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# Tests at Subsonic and Supersonic Speeds on a Slender Cambered Wing with Fin, Underwing Engine Nacelles and Trailing-Edge Controls 

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## Summary.

The tests were made in the $8 \mathrm{ft} \times 8 \mathrm{ft}$ wind tunnel at R.A.E. Bedford on a $1 / 36$ scale model of a possible design for a supersonic transport aircraft. The wing camber was designed, using slender-wing theory, to have attached flow at a $C_{L}$ of 0.02 , and a shift forward of the centre of pressure, relative to the uncambered wing, of $0.3 \bar{c}$ at $C_{L}=0.1$.
The present investigation was restricted to determining the effects of the fin and nacelles on the longitudinal stability, drag, and lateral stability of the wing and to measurements of effectiveness, drag, and hinge moment of the controls.

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## 1. Introduction.

Tests have been made in the $8 \mathrm{ft} \times 8 \mathrm{ft}$ tunnel on a model which represented a possible layout for a supersonic transport aircraft (Bristol type 198). The model was of $1 / 36$ scale, and identical to one a series of seven smaller scale ( $1 / 90$ ) models ( 500 series $)^{1}$, which had been designed to investigate various area distributions and camber shapes. The design philosophy behind these models has been put forward in Ref. 1, but it may be helpful to give a summary of the important details here. Three of the seven models were uncambered, and of these, one was a datum wing-body combination with the body designed simply on full scale payload requirements with no attempt at minimisation of drag. The other two uncambered models featured body waisting, and in one case the nose was lengthened to shift the centre of gravity of the full scale aircraft forward, and so ease the trimming problem. Of the four cambered models, three were designed by linear theory at $M=2.2$ with various combinations of design $C_{L}$ and centre-of-pressure shift, and using the lengthened body with optimised area distribution. The model, which is the subject of these tests, was identical to the remaining cambered model, which used the unlengthened body with optimised area distribution. The camber was designed by slender-wing theory so that the wing would have attached flow at a $C_{L}$ of 0.02 , and a stable separated flow over the upper surface at the cruise $C_{L}$ of 0.1 . At the cruise $\mathrm{C}_{L}$ the forward centre-of-pressure shift (relative to the uncambered wing) was designed to be $0.3 \bar{c}$. Previous experience with wing camber designed by slender-wing theory ${ }^{2}$ has shown that approximately only half the design centre-of-pressure shift is realised at $M=2 \cdot 2$, so that the present model has been designed intentionally for a larger centre of pressure shift than is necessary to trim at $C_{L}=0.1$ and $M=2 \cdot 2$.

In previous designs ${ }^{2,3}$ there have been varying degrees of integration between wing and body, and the body volume has usually been added symmetrically above and below the wing camber line. With the present series of designs there is no attempt at integration and asymmetric distribution of body volume is accepted.

The longitudinal stability and drag of the present model without fin or nacelles and with undeflected controls (defined here as the basic wing-body) has been investigated by Cook ${ }^{4}$, and the present tests are concerned with the measurement of the lateral stability of the basic wing-body, the effectiveness, drag, and hinge moment of the trailing-edge controls, and the effect on longitudinal stability, drag, and lateral stability of adding a stabilising fin and underwing engine nacelles.

## 2. Experimental Details.

### 2.1. Description of the Model.

The wing leading edge has constant sweepback ( $68^{\circ}$ ) over most of the span and is smoothly faired into streamwise tips. The trailing edge is unswept (Fig. 1). At the intersection of the wing leading edge and the body, the wing blends smoothly into a triangular cross-section strake which extends forward to the nose of the model, thus giving a sharp leading edge from nose to tail (Fig. 2). Clearly shown in Fig. 2 is the leading-edge droop of the wing, intended to maintain attached flow at the design $C_{L}$, and the asymmetric distribution of body volume about the wing camber line. Details of the chordwise camber relative to the OH datum of both wings and body are shown in Fig. 3. The OH datum, which is also shown as a reference datum in Figs. 1 to 5 , is aligned in the direction of the free stream when the aircraft is at its design attitude (design $C_{L}=0.02$ ). The OV datum is simply the aircraft centreline.

The engine nacelles are of near rectangular cross-section with scalloped undersurfaces, and are mounted in an underwing location between the inboard and outboard trailing-edge controls (Fig. 4). In order to obtain the correct external flow and internal mass flow at the design Mach number ( $M=2 \cdot 2$ ), a constant area duct was provided through the nacelle.

The planform details of the controls are shown in Fig. 4. Both controls are hinged at their leading edges, the outboard control having a horn type aerodynamic balance projecting ahead of the hinge line. On the port wing, each control is supported from the wing at the hinge line by two strain-gauged beams, which are entirely enclosed within the wing contour. In addition to measuring the control hinge moment, these beams serve to set the control at the required angle; thus it was necessary to manufacture and strain gauge two beams per control for each control setting. The controls on the starboard wing are identical to
those on the port wing except that the beams are not strain gauged. The hinge-line gaps were sealed for all the tests.

Apart from the control hinge moments, all model forces and moments were measured on a sixcomponent internal strain-gauge balance supported by a sting. It was necessary to distort the rear of the model in order to accommodate the sting, the distortion taking the form of a cylindrical shroud which for the majority of tests ended at the wing trailing edge (Fig. 5). For the tests with the fin on, a longer shroud was used, the shroud also serving as a suitable mounting for the fin. The fin is of cropped 'double-delta' planform and 6 per cent thick biconvex section outboard of the kink in the leading edge. Inboard of the kink, the biconvex section is modified by a single wedge extension which blends into the biconvex section ahead of the point of maximum thickness. The fin shape and location are correctly representative of full scale, so that a small area of the fin near the root is shielded by the sting shroud (Fig. 5).

