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Pressure-Plotting and Force Tests at Mach Numbers up to  $2 \cdot 8$  on an Uncambered Slender Wing of  $p = \frac{1}{2}$ ,  $s/c_0 = \frac{1}{4}$  ('Handley Page Ogee')

By A. L. COURTNEY and A. O. ORMEROD

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# Pressure-Plotting and Force Tests at Mach Numbers up to $2 \cdot 8$ on an Uncambered Slender Wing of $p = \frac{1}{2}$ , $s/c_0 = \frac{1}{4}$ ('Handley Page Ogee')

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COMMUNICATED BY THE DEPUTY CONTROLLER AIRCRAFT (RESEARCH AND DEVELOPMENT), MINISTRY OF AVIATION

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#### Summary.

Pressure-plotting and force tests have been made in the 8 ft  $\times$  8 ft Wind Tunnel, Bedford, on an uncambered slender wing of Collingbourne  $p = \frac{1}{2}$  ogee planform,  $s/c_0 = 0.25$ , 'Newby' area distribution, and varying cross-section shape representing an aircraft with a central passenger cabin blending into the wing. The model is one of two designed by Messrs. Handley Page under the auspices of the Supersonic Transport Aircraft Committee.

At zero lift, the wave-drag factor  $K_0$  is about 0.2 below the slender-theory value at all Mach numbers, due to the absence of a predicted rapid expansion towards the trailing edge, and further work on sting interference seems desirable. Apart from the difference near the trailing edge, the measured zero-lift pressures are in quite good agreement with slender or linear thin-wing theory.

At incidence, the pressure gradients are everywhere favourable behind the leading-edge vortex, and there is a large trailing-edge load which is not predicted by slender theory. The cruising centre of pressure is  $0.075c_0$  behind the low-speed aerodynamic centre at  $C_L = 0.5$ . At M = 2.2,  $K_0$  is 0.72 and the lift-dependent drag factor is 1.92, giving an estimated full-scale maximum L/D of 8.3 excluding engines.

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<sup>\*</sup> Replaces R.A.E. Tech. Note No. Aero. 2760-23 109.

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1. Introduction.

This report describes pressure-plotting and force tests made in the 8 ft  $\times$  8 ft Wind Tunnel, Royal Aircraft Establishment, Bedford, on the uncambered member of a pair of slender wings of Collingbourne  $p = \frac{1}{2}$  ogee planform designed by Messrs. Handley Page Ltd.<sup>1</sup> under the auspices of the Supersonic Transport Aircraft Committee. The wing has overall characteristics as follows:

L.E. shape 
$$\frac{s(x)}{s_T} = \frac{1}{2}x + x^2 - \frac{1}{2}x^5$$
$$s_T = 0.25c_0$$
$$p = \frac{\text{wing area}}{2s_T c_0} = 0.5$$
Aspect ratio  $A = 1$   
Area distribution  $S(x) = 0.0515 (x^2 - x^3)c_0^2$  ('Newby')  
Volume coefficient  $\tau = \frac{\text{Volume}}{(\text{wing area})^{3/2}} = 0.0343$ 

and with varying cross-section shapes, as shown in Fig. 1, representing a possible design with a central passenger cabin blending smoothly into the wing cross-section.

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Several factors entered into the choice of a configuration of this kind for wind-tunnel testing. When the tests were planned in 1958, some experimental evidence existed on delta and gothic planforms with simple rhombic or parabolic cross-sections, which had been tested mainly from the viewpoint of providing basic comparisons with theory. It seemed likely, however, that a practical aircraft would differ in several respects from the simple models that had so far been tested, e.g.:

- (i) it would have a more complicated cross-section shape with a thickened centre section for more efficient volume utilization,
- (ii) it would probably have a planform with streamwise tips, but with a lower value of 'p' than the 0.67 of the gothic wing, from considerations of balance and lift/drag ratio,
- (iii) it would have streamwise and spanwise camber to provide trim under cruising conditions whilst maintaining low lift-dependent drag and good flow development and lift for take-off and landing.

A detailed study<sup>2</sup> undertaken by Messrs. Handley Page examined these and other factors in the context of a practical aircraft able to accommodate its passengers and fuel, capable of being balanced, and with acceptable cruising efficiency and airfield performance, and this led to the proposals by Clark in Ref. 1 for uncambered and cambered models of p = 0.5 ogee planform, Newby area distribution and varying cross-section shape.

Since one aim of the tests was to investigate the adequacy of slender-wing design methods applied to more-complicated shapes than hitherto, it was decided that both models should be extensively pressure-plotted as well as force tested. The uncambered model, in addition to providing a datum for the camber tests, would show the effects on pressure distribution of the varying cross-section shape of a practical aircraft, and the cambered model would give information on the camber design methods<sup>1, 3, 4</sup> and show up any regions of adverse pressure gradient or flow separation due to camber.

