 6.26 | 0.173 | 0.0112 | 0.0250 |
|  | 7.31 | 0.213 | 0.0122 | 0.0327 |
|  | 8.37 | 0.255 | 0.0139 | 0.0419 |
|  | 9.1 .3 | 0.299 | 0.0155 | 0.0535 |
|  | 10.49 | 0.344 | 0.0174 | 0.0670 |
|  | 11.55 | 0.389 | 0.0190 | 0.0823 |
|  | 12.62 | 0.439 | 0.0207 | 0.1005 |
| 0.94 | -2.08 | -0.078 | -0.0009 | 0.0125 |
|  | -1.09 | -0.045 | 0 | 0.0107 |
|  | 0 | -0.015 | 0.0014 | 0.0098 |
|  | 1.04 | 0.011 | 0.0030 | 0.0094 |
|  | 2.03 | 0.038 | 0.0047 | 0.0105 |
|  | 3.12 | 0.067 | 0.0061 | 0.0120 |
|  | 417 | 0.102 | 0.0074 | 0.0151 |
|  | 5.22 | 0.137 | 0.0088 | 0.0194 |
|  | 6.27 | 0.175 | 0.0102 | 0.0251 |
|  | 7.32 | 0.216 | 0.0112 | 0.0331 |
|  | 8.38 | 0.259 | 0.0124 | 0.0428 |
|  | 9.43 | 0.305 | 0.0135 | 0.0546 |
|  | 10.49 | 0.348 | 0.0150 | 0.0680 |
|  | 11.55 | 0.398 | 0.0159 | 0.0844 |
|  | 12.61 | 0.447 | 0.0165 | 0.1028 |
| 0.98 | -2.08 | -0.077 | -0.0003 | 0.0130 |
|  | -1.09 | -0.046 | 0.0006 | 0.0110 |
|  | 0 | -0.016 | 0.0015 | 0.0098 |
|  | 1.05 | 0.010 | 0.0033 | 0.0096 |
|  | 2.03 | 0.036 | 0.0048 | 0.0106 |
|  | 3.13 | 0.069 | 0.0059 | 0.0124 |
|  | 4.17 | 0.101 | 0.0072 | 0.0151 |
|  | 5.22 | 0.140 | 0.0080 | 0.0199 |
|  | 6.27 | 0.180 | 0.0089 | 0.0261 |
|  | 7.32 | 0.223 | 0.0092 | 0.0344 |
|  | 8.37 | 0.266 | 0.0096 | 0.042 .3 |
|  | 9.43 | 0.312 | 0.0098 | 0.0565 |
|  | 10.48 | 0.358 | 0.0098 | 0.0707 |
|  | 11.53 | 0.406 | 0.0095 | 0.0870 |
|  | 12.59 | 0.458 | 0.0086 | 0.1059 |

(Contd.)

TABLE 4 (Contd.)