Fig. 6a shows the area distribution of the basic wing-body non-dimensionalized with respect to the total length, $L$, and the effects on this of the sting shroud, the fin, and the nacelles. The component area distributions of the fin and one nacelle are also shown separately in Fig. 6b. The cross-section area of the nacelle is taken to be the total cross-section area of the nacelle less the stream tube entry area at the cowl lip.

The full scale aircraft was designed to have a variable geometry canopy. In the supersonic configuration the only effect the canopy has on the fuselage profile is a small step on the upper surface of the nose at 13.4 per cent $L$, just noticeable in Fig. 1. For take off and landing the upper surface profile ahead of the canopy would retract into the fuselage to improve the pilots' view. Although the present model was tested at subsonic speeds ( $M=0.275$ ) there was no provision for varying the canopy geometry and the supersonic configuration was tested throughout.

The main part of the model (aft of 50 per cent $L$ ), including the nacelles, was made of steel with the nose and fin constructed of glass fibre and epoxy resin on steel cores.

The principal dimensions of the model, and the setting angles of unloaded controls are given in Tables 1 and 2 respectively.

### 2.2. Test Conditions.

The majority of tests on this model were made at supersonic speeds, at Mach numbers of $1.4,1.8$ and 2.2. For the tests on the configuration with engine nacelles $M=1.4$ was omitted. The range of sting incidences covered by the tests was from $-4^{\circ}$ to $+12^{\circ}$, and for the basic wing-body, the wing-body with fin, and the wing-body with nacelles, lateral components were measured at sideslip angles of $-2^{\circ}$ to $+6^{\circ}$ at selected incidences. In addition to the above tests at supersonic speeds, the basic wing-body and the wing-body with fin were tested at $M=0.275$ at incidences of $0^{\circ}$ to $20^{\circ}$ and sideslip angles of $-2^{\circ}$ to $+6^{\circ}$.

At all Mach numbers the Reynolds number was $2 \times 10^{6}$ per foot (approximately $6 \times 10^{6}$ based on root chord, $c_{0}$ ).

All other details of the test programme are given in Table 3.
Bands of distributed roughness (carborundum grains with an effective height of between 0.008 and 0.012 inches) were applied to the leading edges of the wing, fin, and nacelles and the body nose in order to produce a turbulent boundary layer over the model.

### 2.3. Corrections Applied to Results.

Each configuration has been tested with the model both 'upright' and 'inverted' in the tunnel airstream, and the results presented in this note are a mean of these two sets of measurements. This procedure eliminates from the results any effects of flow deflection or flow curvature, apart from the effect of flow curvature on drag.

The model attitude has been corrected for deflections of the balance and sting, and the trailing-edge control setting angles have been corrected for deflection of the support beams.

A tunnel constraint correction has been applied to the model incidence, drag, and pitching-moment
coefficients at $M=0 \cdot 275$. The corrections were derived from the theory of Ref. 5 and the corrected values are given by:

$$
\begin{align*}
\alpha \text { correct } & =\alpha+0.579 C_{L}  \tag{1}\\
C_{D} \text { correct } & =C_{D}+0.00810 C_{L}^{2}  \tag{2}\\
C_{m} \text { correct } & =C_{m}+0.00132 C_{L} \tag{3}
\end{align*}
$$

where $\alpha$ (in degrees), $C_{L}, C_{D}$, and $C_{m}$ are the uncorrected values.
Although the axial force measurements have been corrected for the difference between the base pressure and free-stream static pressure, no other corrections for the presence of the sting shroud have been applied to the results.

The drag results of the configuration with nacelles have been corrected to allow for the internal drag of the nacelles. The location of the nacelles on the present model is such as to allow several possible definitions of internal drag, dependent upon the location of the upstream reference plane. The correction applied to the present drag results is that for the upstream reference plane located at the apex of the intake sideplates at 0.785 L or 2.5 per cent ahead of the cowl lip. The correction was determined from the results of two pressure surveys, one over the region of duct inlet with the nacelle removed and the other over the duct exit with the nacelle in position. Pitot pressures were measured on the starboard wing and static pressures on the port wing. The most usual alternative form of the correction to the present one is with the upstream reference plane in the free stream, and both the above forms of the correction are shown in Fig. 7. The two forms of the correction are only significantly different at negative incidence. Over most of the incidence range the difference between them is of the same order as the experimental accuracy (see section 4). The correction to pitching moment is negligible and has been ignored. No measurements of nacelle internal flow were made with the wing yawed, so that it was not possible to determine any corrections to yawing moment.

## 3. Presentation of Results.

The usual coefficient form of presentation of model forces and moments is used throughout (see list of symbols), and unless otherwise stated the coefficients refer to a stability system of axes. The moment reference centre is at 50 per cent $\bar{c}$ ( $12 \cdot 305$ inches forward of the trailing edge). The tangent definition of incidence $(\alpha)$ and the sine definition of sideslip $(\beta)$ is used throughout:

$$
\begin{align*}
& \tan \alpha=\tan \theta \cos \phi  \tag{4}\\
& \sin \beta=\sin \theta \sin \phi \tag{5}
\end{align*}
$$

where $\theta$ is the total incidence and $\phi$ is the roll angle from the trailing edge horizontal. Unless otherwise stated the model incidence is measured relative to the wing root chord (see Table 1).

Because of the duplication of experimental points by taking measurements with the model both 'upright' and 'inverted', only the mean faired curves are shown in the figures, the experimental points being omitted in the interests of clarity.
4. Accuracy of Results.

At supersonic speeds the absolute experimental accuracy of the meaned results is estimated to be:

$$
\begin{array}{ll}
C_{L} & \pm 0.002 \\
C_{m} & \pm 0.0002 \\
C_{D} & \pm 0.0002 \\
C_{Y} & \pm 0.001
\end{array}
$$

$$
\begin{aligned}
C_{n} & \pm 0.0002 \\
C_{l} & \pm 0.0004 \\
C_{H} & \pm 0.002 .
\end{aligned}
$$

At $M=0.275$ due to the low kinetic pressure the above values should be doubled. The accuracy of differences is probably slightly better than the above figures.