This report gives, for the uncambered wing, the overall lift, drag and pitching-moment results from balance tests at Mach numbers from 0.3 to 2.8, together with a complete set of tabulated pressure-plotting results. The balance tests have been analysed to give zero-lift and lift-dependent drag factors, lift-curve slopes and centres of pressure. Some of the pressure-plotting results have been integrated to give zero-lift drag and streamwise and spanwise distributions of lift, and comparisons are made between the experimental pressure and load distributions and the predictions of slender and/or linear thin-wing theory.

#### 2. Details of Model and Tests.

#### 2.1. Model.

The main design parameters have been given in Section 1. Further details are given in Figs. 1 to 3 showing the general arrangement of the model, pressure-plotting orifices and sting shrouds, and the chordwise and spanwise section shapes. The spanwise section shapes can be expressed analytically; details are given in Ref. 1.

The model was constructed by the Aircraft Research Association, Bedford, and was made of steel with pressure-plotting tubes laid in surface slots filled with Araldite. Root chord was 60 inches and span 30 inches. The main pressure-plotting stations were on the centre-line and at 0.125, 0.33, 0.55 and 0.80 of the semi-span. These were on one surface only, the model being tested at positive and negative incidences to give upper-surface and lower-surface pressure distributions.

The model was sting-supported on its centre-line, and where the sting broke through the wing surface at the rear the model ordinates were distorted by the addition of a sting shroud covering the affected region. For the force tests the sting shroud consisted of a circular cylinder of 3.35 inches diameter, Fig. 1; for the main pressure-plotting tests a smaller sting was used and the shroud was an elliptic cylinder with axes of 2.9 inches and 2.6 inches normal to and parallel to the wing chord plane respectively.

#### 2.2. Tests.

The main balance and pressure-plotting tests were made at a Reynolds number of  $2 \times 10^6$  per foot, giving a Reynolds number of  $10^7$  on root chord; in addition, some tests were made at  $M = 2 \cdot 0$  with the Reynolds number reduced to  $10^6$  per foot.

In the balance tests, results were obtained at Mach numbers of 0.3, 1.4, 1.6, 1.7, 1.8, 2.0, 2.2, 2.4, 2.6 and 2.8, the incidence range (positive and negative) being generally  $0^{\circ}$  to  $12^{\circ}$  in steps of  $0.5^{\circ}$  or  $1^{\circ}$ . For these tests 60-grade carborundum grit was applied in a 0.5 inch band close to the leading edge on upper and lower surfaces in order to fix transition. Azobenzene sublimation tests at a Mach number of 2.4 showed that this was effective in producing transition at the test Reynolds number of  $2 \times 10^{6}$  per foot.

In the pressure-plotting tests, results were obtained at Mach numbers of  $1 \cdot 4$ ,  $1 \cdot 8$ ,  $2 \cdot 0$ ,  $2 \cdot 4$  and  $2 \cdot 8$ . With free transition and the small pressure-plotting sting shroud the incidences tested were 0, 1, 2, 3, 4, 6, 8 and 12 degrees (positive and négative). Some tests were also made with fixed transition and the larger sting shroud of the forces tests; these covered the same range of Mach numbers but were restricted to incidences of 0, 2, 4 and 6 degrees.

Oil-flow studies of the flow close to the upper surface were made at an incidence of 6 degrees at Mach numbers of 1.4, 2.0, 2.4 and 2.8, using a mixture of titanium oxide in oil.

## 3. Reduction and Presentation of Results.

#### 3.1. Balance Tests.

The overall lift, drag and pitching-moment results from the balance tests are given with some analysis in Figs. 4 to 11. In the  $C_L$  vs.  $\alpha$  curves of Fig. 4 the incidence has been corrected for sting deflection under load but not for possible downwash or curvature of the working-section flow. As can be seen in Figs. 4 to 7, the lift and pitching-moment curves do not pass exactly through the origin, and additional balance tests with the model (and axes) inverted give lift curves displaced on the opposite side of the origin, indicating some downwash or curvature in the tunnel flow, Fig. 5. The maximum error in incidence is less than  $0 \cdot 1^{\circ}$ . The effects of inverting the model on pitching moments are shown in Fig. 7, and here it can be seen that the mean values of  $C_{m0}$  (based on  $\bar{c}$ ) as between model upright and inverted are not zero but vary smoothly from about -0.0004 at M = 1.4 to -0.0002 at M = 2.8; this could be due to balance errors or to slight asymmetry in the model. The maximum measured difference in  $C_{m0}$  between model upright and inverted is 0.0012 at M = 1.6, representing, if genuine, a tunnel flow curvature equivalent to a  $\Delta C_{m0}$  of 0.0006 at this Mach number. Tunnel flow effects are also apparent in Fig. 11 giving the overall lift-dependent drag factor

$$K = \frac{\pi A (C_D - C_{D\,0})}{C_L^2} \tag{1}$$

which is different for positive and negative incidences. It is assumed that the true value of K is

given by the mean value for positive and negative incidences; the lower part of Fig. 11 shows that this gives very good agreement with the mean experimental curve of Ref. 7.