| M | $\alpha$ | $c_{L}$ | $\mathrm{C}_{\mathrm{m}}$ | $C_{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.02 | -2.07 | -0.086 | 0.0025 | 0.0158 |
|  | -1.08 | -0.049 | 0.0025 | 0.0133 |
|  | +0.01 | -0.017 | 0.0027 | 0.0123 |
|  | 1.05 | 0.009 | 0.0037 | 0.0115 |
|  | 2.03 | 0.038 | 0.0045 | 0.0128 |
|  | 3.12 | 0.071 | 0.0048 | 0.0147 |
|  | 4.17 | 0.108 | 0.0051 | 0.0178 |
|  | 5.21 | 0.145 | 0.0048 | 0.0228 |
|  | 6.26 | 0.188 | 0.0047 | 0.0295 |
|  | 7.30 | 0.231 | 0.0042 | 0.0377 |
|  | 8.35 | 0.275 | 0.0042 | 0.0479 |
|  | 9.40 | 0.317 | 0.0047 | 0.0593 |
|  | 10.46 | 0.360 | 0.0047 | 0.0730 |
|  | 11.51 | 0.405 | 0.0047 | 0.0889 |
|  | 12.57 | 0.455 | 0.0048 | 0.1072 |
| 1.42 | -0.39 | -0.022 | +0.0049 | +0.0122 |
|  | +0.13 | -0.011 | +0.0048 | +0.0121 |
|  | +1.16 | +0.017 | +0.0046 | +0.0120 |
|  | +2.19 | +0.045 | $+0.0042$ | +0.0129 |
|  | +3.23 | +0.074 | +0.0038 | +0.0148 |
|  | +4.27 | +0.108 | +0.0034 | +0.0178 |
|  | +5.31 | +0.141 | +0.0029 | +0.0221 |
|  | +6.35 | +0.176 | +0.0026 | +0.0278 |
|  | +7.39 | +0.211 | +0.0022 | +0.0349 |
|  | +8.44 | +0.247 | +0.0021 | +0.0434 |
|  | +9.48 | +0.284 | +0.0018 | +0.0539 |
|  | +10.53 | +0.320 | +0.0017 | +0.0653 |
|  | +11.58 | +0.356 | +0.0020 | +0.0783 |
|  | +12.63 | +0.392 | +0.0018 | +0.0927 |
|  | +0.13 | -0.010 | +0.0047 | +0.0118 |
| 1.61 | -1.84 | -0.059 | +0.0052 | +0.0131 |
|  | -0.86 | -0.030 | +0.0048 | +0.0119 |
|  | +0.23 | -0.004 | +0.0047 | +0.0113 |
|  | +1.26 | +0.022 | +0.0044 | +0.0113 |
|  | +2.29 | +0.048 | +0.0040 | +0.0125 |
|  | +3.22 | +0.074 | +0.0035 | +0.0140 |
|  | +4.35 | +0.106 | +0.0030 | +0.0170 |
|  | +5.39 | +0.137 | +0.0026 | +0.0210 |
|  | +6.43 | +0.170 | +0.0022 | +0.0266 |
|  | +7.47 | +0.203 | +0.0019 | +0.0334 |
|  | +8.52 | +0.236 | +0.0017 | +0.0413 |
|  | +9.56 | +0.269 | +0.0018 | +0.0506 |
|  | +10.61 | +0.303 | +0.0017 | +0.0617 |
|  | +11.65 | +0.335 | +0.0018 | +0.0735 |
|  | +12.70 | +0.367 | +0.0020 | +0.0868 |
|  | +0.27 | -0.005 | +0.0047 | +0.0113 |

(Conti.)

TABIE 4 (Conti.)