An unpublished flow survey has shown that the Mach number variation over the region of the model is within the following limits:

| $M_{\text {nominal }}$ | Variation |
| :---: | :---: |
| 0.275 | $\pm 0.001$ |
| 1.4 to 2.2 | $\pm 0.005$. |

Model incidence and sideslip angles and control setting angles are all accurate to $\pm 0.03 \mathrm{deg}$.

## 5. Discussion of Results.

The analysis of the longitudinal stability and drag results for the basic wing-body is given elsewhere ${ }^{4}$ and will not be discussed here.

### 5.1. Effect of Fin and Nacelles on Longitudinal Stability and Drag.

At $M=0.275$ the effect of the fin on lift, pitching moment and drag is small (Figs. 8, 9 and 10), and in view of the relatively large values of $C_{L}$ and $C_{D}$ which would be experienced by an aircraft at take off and landing ( $C_{L} \bumpeq 0.50, C_{D} \bumpeq 0.11$ ), is of little concern.

At supersonic speeds where the cruise $\mathrm{C}_{L}$ is relatively small ( $0 \cdot 1$ ) the effect of the fin is more significant. At low incidence addition of the fin produces a small decrease in $C_{L}$, whereas at high incidence this is partly or wholly offset by a slight increase in lift-curve slope with the fin present (Fig. 11). This latter effect is probably due to the extra length of sting shroud which is capable of taking carry-over lift from the wing. The nacelles give an increase of lift at all incidences. The different sense of the lift increment at low incidences resulting from the addition of fin and nacelles is due entirely to the location of these components, above and below the wing respectively.

At zero $C_{L}$ the effects on $C_{m}$ of fin and nacelles are consistent with their respective lift increments and locations (Fig. 12). Adding the fin produces a nose-up change in $C_{m}$ whereas the nacelles give a nose down change. In both cases a slight rearward movement of aerodynamic-centre position occurs. In the case of the nacelles this may well be due to the additional plan area located behind the wing trailing edge (Fig. 4). With the fin, the aerodynamic-centre movement is probably not a genuine fin effect but due to the extra length of sting shroud, which was inferred to be the cause of the increased lift-curve slope with this configuration. The full scale body radius aft of the trailing edge is much less than that of the sting shroud (Fig. 5) and consequently will support much less carry-over lift, and in addition, the contracting afterbody will develop some negative lift which will move the aerodynamic-centre position forwards, so that its true location 'fin on' may well be further forward than indicated by Fig. 12.

Fig. 13 shows the effect of fin and nacelles on the drag polar.
5.1.1. Incremental loads due to fin and nacelles. The incremental values of $C_{L}$ and $C_{m}$ at $\alpha=2.90^{\circ}$ (wing trailing edge at zero incidence) due to the fin have been replotted in Fig. 14a and $b$.

Using linear theory, Jones ${ }^{6}$ has calculated the lift and pitching moment produced at supersonic speeds by a delta fin of biconvex section mounted on a flat wing with unswept trailing edge. The only restriction imposed in Ref. 6 on fin location was that the Mach line from the fin root leading edge should not intersect the wing leading edge. Using the charts of Ref. 6 and a simplified model of the fin, shown in Fig. 15, an attempt has been made to estimate the lift and pitching moment produced by the present fin. The wing was assumed to be flat and the sting shroud and body were ignored. Initially the lift and pitching moment were determined for a delta fin of $58^{\circ} 33^{\prime}$ leading edge sweepback located with its trailing edge in the same
position as that of the present fin (Fig. 15). A correction to allow for the dorsal extension of the present fin was then obtained by assuming that the additional fin volume could be represented by a delta fin of $79^{\circ} 18^{\prime}$ leading edge sweepback and biconvex section with its trailing edge situated 10.295 inches ahead of the trailing edge of the present fin. The accuracy of prediction is not very good (Fig. 14a and b), the measured values of $\Delta C_{L}$ and $\Delta C_{m}$ due to the fin being smaller than the theoretical values. Since the cropped tip of the fin lies behind the wing trailing edge it cannot influence the induced lift and pitching moment, so that the main sources of error in the prediction are the effect of the dorsal extension on the pressure field from the main part of the fin, and the effect of the sting shroud extension in carrying additional induced load aft of the wing trailing edge. The sense of this additional induced load is almost certainly such as to increase $C_{L}$ and decrease $C_{m}$ which could account for the disparity.
The contribution of skin friction to the drag increment of the fin was calculated by determining the skin-friction drag of a series of chordwise strips and integrating these across the span of the fin. The boundary layer was assumed to be turbulent from the fin leading edge, and the skin-friction coefficient of each strip was calculated by the intermediate enthalpy method using the Prandtl-Schlichting formula.
Estimates of the fin wave drag were obtained from the charts of standard methods. A simplified planform shape was assumed, with the forward part of the double-delta planform being ignored. These estimates of fin drag coefficient are shown in Fig. 14 c in comparison with the measured drag-coefficient increment due to the fin. At both subsonic and supersonic speeds there is evidence of favourable interference between wing and fin, the measured drag coefficients being much lower than predicted.
The increments in $C_{L}$ and $C_{m}$ at $\alpha=2.9^{\circ}$ and in minimum $C_{D}$, due to the nacelles, are shown in Fig. 16. The skin friction drag coefficient of the nacelles, shown in Fig. 16c, was estimated as the skin-friction drag of the external wetted area of the nacelle under the wing, less the skin-friction drag of the wing covered by the nacelles (from apex of intake sideplates to wing trailing edge), plus the small additional skin-friction drag of the upper surface of the nacelles projecting beyond the wing trailing edge. The method of estimation of the skin-friction drag coefficient was identical to that for the fin, except that here it was considered accurate enough to base the skin-friction coefficients on the mean Reynolds numbers involved rather than perform integrations. Simple estimates of nacelle wave-drag coefficients were obtained from the charts of standard methods. The nacelle area distribution was used to calculate an equivalent quasi-cylindrical half-body of revolution having a parabolic profile. The estimated dragcoefficient increment is much lower than measured (Fig. 16c). Although the wave-drag estimate is very approximate, it is not likely to be in error by the amount shown in Fig. 16c so that there would appear to be a significant amount of unfavourable interference.