These departures from complete model and tunnel symmetry cause no difficulty in the interpretation and analysis of the present results for the symmetrical wing, and it is not proposed to pursue them further at this stage. Attention is drawn to them mainly because of their relevance in the testing and analysis of cambered wings where extra care is obviously needed; the apparent  $\Delta C_{m0}$  of 0.0006 at M = 1.6, for instance, represents about 15% of the design  $C_{m0}$  for a cambered version of the present wing.

Pitching-moment coefficients are based on the aerodynamic mean chord  $\bar{c}$  (= 0.62 $c_0$ ) and are quoted about an arbitrarily chosen axis at  $0.5\bar{c}$  (0.69 $c_0$ ) giving roughly neutral stability.

The overall drag coefficients have been adjusted to free-stream static pressure over the sting-shroud base area, and are presented both corrected and uncorrected for sting interference in Fig. 9. The sting interference has been estimated in two parts, namely

(i) an allowance for the rearward-facing wing surface masked by the cylindrical sting shroud, and

(ii) an allowance for the pressure field of the sting shroud based on some pressure-plotting measurements with and without sting on another wing.

1.4	1.8	2.0	2.4	2.8
0.00053	0.00040	0.00034	0.00029	0.00024
0.00072	0.00052	0.00045	0.00034	0.00029
0.00125	0.00092	0.00079	0.00063	0.00053
	1 · 4 0 · 00053 0 · 00072 0 · 00125	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		$1 \cdot 4$ $1 \cdot 8$ $2 \cdot 0$ $2 \cdot 4$ $0 \cdot 00053$ $0 \cdot 00040$ $0 \cdot 00034$ $0 \cdot 00029$ $0 \cdot 00072$ $0 \cdot 00052$ $0 \cdot 00045$ $0 \cdot 00034$ $0 \cdot 00125$ $0 \cdot 00092$ $0 \cdot 00079$ $0 \cdot 00063$

The estimated corrections for the balance sting are:

The overall corrections are quite large, amounting to about one-third of the zero-lift wave drag, and emphasize the need for more information on sting interference effects to improve the accuracy of estimation. In the present case it will be seen below that very good agreement is obtained between the integrated pressure drag and the wave drag derived from the balance tests using the above corrections and an estimated skin-friction drag, but in view of other uncertainties this cannot be taken as establishing the accuracy of the assumed sting corrections.

In Fig. 9, comparing the zero-lift wave drag derived from the balance tests with that obtained by integrating the measured pressure distributions, the sting correction for the pressure-plotting results consists only of the pressure-field term, the masking term being avoided by extrapolating the measured pressures to the centre-line as though the sting shroud were absent. Because of this, and the smaller size of the pressure-plotting sting, the corrections to the pressure-plotting results are only about half those given above for the balance tests.

#### 3.2. Pressure-Plotting Tests.

The measured values of  $10^3 C_p$  for all test Mach numbers and incidences are given in Tables 1 to 3. Table 1 gives the results with transition free and the small sting shroud, at  $R = 2 \times 10^6$  per foot; Table 2 shows the effect of reducing R to  $1 \times 10^6$  per foot at M = 2; and Table 3 gives the results with transition fixed and the large sting shroud, at  $R = 2 \times 10^6$  per foot. The results are tabulated against  $x/c_0$  at various spanwise positions, where x is the distance from the wing apex and  $c_0$  is the centre-line chord. Positive and negative incidences, respectively, refer to upper-surface and lower-surface pressures. The incidences are corrected for sting deflection under load, but not for tunnel flow effects.

A graphical presentation of some of the basic pressure-plotting data is given in Figs. 12 to 15 where  $C_p$  is plotted against  $x/c_0$  for the various pressure-plotting stations. In these figures the incidences are corrected for sting deflection but not for tunnel flow effects. In Figs. 16 to 21, however, involving loads per unit incidence, small corrections have been applied to the incidence values using Fig. 5. The effects on the basic pressure distributions are also small, as can be seen from Fig. 13 showing the effect at one pressure-plotting station of inverting the model at various Mach numbers.