| M | $\alpha$ | $\mathrm{C}_{\text {L }}$ | $\mathrm{C}_{\mathrm{m}}$ | $\mathrm{C}_{\text {D }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.82 | -1.99 | -0.060 | +0.0052 | +0.0129 |
|  | -1.06 | -0.031 | +0.0048 | +0.0112 |
|  | -0.44 | -0.018 | +0.0045 | +0.0107 |
|  | +0.02 | -0.007 | +0.0045 | +0.0104 |
|  | $+0.54$ | +0.006 | +0.0043 | +0.0102 |
|  | +1.05 | +0.018 | +0.0042 | +0.0104 |
|  | +1.57 | +0.030 | +0.0040 | +0.0109 |
|  | +2.08 | +0.044 | +0.0037 | +0.0117 |
|  | +2.65 | +0.056 | +0.0035 | +0.0124 |
|  | +3.11 | +0.071 | +0.0032 | +0.0132 |
|  | +4.15 | +0.099 | +0.0027 | +0.0159 |
|  | +5.18 | +0.128 | +0.0024 | +0.0199 |
|  | +6.22 | +0.159 | +0.0021 | +0.0250 |
|  | +7.26 | +0.190 | +0.0019 | +0.0313 |
|  | +8.30 | +0.220 | +0.0017 | +0.0386 |
|  | +9.39 | +0.249 | +0.0018 | +0.0473 |
|  | +10.38 | +0.280 | +0.0019 | +0.0573 |
|  | +11.47 | +0.310 | +0.0020 | +0.0687 |
|  | +12.46 | +0.340 | +0.0023 | +0.0808 |
|  | +0.02 | -0.008 | +0.0044 | $+0.0104$ |
| 2.00 | -1.99 | -0.063 | $+0.0047$ | +0.0122 |
|  | -1.06 | -0.036 | +0.0043 | +0.0106 |
|  | -0. 50 | -0.023 | $+0.0041$ | +0.0101 |
|  | $+0.01$ | -0.013 | $+0.0041$ | +0.0097 |
|  | +0. 53 | 0 | +0.0041 | +0.0088 |
|  | +1.04 | +0.012 | +0.0040 | +0.0091 |
|  | +1.55 | +0.023 | +0.0040 | +0.0097 |
|  | +2.06 | +0.037 | $+0.0037$ | +0.0105 |
|  | +2.58 | +0.047 | +0.0036 | +0.0112 |
|  | +3.09 | $+0.060$ | +0.0033 | +0.0122 |
|  | +3.09 | +0.060 | +0.0033 | +0.0124 |
|  | +4•11 | +0.087 | +0.0028 | +0.0149 |
|  | +5.14 | +0.115 | +0.0025 | +0.0185 |
|  | +6.17 | +0.142 | +0.0022 | +0.0230 |
|  | +7.20 | +0.171 | +0.0021 | +0.0289 |
|  | +8.23 | +0.198 | +0.0022 | +0.0355 |
|  | +9.26 | +0.226 | +0.0023 | +0.0432 |
|  | +10.30 | +0.254 | +0.0024 | +0.0523 |
|  | +11.33 | +0.280 | +0.0026 | +0.0621 |
|  | +12.36 | +0. 308 | +0.0029 | +0.0735 |
|  | +0.01 | -0.012 | +0.0041 | +0.0095 |
|  | +0.01 | -0.012 | +0.0041 | +0.0095 |
|  | +0.53 | -0.001 | $+0.0042$ | +0.0087 |

## SYMBOLS

| A | aspect ratio |
| :---: | :---: |
| $C_{L}$ | lift coefficient |
| $C_{D}$ | drag coefficient |
| $C_{m}$ | pitching moment coefficient moment/qS $\overline{\bar{c}}$ referred to $0.66 c_{0}$ |
| $\overline{\bar{c}}$ | aerodynamic mean chord |
| $c_{0}$ | root chord |
| M | Mach number |
| p | planform parameter $=S / 2 c_{0} S_{T}$ |
| q | free stream kinetic pressure |
| R | Reynolds number |
| S | wing area |
| $S_{T}$ | wing semi-span |
| $x, y, z$ $\alpha$ | coordinates non-dimensionalised w.r.t. co angle of incidence |
| $\stackrel{\rightharpoonup}{\alpha}$ | attachment incrdence |
| $\beta$ | $\sqrt{M^{2}-1}$ |

Superscript - attachment candıtions

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Fig. I Planform of wings


Fig. 2 Sections of wings


Fig 3 Design chordwise variation of cross-load: Wings 10 and II


Fig. 4 Wing 9. Variation of drag coefficient with incidence near attachment, $\mathrm{M}=1 \cdot 8$. Carborundum 0.007 in high


Fig. 5 Azo benzene photographs showing transitional boundary layer. Wing 9. $M=2.0 \alpha=0^{\circ}$ carborundum $0.007^{\text {" }}$ high


Fig. 6 Wing 9. Variation of lift coefficient with incidence


Fig. 6 contd.


Fig. 7 Wing 1O. Variation of lift coefficient with incidence

b $M=1.42$ to 2.00

Fig 7 contd.


Fig. 8 Wing II. Variation of lift coefficient with incidence

b $M=1.42$ to 2.00

Fig. 8 contd.


Fig. 9 Wings $9-11$. Comparison of lift development from the attachment incidence

b $M=1.02$ to $M=2.00$

Fig. 9 contd.