### 5.2. Trailing-Edge Controls.

Deflection of the trailing-edge controls as elevators has only a small effect on lift-curve slope (Figs. 17 and 20a) or aerodynamic-centre position (Figs. 18 and 21a), so that the increments in $C_{L}$ and $C_{m}$ are virtually independent of $\alpha$ and $C_{L}$ respectively. The increase in $C_{D}$ due to deflecting the controls as elevators is shown by Figs. 19 and 22a. Differential movement of the outboard controls (as ailerons) has no effect on $C_{L}$ or $C_{m}$ (Figs. 20b and 21 b respectively), and the increase in $C_{D}$ is shown by Fig. 22b. The rollingmoment coefficient increment due to a constant aileron angle decreases slightly with increasing incidence (Fig. 23). At $\alpha=2.90^{\circ}$, where the wing trailing edge is horizontal (see Table 1), the increments in $C_{L}, C_{m}$ and $C_{l}$ vary linearly with control-setting angle within the range of setting angles tested (Figs. 24, 25 and 26).
5.2.1. Control effectiveness. The supersonic linear-theory solutions for $d C_{L} / d \eta_{c}$ and $d C_{m} / d \eta_{c}$ of a rectangular control in an inboard location are given in Ref. 7, and a method for correcting this lineartheory solution for control-thickness effects is suggested by Tucker and Nelson in Ref. 8. Although this correction applies strictly only to rectangular planform or two-dimensional wings, an analysis of hinge moments on rectangular controls ${ }^{9}$ showed that the experimental correlation was improved when this thickness factor obtained from Ref. 8 was used to correct the results for all types of planform. In view of this result, the linear-theory estimates of $d C_{L} / d \eta_{c}$ and $d C_{m} / d \eta_{c}$ obtained for the inboard controls have been corrected for thickness in a similar manner. The linear-theory estimate of Ref. 7 assumes full lift carry-over at the outboard edges of the control (lift induced on the wing by the control pressure field
within the Mach cone from the control leading edge tip). There is some experimental evidence ${ }^{10}$ to show that only part of this carry-over lift is realized in practice so that a second estimate of $d C_{L} / d \eta_{c}$ and $d C_{m} / d \eta_{c}$ has been obtained assuming the control tips to be unbounded by the wing. This solution (labelled 'no lift carry-over' in Figs. 28 and 29) is identical to that for an isolated rectangular wing ${ }^{11}$ and it has been corrected for thickness effects in the manner of the solution with full lift carry-over. Both estimates have been corrected for sting-shroud interference using the linear-theory factors of Ref. 12.
An estimate has also been made of $d C_{L} / d \eta_{c}$ for the outboard controls. The linear-theory perturbation potential along the control trailing edge was calculated using Evvards method ${ }^{13}$, and the overall lift obtained by numerical integration. Because of the amount of work involved only one solution (with full lift carry-over at the inboard edge of the control) was obtained, and this has been corrected for controlthickness effects as for the inboard control.
The derivatives $d C_{l} / d \xi_{c}, d C_{L} / d \eta_{c}$ and $d C_{m} / d \eta_{c}$ are plotted against Mach numbers in Figs. 27, 28 and 29 respectively. At $M=1.4$ the experimental results fall between the two estimates whereas at $M=2.2$ both estimates are too large. These results are in reasonable agreement with previous measurements of control effectiveness on a slender wing ${ }^{14}$.
Measurements of the lift-effectiveness parameter $d C_{L c} / d \eta_{c}\left(C_{L c}\right.$ is the lift coefficient based on control area) for rectangular and near rectangular controls have been collected from various sources, and are plotted in the form $1 / A_{c} d C_{L c} / d \eta_{c}$ against $A_{c} \sqrt{M^{2}-1}$ in Fig. 30. Figs. 30a and 30b show the results before and after correction for control thickness and body interference respectively. With the exception of the results from Ref. 15 there is fair correlation with a scatter of approximately $\pm 10$ per cent on the mean curve. The corrections for control thickness and body interference improve the agreement with theory although the measured results still tend to be slightly low.
5.2.2. Drag due to control deflection. Theoretical expressions have been derived ${ }^{14}$ for the effect of control deflection on the minimum drag coefficient and the lift coefficient at minimum drag. They are reproduced below:

$$
\begin{align*}
& \Delta C_{D m}=a_{2}^{\prime} \eta_{c}^{2}+\left(\frac{a_{1}^{\prime}+a_{2}^{\prime}+a_{2}^{\prime \prime}}{a_{1}}\right) \eta_{c}\left(C_{L m}-\Delta C_{L}\right)-\frac{\pi A}{K}\left[\frac{\eta_{c}\left(a_{1}^{\prime}+a_{2}^{\prime}+a_{2}^{\prime \prime}\right)}{2 a_{1}}\right]^{2}  \tag{6}\\
& \Delta C_{L m}=\left(a_{2}^{\prime}+a_{2}^{\prime \prime}\right) \eta_{c}-\frac{\pi A}{K}\left[\eta_{c} \frac{\left(a_{1}^{\prime}+a_{2}^{\prime}+a_{2}^{\prime \prime}\right)}{2 a_{1}}\right] \tag{7}
\end{align*}
$$

where $\Delta C_{D m}$ and $\Delta C_{L m}$ are the increments in the minimum drag coefficient and in the lift coefficient at minimum drag respectively, $\eta_{c}$ is the control setting angle in radians, positive when the trailing edge is deflected downwards,
$A$ the wing aspect ratio,
$K$ the drag due to lift factor of the wing $\left(=\pi A \frac{d C_{D}}{d C_{L}^{2}}\right)$,
$C_{L m}$ is the lift coefficient at minimum drag with the controls undeflected,
$\Delta C_{L}$ is the lift on the wing when it is at zero incidence (measured relative to the undeflected controls).