Fig. 13 includes, of course, experimental inaccuracies as well as the direct effects of inverting the model. The accuracy of the capsule manometers used in these tests corresponds to a random scatter of about  $\pm 0.004$  in  $C_p$  on individual pressure readings. In addition, there is evidence of an effective zero error increasing or decreasing the general pressure level for any one scan of the manometers, i.e. at one incidence setting. This is due partly to variations in tunnel stagnation pressure, which was used as the common reference or datum pressure on one side of all the manometers, and partly, it is thought, to condensation in the working section. The results suggest a possible inaccuracy of about  $\pm 0.005$  in  $C_p$  due to this, on any set of readings at one incidence<sup>\*</sup>. No attempt has been made here to correct the basic data for this type of error, but in deriving the load distributions of Figs. 16 to 21 a watch has been kept for obvious discontinuities arising from this cause, and appropriate corrections included, making use also of comparisons between the integrated loadings and the balance measurements.

#### 3.3. Flow Visualization.

Photographs of oil flow on the upper surface at  $\alpha = 6 \cdot 4^{\circ}$  and various Mach numbers are given in Fig. 23. In these pictures transition is fixed on the port wing and free on the starboard wing; this does not seem to have produced any significant differences in the flow pattern at the test incidence. The difference in texture and flow development on the two sides is due to the use of different oils, castor oil on the starboard wing and the more usual mineral oil on the port wing; the castor oil gave the final well-scrubbed picture more quickly but remained sufficiently fluid to give a new pattern if conditions were altered. In this connection it should be noted that the  $M = 2 \cdot 4$  picture was produced immediately after the  $M = 2 \cdot 8$  picture, without a fresh application of oil; the traces of the  $M = 2 \cdot 8$  pattern which remain, particularly on the port wing, should therefore be ignored. It should also be remembered that there is considerable distortion in perspective in Fig. 23 due to the off-centre camera position.

#### 4. Overall Force Results.

#### 4.1. Lift.

Lift curves for Mach numbers of 0.3 to 2.8 are given in Fig. 4. The dashed lines represent the slope at zero incidence, and the amount of non-linear lift developed can be seen by the departure of the experimental points from these lines at high incidences. As is usually found, the non-linear

<sup>\*</sup> This type of inaccuracy will be reduced in future tests by using atmospheric pressure instead of tunnel stagnation pressure as the reference pressure for the manometers.

lift contribution decreases as Mach number increases, and on this wing it is relatively small beyond M = 2, i.e. when  $\beta s/c_0$  approaches and exceeds about 0.5. At low speed (M = 0.3) it is given quite closely by

$$\Delta C_L = 2 \cdot 5 \alpha^2.$$

The non-linear lift contribution at a typical cruising lift coefficient of 0.075 can be seen from Fig. 6 giving  $C_L/\alpha$  at  $C_L = 0$  and  $C_L = 0.075$  plotted against Mach number. It amounts to about 10% at M = 0.3 and M = 1.4, but by M = 2.0 it has fallen to only about 3%.

The zero-incidence lift slope, Fig. 6, is 1.41 at low Mach number, rising to about 1.65 transonically then falling steadily to 1.16 at M = 2.8. The transonic value is fairly close to that given by slender-wing theory,  $\pi A/2 = 1.57$ . Fig. 6 shows that at Mach numbers up to about 2 the lift slope agrees well with the linear-theory value for a cropped delta wing of the same aspect ratio and span<sup>8</sup>. At higher speeds, however, it falls below this value and becomes more nearly equal to that for a delta wing of the same aspect ratio<sup>8</sup>.

#### 4.2. Pitching Moments.

At low speed (M = 0.3) Fig. 7 shows that  $C_m$  varies linearly with  $C_L$  up to about  $C_L = 0.25$ , with a progressive reduction in stability at higher incidences. The low-speed aerodynamic centre, Fig. 8, is at  $0.639 c_0$  at low incidences, moving forward to  $0.624c_0$  at  $C_L = 0.5$ . The aerodynamiccentre position at  $C_L = 0.5$  is about  $0.03c_0$  further forward than the mean value suggested by an unpublished correlation by Spence in terms of planform centre of area  $(0.691c_0$  for the present wing).

At supersonic speeds, as discussed earlier, the  $C_m$  vs.  $C_L$  curves of Fig. 7 do not pass through the origin but exhibit  $C_{m\,0}$  values which are generally less than 0.0005. In view of the nominal symmetry of the model these non-zero  $C_{m\,0}$  values have been ignored in calculating the centres of pressure given in Fig. 8. The effect of this is small, however, and the centres of pressure obtained simply by dividing the uncorrected  $C_m$  by  $C_L$  in the normal manner do not differ by more than about  $0.005 c_0$  from the curve shown.