Fig. 10 Wing 9. Variation of pitching moment coefficient with lift coefficient


Fig.II Wing 10. Variation of pitching moment coefficient with lift coefficient


Fig. 12 Wing II. Variation of pitching moment coefficient with lift coefficient


Fig. 15 Wings 10 and II. Variation of zero lift pitching moment
with Mach Number


Fig. 16 Wing $1 O$ and II.Variation of trimmed lift coefficient with Mach No at supersonic speeds


Fig. 17 Wing 9.Variation of drag coefficient with lift coefficient.


Fig. 17 contd.


Fig. 18 Wing 1O. Variation of drag coefficient with lift coefficient




Fig 19 contd.



Fig 21 Variation of drag due to lift factor with lift coefficient and Mach number

Fig 21 contd



Fig. 22 Variation of drag due to lift factor with slenderness parameter



Fig 23 Variation of lift/drag ratio with lift coefficient



Fig. 23 contd


Fig. 24 Variation of roughness shock wave positions with incidence $\mathrm{M}=2 . \mathrm{O}$ carborundum $\mathrm{O} . \mathrm{O} 2 \mathrm{O}$ in high.
$81=W$ a6pe-6u!pम ay

$070=0=0$
$0.0=0$
$o^{*} 9=0$

$o+1=y=0$
$o t=0$
$\mathrm{V}_{2}=0-20$
$\mathrm{ob}^{2}=0$
$00=-0$
$00=m$
ponulua) $s \tau^{6!}$ !!

$0 z^{\circ} 9=2-2$
$0^{+} 0 y=2$



$O * C=2-0$
$o C^{*}=2=2$

$\begin{array}{ll}9 & \\ 0 & 0 \\ \text { gi } & \\ \text { in } & 6 \\ 0 & 0 \\ 3 & 0\end{array}$
1
Q1 4
$0=$
0 -
popnpuos sc'64





\&
8
${ }_{0} k=2=0$
\&
$\begin{array}{ll}4 & 8 \\ 4\end{array}$


Fig. 26 Wing 9. Oil flow photographs

(a) $a_{0}=7.3^{\circ}$

(b) $a=8.3^{\circ}$

Fig. 27 Wing 10. Oil flow photographs, $M=1.4$

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The wings were designed by slender wing theory for attached flow along the leading-edge at particular values of lift and pitching moment. The design and measured attachment conditions agreed fairly well. The non-linear lift developed could be related with the type of vortex development above the attachment incidence.

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Ilott, G.P.
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Ilott, G.P.
THE LONGITUDINAL CHARACTERISTICS OF THREE SLENDER "MILD OGEE" WINGS AT MACH NUXIBERS FROM 0.4 T0 2.0

Wind tunnel measurements of 11 ft , pitching moment and drag on one plane and two cambered wings of "mild ogee" planform ( $p=8 / 15$ ) are reported. The se measurements are supplemented by vapour screen and oil flow observations.

The wings were designed by slender wing theory for attached flow along the leading-edge at particular values of lift and pitahing moment. The design and measured attachment conditions agreed fairly mell. The non-linear lift developed could be related with the type of vortex development above the attachment incidence.

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[^0]:    * Replaces R.A.E. Tech. Report 67202 - A.R.C. 30166

[^1]:    *Although the centre line camber, $\mathrm{C}(\mathrm{X})$, for \#ing 10 was determined algebralcally, $\mathrm{C}(\mathrm{X})$ for wing 11 was found numerically.

[^2]:    *Incidence for the cambered wangs is defined as the ancidence of the plane containing the wang apex and the centre section of the wing tralling-edge.

[^3]:    *In these experiments a television camera mounted on the model sting recorded the vapour screen. Photographs of the televasion pletures for one station on the wing are reproduced in Fig. 25.
    fit is possible that this "array" is really an array of subsidıary vortex cores along the main vortex sheet and thus a three-dimensional counterpart to similar arrays observed by Pierce ${ }^{15}$ on two-dimensional plates moved in still air. The present investigation could not go far enough to establish the nature of the vortex development in sufficient detail.