$$
\left.\begin{array}{l}
a_{1}=\left(d C_{L} / d \alpha\right) \text { wing per rad } \\
a_{1}^{\prime}=\left(d C_{L} / d \alpha\right) \text { control per rad } \\
a_{2}^{\prime}=\left(d C_{L} / d \eta_{c}\right) \text { control per rad } \\
a_{2}^{\prime \prime}=\left(d C_{L} / d \eta_{c}\right) \text { control carry-over lift per rad }
\end{array}\right\} \text { based on wing area. }
$$

Measured values of $a_{1}, K, C_{L m}$ and $\Delta C_{L}$ obtained with the controls undeflected have been used in the estimation of $\Delta C_{D m}$ and $\Delta C_{L m}$ together with linear theory values of $a_{1}^{\prime}$ derived using Evvards' approximate method ${ }^{16}$ and corrected for thickness effects in the manner of Ref. 8. Two calculations of $\Delta C_{D m}$ and $\Delta C_{L m}$ were performed, one using linear-theory values of $a_{2}^{\prime}$ and $a_{2}^{\prime \prime}$ corrected for control thickness and body-interference effects (section 5.2.1) and another with the present measured values of $a_{2}^{\prime}$ with $a_{2}^{\prime \prime}$ assumed to be zero.

Only fair agreement between theory and experiment is obtained using the theoretical values of $a_{2}^{\prime}$ and $a_{2}^{\prime \prime}$ (Figs. 31 and 32), which is not surprising in view of the disparity shown in Fig. 28 between experimental values of $d C_{L} / d \eta_{c}$ and theory with full lift carry-over. Somewhat better agreement is obtained, especially for the outboard controls, when measured values of $a_{2}^{\prime}$ are used. However, although it may be smaller than theory predicts, it is unlikely that $a_{2}^{\prime \prime}$ will be zero, so that part of the difference may be due to the use of incorrect values of $a_{1}^{\prime}$ in the calculations.
5.2.3. Control hinge moment. The variation of $C_{B}$ with $\alpha$ is slightly non-linear for both inboard and outboard controls (Figs. 33 and 34); however the variation with control setting angle $\eta_{c}$ is linear (Fig. 35). Analysis of the hinge-moment derivative $d C_{H} / d \eta_{c}$ for rectangular controls on various wings ${ }^{9}$ has demonstrated good experimental correlation and agreement with theory at supersonic speeds. The analysis of Ref. 9 was applied to the prediction of $d C_{H} / d \eta_{c}$ for the inboard controls on the present model. The lineartheory estimate for $d C_{H} / d \eta_{c}$ was first obtained assuming that the outboard edges of the control are free (the lift distribution along the control trailing edge becomes zero at the tip and there is no lift carry-over onto the adjacent wing). This estimate was then corrected for control thickness in the manner of Ref. 8 and for interference effects from the strong shroud using the linear theory factors of Ref. 12. Fig. 36a shows that good agreement is obtained between theory and experiment, the predicted values of $d C_{H} / d \eta$ being approximately $6 \frac{1}{2}$ per cent too high.

Although estimated values of $d C_{L} / d \eta_{c}$ for the outboard control were obtained using Evvards' method ${ }^{13}$, the method was considered to be too laborious for the calculation of $d C_{H} / d \eta$. Czarnecki and Lord ${ }^{17}$ have shown that for controls with horn balances a linear relationship exists between $d C_{H} / d \eta$ and the ratio of the horn area (defined as that area ahead of the hinge line) to control total area. Using the method of Ref. 9 an estimate of $d C_{H} / d \eta$ was calculated for a rectangular control having the same area and span as the outboard control with its hinge line at the leading edge. The experimental results of Ref. 17 were used to obtain the horn area ratio for complete balance ( 39 per cent). This ratio was assumed to be constant for all Mach numbers and was used to obtain a factor which was then applied to the rectangular control value of $d C_{H} / d \eta$. Fig. 36b shows both the theoretical curve for the rectangular control and the factored curve, but the measured values agree with the latter only at $M=2 \cdot 2$, falling between the two theoretical curves at lower Mach numbers. It would appear that a more thorough theoretical treatment is necessary in order to predict accurately the hinge-moment characteristics of controls with horn balances.

Evvards' approximate method ${ }^{16}$ was used to calculate linear-theory values of $d C_{H} / d \alpha$ for both inboard and outboard controls, the appropriate factor from Ref. 8 being applied to correct these for control thickness effects. For the inboard controls (Fig. 36c) the predicted values of $d C_{H} / d \alpha$ agree well with experiments; however the measured values of $d C_{H} / d \alpha$ for the outboard controls are in general much larger than theory and in addition they exhibit a large variation with incidence, possibly due to leading-edge flowseparation effects (Fig. 36d).

### 5.3. Lateral Stability and Fin Effectiveness.

5.3.1. Basic wing body. The main feature of the lateral-stability measurements at $M=0.275$ is the non-linear variation of $C_{Y}$ with $\beta$ (Fig. 37). The unusual behaviour of $C_{Y}$ at $\alpha=11.66^{\circ}$ could possibly be due to some asymmetric flow over the model. The same asymmetry is present with the fin on (section 5.3.2). At supersonic speeds non-linearities are present at high incidence (Fig. 38). The variation of $C_{n}$ and $C_{l}$ with $\beta$ at all speeds requires no comment (Figs. 37, 39, and 40).