Another feature of Fig. 7 is the inflected shape of the  $C_m$  vs.  $C_L$  curves near  $C_L = 0$ , where there is a reduction in stability. This is exaggerated in Fig. 7 by the open  $C_m$  scale for the supersonic results; the experimental scatter appears large for the same reason. The reduction of stability is generally of the order of  $0.01\bar{c}$ , except at M = 1.4 where it amounts to  $0.02\bar{c}$ . It has been observed on other wings, for instance the cambered and uncambered gothic wings of Ref. 10, and it appears that in a small incidence range on either side of the attachment incidence the flow behaves to some extent as if attached, and the leading-edge vortex regime is not fully established until higher incidence. There is a corresponding effect on lift-curve slope, Fig. 4, particularly at M = 1.4 where there is a fairly sudden increase of slope near  $\alpha = \pm 1\frac{1}{2}^\circ$ . The pressure distributions of Fig. 14a for M = 1.4,  $\alpha = 1^\circ$ , show that at  $y/s_T = 0.55$ , and further inboard, any suction peaks due to leading-edge separation are of very limited chordwise extent; they do not affect the first pressureplotting point at 0.025 of the local chord. At  $y/s_T = 0.8$ , however, the peak suction region extends back to 0.15 of the local chord, so that at very small incidences it appears that the effects of separation may be confined to the outer parts of the wing, with little effect on overall forces.

On the present plane wing, at any rate, the reductions in stability are confined to lift coefficients of less than 0.02 and so would not be of operational significance on an aircraft designed to cruise at a lift coefficient of around 0.075 at Mach numbers of 2 or more. Also, an operational aircraft would have its centre of gravity about  $0.1\overline{c}$  further forward than the axis position used in Fig. 7, because of low-speed stability requirements, and would therefore have a positive stability margin of about  $0.09\overline{c}$  in the kink region instead of the instability shown in Fig. 7. The small stability changes near the attachment incidence are thus not likely to cause any operational difficulty in themselves. However, it is obviously undesirable for an aircraft to cruise in this region of fairly rapid change of leading-edge flow characteristics near attachment, and this means that, in the design of cambered wings, there should be a sufficient margin between the cruising lift coefficient and the attachment lift coefficient to ensure a properly developed leading-edge flow at cruise.

In Fig. 8, showing the variation of centre of pressure with Mach number at  $C_L = 0.075$ , results are given both allowing for and ignoring the inflection near  $C_L = 0$ , and the difference is generally less than  $0.005c_0$ . The centre of pressure is at about  $0.698c_0$  for Mach numbers of 1.4 to 2.0, moving forward slightly to  $0.691c_0$  by M = 2.8. The value given by slender-wing theory for attached flow is about  $0.05c_0$  further forward, at  $0.64c_0$ . As shown in Fig. 8, this is the same as the measured centre-of-pressure position for subsonic speeds.

If the aircraft centre of gravity is chosen so as to give at worst neutral stability for take-off and landing, then the difference between the cruising centre-of-pressure position and the low-speed aerodynamic-centre position at  $C_L \sim 0.5$  represents the minimum forward shift of the centre of pressure required, from camber or flaps, for trim under cruising conditions<sup>\*</sup>. For the present wing this amounts to a forward shift of  $0.074c_0$ , i.e. a  $\Delta C_m$  based on  $c_0$  of +0.0055 for a typical cruising  $C_L$  of 0.075. It should be noted, however, that the cambered version of the present wing, which was designed earlier, is intended to give a  $\Delta C_m$  based on  $c_0$  of only 0.0026, i.e. about half what would now seem to be required assuming no changes in stability due to camber.

#### 4.3. Drag.

4.3.1. Wave drag at zero lift.—As can be seen in Fig. 9, at the test Reynolds number of  $10^7$  based on  $c_0$  about two-thirds of the total zero-lift drag is skin friction, and only the remaining one-third is wave drag. A reliable estimate of the friction drag is therefore needed in order to derive the wave drag accurately. In Fig. 9 the mean skin-friction coefficient over a chord-length 'c' has been calculated from equations (5) and (7) of Ref. 7 for a flat plate with fully turbulent boundary layer and zero heat transfer, giving

$$(C_F)_c = 0.074 R_c^{-1/5} \left[ 1 + \sigma^{1/3} \frac{\gamma - 1}{2} M_0^2 \right]^{(n-3)/5}$$
(2)

$$= 0.074 R_c^{-1/5} G(M_0), \text{ say}$$
(3)

where

 $R_c$  = Reynolds number based on local chord

#### $\sigma = Prandtl number$

assuming  $\sigma = 0.72$  and n = 0.76. The overall skin-friction coefficient has been obtained by integrating equation (3) stripwise across the span to give

$$(C_F)_{\rm wing} = 0.074 R_{c_0}^{-1/5} \lambda G(M_0) \tag{4}$$

where

$$\lambda = \frac{1}{p} \int_{0}^{1} \left(\frac{c}{c_{0}}\right)^{4/5} d\eta$$
  
= 1.125 for the present planform

and

 $R_{c_0}$  = Reynolds number based on root chord.