The derivatives $y_{v}, n_{v}$ and $l_{v}$ defined as $\left(d C_{Y} / d \beta\right)_{\beta=0},\left(d C_{n} / d \beta\right)_{\beta=0}$ and $\left(d C_{l} / d \beta\right)_{\beta=0}$ respectively, where $\beta$ is in radians, are plotted in Fig. 41. At $M=0.275, y_{v}$ changes from negative to positive with increasing $\alpha$. This type of variation has been observed before ${ }^{14}$, and is thought to be due to flow separation effects (wing vortices becoming asymmetric under conditions of yaw). The slender-body theory estimate ${ }^{18}$ of $y_{v}$ at zero incidence is much too low (Fig. 41a), so that although the absence of a sting shroud full scale would probably result in a smaller $y_{v}$, it is not possible to calculate the size of the reduction. The value of $n_{v}$ for stability axes changes sign with increasing incidence (Fig. 41a), but this variation is due solely to the resolved component of $l_{v}$ referred to body axes, $n_{v}$ in body axes remaining constant. In general the slope of the $l_{v}$ with $\alpha$ curve is predicted by slender-body theory ${ }^{18}$ (flat-plate model), although as might be expected from the flat-plate assumptions this estimate does not give the correct value of $l_{v}$ at $\alpha=0^{\circ}$.

In general, at supersonic speeds both $y_{v}$ and $n_{v}$ increase slightly with increasing Mach number and there is no significant variation with incidence (Fig. 41b). The slender body estimate ${ }^{18}$ of $y_{v}$ is again much too low. $d l_{v} / d \alpha$ decreases with increasing Mach number and there are also slight variations with incidence. Linear theory estimates ${ }^{19}$ of $l_{v}$ referred to body axes at supersonic speeds have been obtained for the present wing. For these estimates the effect of camber, the presence of the body and the cropped wing tips were all ignored. The measured values of $d l_{v} / d \alpha$ at low incidence, where the wing flow is attached, are in fair agreement with theory at $M=1.4$ and 1.8 (Fig. 42) but the measured values at high incidence are all much less than predicted. At $M=2 \cdot 2$, the comparison between theory and experiment is poor at all incidences. As at subsonic speeds (Fig. 41) the correct value of $l_{v}$ at zero incidence was not predicted by the theory due to the flat-plate assumptions.
5.3.2. Effect of fin and nacelles. The plots of $C_{Y}, C_{n}$ and $C_{l}$ against $\beta$ are shown in Figs. 43 to 46 for the configuration with fin and in Figs. 47 to 49 for the configuration with nacelles. The majority of these results are straightforward, however, although the variation of $C_{Y}$ with $\beta$ at $M=0.275$ is more linear for the configuration with fin (Fig. 43), than for the basic wing-body (Fig. 37), the large positive value of $\mathrm{C}_{Y}$ at zero $\beta$ at $\alpha=11.66^{\circ}$ is still present.

The addition of the fin makes the wing laterally stable with the present cg position at all the Mach numbers tested (Figs. 50 and 52) and although $-l_{v}$ is increased at supersonic speeds (Fig. 53) there is a substantial reduction at $M=0.275$ at high incidence (Fig. 50). The nacelles increase $-y_{v}$ at all incidences (Fig. 51), but the effect on $n_{v}$ is much smaller (Fig. 52) due to the proximity of the nacelle centre of pressure to the moment reference centre.

The prediction of the lift-curve slope of the isolated fin presents some problems because of its planform shape. Linear theory estimates of $d C_{L} / d \alpha$ for a 'double-delta' fin, having the same root chord and leadingedge sweepback angles as the present fin but without the cropped tip, were obtained over a limited Mach number range ( 1.52 to 1.78 ) from the charts of Ref. 20. These values were then compared with others obtained by taking the lift-curve slopes of the rear delta (leading-edge sweepback $58^{\circ} 33^{\prime}$ ) and adjusting these to the larger reference area of the 'double-delta'. In other words, the lift on that part of a 'doubledelta' forward of the crank in the leading edge is assumed to be independent of the leading-edge sweepback forward of the crank. For slender shapes this is a reasonable assumption and in fact follows from slender body theory. Providing that the forward part of the double delta is small compared with the rest of the wing (as in the present case), then the lift on the rear of the wing will not be significantly affected by the shape of the forward part. Over this limited range of Mach number it was found that the two estimates of lift curve slope agreed to within 3 per cent. It was therefore decided that, for the present fin which has a cropped tip, only the second method would be used, that is, the lift-curve slope of a cropped delta with $58^{\circ} 33^{\prime}$ leading-edge sweepback would be adjusted to the reference area of the cropped 'double-delta', and that this method would be used for all Mach numbers.

Estimates of $\Delta y_{v_{\text {Fin }}}$, the increment in $y_{v}$ due to the fin, have been obtained using the above values of lift-curve slope and making allowance for interference between fin and sting shroud with the methods of Ref. 21. At $M=0.275$ this estimate is much too large ( 50 per cent) (Fig. 54 ), and much better agreement is obtained between experiment and a predicted value based on fin lift alone, i.e. a fin added to a reflection plane. At supersonic speeds the estimates based on the method of Ref. 21 are again much too large, in this case they are beyond the range of each graph and have been omitted from Fig. 55. The empirical
wing body interference factors from standard methods are somewhat smaller than the slender body factors of Ref. 21 but even these give estimates which are too large (Fig. 55). The fin lift alone estimates are slightly less than the measured values as at subsonic speeds. Because of this difficulty in accurately predicting the fin effect on $y_{v}$ no attempt has been made to predict the fin effect on either $n_{v}$ or $l_{v}$ (Figs. 56 and 57 respectively).

## 6. Conclusions.

Although the agreement between measured and predicted ${ }^{6}$ values of the lift and pitching-moment increments due to the fin was only fair, it was thought that this was because the theory was not fully representative of the present model.

Fair correlation was obtained between the measured lift effectiveness of the inboard controls and results from other sources including both part span and full span rectangular trailing edge controls. After suitable corrections for control thickness and control-body interference effects had been applied the experimental results were only slightly lower than the linear-theory estimate for a full-span rectangular control for $A_{c} \sqrt{M^{2}-1}>2$.

It was possible to estimate the drag due to the controls with fair accuracy providing that accurate values of the control lift effectiveness were used in the calculations.

Measured values of the hinge-moment derivatives $d C_{H} / d \alpha$ and $d C_{H} / d \eta$ for the inboard controls were in good agreement with theory, but for the outboard controls the agreement varied from fair to poor.

Slender-body theory was inadequate for predicting $y_{v}$ for the basic wing-body combination both at subsonic and supersonic speeds. Measured values of $d l_{v} / d \alpha$ were in good agreement at subsonic speeds with slender-body theory estimates and at low supersonic speeds and low incidences with linear-theory estimates.

It was not possible to estimate the contribution of the fin to $y_{v}$ with any accuracy.

right hand system of axes
$x$ positive backwards
$y$ positive to starboard
$z$ positive downwards
$\alpha \quad$ Incidence angle
$\beta \quad$ Sideslip angle
$\theta \quad$ Total incidence angle
$\phi \quad$ Roll angle measured from the trailing edge horizontal
$\eta_{c} \quad$ Control setting angle for controls deflected as elevators (positive trailing edge down)
$\xi_{c} \quad$ Control setting angle for controls deflected as ailerons (positive trailing edge up for port control, trailing edge down for starboard control)

Suffices
c Refers to control
m

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TABLE 1
Principal Dimensions of Model

| Overall length of model, $L$ | $56 \cdot 855 \mathrm{in}$ |
| :--- | :--- |
| Wing span, $b$ | $28 \cdot 093$ in |
| Wing root chord (gross wing) $C_{0}$ | $36 \cdot 789 \mathrm{in}$ |
| Wing standard mean chord (gross wing), $\bar{c}$ | $19 \cdot 390 \mathrm{in}$ |
| Wing aerodynamic mean chord (gross wing), $\bar{c}$ | $24 \cdot 610 \mathrm{in}$ |
| Wing reference area (gross wing), $S$ | 544.7 sq in |
| Distance of moment reference centre from wing trailing edge | $12 \cdot 305 \mathrm{in}$ |
| Incidence of wing-root chord relative to OH datum | $3^{\circ} 36^{\prime}$ |
| Incidence of sting-balance axis relative to OH datum | $4^{\circ} 20^{\prime}$ |
| Incidence of wing trailing-edge plane relative to OH datum | $0^{\circ} 42^{\prime}$ |
| Wing leading-edge sweepback | $68^{\circ}$ |
| Inboard control plan area | $11 \cdot 484 \mathrm{sq}$ in |
| Inboard control chord | $3 \cdot 350 \mathrm{in}$ |
| Inboard control mean included trailing-edge angle | $7 \cdot 30^{\circ}$ |
| Outboard control plan area | $15 \cdot 899 \mathrm{sq}$ in |
| Outboard control reference chord | $3 \cdot 150$ in |
| Outboard control mean included trailing-edge angle | $6.00^{\circ}$ |
| Fin plan area | 52.296 sq in |

TABLE 2
Setting Angles of Unloaded Controls

| Nominal settings | $0^{\circ}$ | $+3^{\circ}$ | $-3^{\circ}$ | $+6^{\circ}$ | $-6^{\circ}$ |
| :--- | :---: | :--- | :--- | :--- | :--- |
| Port outboard | $0^{\circ}$ | $+2.90^{\circ}$ | $-3.23^{\circ}$ | $+6.23^{\circ}$ | $-6.57^{\circ}$ |
| Port inboard | $0^{\circ}$ |  | $-3.05^{\circ}$ |  | $-6.53^{\circ}$ |
| Starboard outboard | $0^{\circ}$ | $+3.32^{\circ}$ | $-3.20^{\circ}$ | $+6.42^{\circ}$ | $-6.38^{\circ}$ |
| Starboard inboard | $0^{\circ}$ |  | $-2.58^{\circ}$ |  | $-6.13^{\circ}$ |

Positive angles are for trailing edge deflected downwards.

TABLE 3

Test Details



Fig. 1. Basic wing-body shape.


Fig. 2. Details of wing-body cross-section.


Fig. 3. Chordwise camber details (relative to O.H. datum).


Fig. 4. Details of nacelles and controls.


Fig. 5. Details of fin and rear fuselage distortion.


Fig. 6. Cross-section area distribution.


Fig. 6 (contd.)

(a) $M=1 \cdot 8$

(b) $M=2 \cdot 2$

Fig. 7. Nacelle internal flow correction to axial force (one nacelle).


Fig. 8. Effect of fin on lift at subsonic speeds ( $M=0.275$ ).


Fig. 9. Effect of fin on pitching moment at subsonic speeds ( $M=0.275$ ).


Fig. 10. Effect of fin on drag at subsonic speeds
( $M=0.275$ ).


Fig.11. Effect of fin and nacelles on lift at supersonic speeds.


Fig. 12. Effect of fin and nacelles on pitching moment at supersonic speeds.


Fig. 13. Effect of fin and nacelles on drag at supersonic speeds.

(a) $\Delta C_{L}$ due to fin at $\alpha=2.90^{\circ}$

(b) $\Delta \mathrm{C}_{\mathrm{m}}$ due to fin at $\propto=2.90^{\circ}$

(c) $\Delta C_{D m}$ due to fin.

Fig. 14. Incremental loads due to fin.


Fig. 15. Model used for theoretical estimates of lift and pitching moment due to fin.