\* Assuming no effect of camber or flaps on stability.

The friction drag is then given by

$$C_{DF} = \left(\frac{\text{Total wetted area}}{\text{Planform area}}\right) \times (C_F)_{\text{wing}}.$$
(5)

The mean value of  $C_F$  is sometimes calculated by using a mean value of R based on  $\bar{c}$  or  $\bar{c}$  in equation (3), instead of integrating the values based on local chord as in equation (4). For the present planform, the use of  $\bar{c}$  or  $\bar{c}$  in equation (3) would give friction drags 2% larger and 2% smaller, respectively, than the strip method used here. The differences are quite small, but the percentage difference in wave drag is of course twice as great. It should also be noted that both equation (3) and equation (4) are derived for flat plates, i.e. the usual assumption is made that the overall friction drag is unaffected by pressure gradients due to thickness. In equation (5), however, the true wetted area is used rather than twice the plan area as for a flat plate. The increase in area is about 4% for the present model, but for designs with more pronounced central bodies the figure would be larger; in two recent project studies it amounted to about 8%. There does not appear to be any justification for disregarding this factor, as is sometimes done; in fact to do so would lead to inconsistencies in the derived wave drags for models with different central bodies.

The zero-lift wave-drag coefficients  $(C_{D\,0})_w$  derived from the balance tests, using these estimates for skin friction and the sting corrections of Section 3.1, are plotted against Mach number in the top half of Fig. 9;  $(C_{D\,0})_w$  varies from 0.0033 at M = 1.4 to 0.0018 at M = 1.8. Also shown in Fig. 9 are the values obtained by integrating the pressure-plotting data and applying a correction for sting interference, and it can be seen that the agreement between the balance and pressureplotting results is remarkably good. This could mean that the various assumptions made in producing Fig. 9 are correct; on the other hand, it could be due simply to a fortuitous cancelling of errors. In addition to the uncertainties in friction drag and sting corrections already noted, the integration of the pressure-plotting data also involves some uncertainty since the absence of pressure tappings at the leading edge necessitated some extrapolation in this region.

The lower half of Fig. 9 shows the zero-lift wave-drag factor  $K_0$ , given by

$$K_0 = \left[\frac{\pi \times (\text{wing area}) \times c_0^4}{128 \times (\text{volume})^2}\right] (C_{D\,0})_w \tag{6}$$

plotted against Mach number.  $K_0$  varies from  $1 \cdot 1$  at  $M = 1 \cdot 4$  to  $0 \cdot 6$  at  $M = 2 \cdot 8$ , where its value appears to be roughly a minimum. At  $M = 2 \cdot 8$  part of the wing (near  $0 \cdot 58 \times \text{semispan}$ ) is approaching sonic leading-edge conditions,  $\beta ds/dx$  being  $0 \cdot 9$  in this region; the overall value of  $\beta s_T/c_0$  is  $0 \cdot 655$  at this Mach number.

Comparing the measured values of  $K_0$  with the results from slender-wing theory shown in Fig. 9, it can be seen that the decrease of  $K_0$  with increasing speed is well predicted by slender theory, and that the measured values of  $K_0$  are less (by about  $0 \cdot 2$ ) than the slender-theory values. In these respects the present wing, with Newby area distribution and  $p = \frac{1}{2}$  planform, behaves similarly to earlier wings with Newby or Lord V area distributions and delta, gothic and mild gothic planforms. In contrast, preliminary results on some later wings with more 'necked-in' planforms ( $p < \frac{1}{2}$ ), and area distributions having further-aft maxima and larger trailing-edge derivatives, show that for these planforms the achieved values of  $K_0$  are considerably larger than the slender-theory values.

Linear thin-wing-theory drag calculations have not yet been made, but a few pressure distributions have been calculated, as shown in Fig. 12. If the differences between these and the

slender-theory distributions are integrated, assuming the same pressures near the leading edge, it is found that at M = 2 the 'linear-theory' value of  $K_0$  is 0.92, compared with 0.96 on slender theory. This comparison must be treated with reserve, however, as the proper linear-theory drag may involve differences near the leading edge, compared with slender theory, which have not been taken into account.