(a) $\Delta C_{L}$ due to nacelles $\alpha=2.90^{\circ}$

(b) $\Delta C_{m}$ due to nacelles $\alpha=2.90^{\circ}$

(c) $\Delta C_{D_{m}}$ due to nacelles

Fig. 16. Incremental loads due to nacelles.


Fig. 17. Effect of inboard controls as elevators on lift at supersonic speeds.


Fig. 18. Effect of inboard controls as elevators on pitching moment at supersonic speeds.


Fig. 19. Effect of inboard controls as elevators on drag at supersonic speeds.

(a) As elevators

Fig. 20. Effect of outboard controls on lift at supersonic speeds.

(b) As allerons

Fig. 20 (contd.)


Fig. 21. Effect of outboard controls on pitching moment at supersonic speeds.


Fig. 21 (contd.)


Fig. 22. Effect of outboard controls on drag at supersonic speeds.

(b) As ailerons

Fig. 22 (contd.)


(b) $M=1 \cdot 8$


Fig. 23. Effect of outboard controls as ailerons on rolling moment at supersonic speeds.




Fig. 25. Incremental pitching moment coefficients due to controls, $\alpha=2.90^{\circ}$.


Fig. 26. Incremental rolling moment due to outboard controls, $\alpha=2 \cdot 90^{\circ}$.


Fig. 27. Rolling moment effectiveness of outboard controls, $\alpha=2 \cdot 90^{\circ}$.


(b) Outboard controls

Fig. 28. Lift effectiveness of controls, $\alpha=2.90^{\circ}$.

(a) Inboard controls
$\underset{\infty}{\infty}$

(b) Outboard controls

FIG. 29. Pitching moment effectiveness of controls,

$$
\alpha=2.90^{\circ}
$$


(a) Experimental values not corrected for control thickness or body interference

(b) Experimental values corrected for control thickness and body interference
Fig. 30. Lift effectiveness correlation for various rectangular controls.


39
(a) Inboard controls as elevators

(b) Outboard controls as elevators


Fig. 31. Minimum drag increment due to control deflection.

(a) Inboard controls as elevators $-x-\eta_{c}=-3^{\circ}$ $-0-\eta_{\mathrm{c}}=-6^{\circ}$

(b) Outboard controls as elevators.

(c) Outboard controls as ailerons.

Fig. 32. Increment in lift at minimum drag due to control deflection.


Fig. 33. Effect of incidence and control setting on inboard control hinge moments.


Fig. 34. Effect of incidence and control setting on outboard control hinge moments.


Fig. 34 (contd.). Effect of incidence and control setting on outboard control hinge moments.

(a) Inboard controls

(b) Outboard controls

Fig. 35. Variation of control hinge moment coefficient with control setting, $\alpha=2 \cdot 90^{\circ}$.


Fig. 36. Variation with Mach No. of the hinge moment derivatives $\frac{d C_{H}}{d \eta}$ and $\frac{d C_{H}}{\mathrm{~d} \alpha}$.


Fig. 37. Variation of $C_{y}, C_{n}$ and $C_{l}$ with $\beta$ for the basic wing-body at subsonic speeds ( $M=0.275$ ).


Fig. 38. Variation of $C_{y}$ with $\beta$ for the basic wing-body at supersonic speeds.


Fig. 39. Variation of $C_{n}$ with $\beta$ for the basic wing-body at supersonic speeds.


Fig. 40. Variation of $C_{l}$ with $\beta$ for the basic wing-body at supersonic speeds.


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Fig. 41. Effect of incidence and Mach No. on the derivatives $y_{v}, n_{v}$ and $l_{v}$ for the basic wing-body.

(b) Supersonic speeds

Fig. 41 (contd.)


Fig. 42. Comparison of experimental and theoretical values of body axes $l_{v}$ at supersonic speeds.


Fig. 43. Variation of $C_{y}, C_{n}$ and $C_{l}$ with $\beta$ for the wing-body with fin (long shroud) at subsonic speeds ( $M=0.275$ ).


Fig. 44. Variation of $C_{y}$ with $\beta$ for the wing-body with fin (long shroud) at supersonic speeds.




Fig. 45. Variation of $C_{n}$ with $\beta$ for the wing-body with fin (long shroud) at supersonic speeds.


Fig. 46. Variation of $C_{l}$ with $\beta$ for the wing-body with fin (long shroud) at supersonic speeds.



Fig. 48. Variation of $C_{n}$ with $\beta$ for the wing-body with nacelles at supersonic speeds.


Fig. 49. Variation of $C_{l}$ with $\beta$ for the wing-body with nacelles at supersonic speeds.


Fig. 50. Effect of fin on $y_{v}, n_{v}$ and $l_{v}$ at subsonic speeds $(M=0.275)$.

(a) $M=1.4$

(c) $M=2.2$

Fig. 51. Effect of fin and nacelles on $y_{v}$ at supersonic speeds.


Fig. 52. Effect of fin and nacelles on $n_{v}$ at supersonic speeds.

(a) $M=1.4$

(b) $M=1.8$

(c) $M=2.2$

Fig. 53. Effect of fin and nacelles on $l_{v}$ at supersonic speeds.




Fig. 54. Increments in $y_{v}, n_{v}$ and $l_{v}$ due to the fin at subsonic speeds ( $M=0.275$ ).

(a) $M=1 \cdot 4$

(b) $M=1.8$


Fig. 55. Increments in $y_{v}$ due to fin and nacelles at supersonic speeds.


(b) $M=1 \cdot 8$


Fig. 56. Increments in $n_{v}$ due to fin and nacelles at supersonic speeds.

(c) $M=2 \cdot 2$
$\longrightarrow-\longrightarrow \ell_{V}$ due to fin and shroud extension ----x----- $\Delta e_{v}$ due to nacelles

Fig. 57. Increments in $l_{v}$ due to fin and nacelles at supersonic speeds.

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[^0]:    *Replaces R.A.E. Tech. Report No. 67217 (A.R.C. 30070 ).