One reason for the smaller measured drag compared with theory on the present wing can be seen from the pressure distributions of Fig. 12. These will be further discussed in Section 5.1, but it may be noted at this stage that both linear and slender theories predict rapidly increasing suctions towards the trailing edge, particularly on the inner part of the wing, and these are not realized experimentally. If the pressure differences at the rear, compared with slender theory, are integrated, and allowance made for the pressure field of the sting shroud which is of course included in the experimental pressures, it is found that they account almost exactly for the drag differences shown in Fig. 9. At M = 2, for instance, the observed pressure differences at the rear, compared with slender theory, correspond to  $\Delta C_D = 0.0010$  and the sting correction is  $\Delta C_D = 0.0004$ , leaving  $\Delta C_D = 0.0006$  as the true discrepancy; this compares with  $\Delta C_D = 0.0005$  in Fig. 9\*. The spanwise distribution of drag is shown in Fig. 10 and it can be seen that most of the drag, and most of the discrepancy between theory and experiment, is concentrated on the inner part of the wing. Further discussion on this subject will be found in Section 5.1.

4.3.2. Drag due to lift.—As noted in Section 3.1, the experimental values of the overall lift-dependent drag factor, K, are different for positive and negative incidences because of tunnel flow effects. Results are given in Fig. 11 for both positive and negative incidences; the differences are fairly small beyond  $C_L = 0.1$ . In the lower part of Fig. 11 the mean values of K at  $C_L = 0.1$  are plotted against Mach number, and it can be seen that K increases from about 1.5 at M = 1.4, to 2.4 at M = 2.8. The measured values agree very well with the mean curve derived in Ref. 7 from experimental results on a number of wings with no camber or with transverse camber only.

The lift-dependent drag factor is sometimes expressed in the form

$$K = K_{\mathcal{V}} + 2\left(\frac{\beta s_T}{c_0}\right)^2 K_{\mathcal{W}} \tag{7}$$

 $K_V$  being the 'vortex-drag factor' and  $K_W$  the 'lift-dependent wave-drag factor'. For the present wing, the values which best fit the supersonic results are  $K_V = 1.35$ ,  $K_W = 1.20$ ; the corresponding values of K are shown as crosses in the lower part of Fig. 11. For Mach numbers of 1.5 to 2.8 this arbitrary choice of  $K_V$  and  $K_W$  gives excellent agreement with the experimental results, but the choice of  $K_V = 1.35$  does not agree with the low-speed results giving K = 1.6 at M = 0.3.

With the R. T. Jones lower-bound values of  $K_V = K_W = 1$ , the value of K at M = 2 would be 1.38, compared with a measured value of 1.80 at this Mach number. Thus, although the measured value for this planform is no worse than would be expected from the mean curve of Ref. 5 for uncambered wings, there is evidently scope for reduction of K by suitable camber and twist. Values of  $K_V$  and  $K_W$  of about 1.1 have already been measured on the uncambered gothic

<sup>\*</sup> In view of the uncertainties in measuring and integrating the pressures, and in allowing for skin friction and sting interference, this apparently close agreement could be no more than fortuitous. It should not be taken as conclusive proof that the whole of the discrepancy between theoretical and measured wave drag is attributable to the observed pressure differences near the rear, although these obviously play a large part.

wing of Ref. 8 for instance, and if similar results could be achieved on the present planform by the use of camber and twist, the value of K at a Mach number of 2 would be reduced from 1.8 to about 1.5.

4.3.3. Lift/drag ratio.—Because of the low Reynolds number and the absence of full-scale items such as fins, etc., the lift/drag ratio given directly by model experiments is of little significance except as a rough means of comparison with other model results. For the present wing, the measured values of  $(L/D)_{max}$  are

$$7 \cdot 45$$
 at  $M = 1 \cdot 4$   
 $7 \cdot 35$  at  $M = 2 \cdot 2$   
and  $7 \cdot 05$  at  $M = 2 \cdot 8$ .

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The full-scale aircraft will achieve higher values than these, the extra drag of fins and miscellaneous items being more than offset by the reduction of friction drag at the higher Reynolds number. For an aircraft cruising at  $M = 2 \cdot 2$  at high altitude a typical drag coefficient for skin friction, fin and miscellaneous items (but excluding engines) would be about 0.00375. With  $K_0 = 0.72$  and K = 1.92, and assuming the same volume coefficient ( $\tau = 0.0343$ ) as for the model, the full-scale value of L/D, excluding engine drag, would be  $8 \cdot 3$  at  $M = 2 \cdot 2$ .

#### 5. Pressure-Plotting Results.

#### 5.1. Zero-lift Pressure Distributions.

Pressure distributions at zero lift are given in Fig. 12 for Mach numbers of  $1 \cdot 4$ ,  $2 \cdot 0$ ,  $2 \cdot 4$  and  $2 \cdot 8$ , uncorrected for sting interference effects. Two sets of results are given, the circles representing tests with transition free and the small pressure-plotting sting shroud, and the crosses tests with transition fixed and the larger balance sting shroud. All results are for  $R = 10^7$  based on  $c_0$ ; tests at half this Reynolds number at M = 2 showed no significant differences.

The effects of fixing transition in Fig. 12 are inconsistent; at Mach numbers of 1.4 and 2.8 there is hardly any difference between the results (except at the rear, due to the shroud change) but at Mach numbers of 2.0 and 2.4 the values of  $C_p$  with fixed transition are about 0.01 more negative than those with free transition. The inconsistency is probably due to errors in measurement of the type discussed in Section 3.2, affecting the complete set of readings at any one incidence. In Fig. 15, where a similar comparison is given for a number of incidences at M = 2.0, the effect of fixing transition is to make  $C_p$  fairly consistently more negative on both upper and lower surfaces. It is not clear why fixing transition should have such an effect, but it is not of great importance in the present context. It does not affect the general shape of the measured distributions, or their qualitative agreement or disagreement with theory, and it has little effect on either drag or lift since the pressure change seems to be roughly the same over the whole wing surface. Subsequent discussion will be based on the results with free transition and the smaller sting shroud.

Fig. 12 shows that except near the rear of the model, as noted in Section 4.3.1, the agreement of the measured pressures with theory is qualitatively quite good apart from one or two points near the front of the centre section and near  $0.4c_0$  at  $y/s_T = 0.125$ . It is not known whether the uneven pressure distributions in these areas are genuine or not, since examination of the model after test showed local imperfections in the Araldite filling around the orifices in question, which might have caused them to give a consistently high or low reading. In integrating the distributions it has been assumed that the readings are in fact unrepresentative, and smooth curves have been drawn through them.

Fig. 12 includes theoretical results using both slender-wing theory and linear thin-wing theory. At M = 1.4, the two theories give very similar results and the measurements agree well with either except towards the rear. With increase of speed both theories predict reductions in the favourable pressure gradients, and a general lowering of suctions over the rear and outer parts of the wing (compare M = 1.4 and M = 2.8, for instance), and the experimental results follow these general trends fairly closely. The differences between the two theories increase at the higher Mach numbers, however, linear theory predicting higher suctions on the outer sections and lower suctions near the trailing edge of the inner sections compared with slender theory. Because of the experimental scatter and the differences between transition-fixed and transition-free results, it is not possible to say that one theory gives better agreement than the other at the higher Mach numbers.

One of the aims in the design of this model was to see whether a wing with varying cross-section shapes could be designed, using slender-wing theory, to give smooth pressure distributions and small velocity increments due to thickness, and low drag. At the time, the design of such a wing represented a fairly difficult problem; it was all too easy to produce shapes which, while apparently smooth, gave 'lumpy' pressure distributions. Even when a shape was produced, e.g. the present one, which should give acceptable distributions according to slender theory, there remained the doubt whether the theoretical distributions would be achieved in practice. In this context, the results of Fig. 12 indicate a large measure of success for the design procedures of Ref. 1; the model has achieved smooth pressure distributions and small velocity increments everywhere, there is good agreement between theory and experiment except near the trailing edge, and the drag due to thickness is low.

As noted in Section 4.3.1, part of the apparent difference between the theoretical slender-wing pressures and the measured pressures on the rear part of the inner sections is due to sting-shroud interference; on the assumptions used here this accounts for 30% to 40% of the observed pressure difference, depending on Mach number. The differences remaining after applying this correction are quite large, however, corresponding to  $\Delta C_D = 0.0006$  at M = 2 which represents 25% of the zero-lift wave drag at this speed. Various possible explanations can be thought of for the pressure differences; these are discussed below.

First, there is the question of the adequacy of the sting-interference correction, and in the present context we are concerned only with the pressure-field term of Section 3.1; the term due to the masking of rear-facing surfaces affects only the forces measured on the balance. The correction applied here is based on pressure measurements made on a Lord V delta, with and without a rear sting. These were integrated to give a drag correction due to the sting shroud on that wing, and for the present wing this has been scaled according to the 1.6th power9 of the effective cone angle of the added volume above the wing surface, according to the amount of rear-facing surface behind the Mach wave from the shroud leading edge, and according to the relative shroud diameters and wing areas, giving a drag correction about twice as large as that for wing F. Preliminary results from pressure measurements with and without sting on a similar model tend to confirm the original figures for the Lord V delta. However, both these wings had thickness distributions giving a fairly flat pressure distribution over the rear of the inner sections. The present wing is the first to be tested with thickness distributions giving rapid increases of suction towards the rear. It is not immediately obvious from the theory which particular features of the thickness distributions of the present wing (Figs. 2 and 3) are mainly responsible for these increases of suction. It seems likely, however, that they are associated with the large streamwise slopes and curvatures towards the rear of the inner sections only, and the consequent heavy concentration of sinks in this relatively small region. It is precisely this region which is masked by the addition of the cylindrical sting shroud. In scaling the Lord V delta sting correction some account has been taken of this factor, by introducing the equivalent cone angle of the added volume above the wing surface, but it may be that the allowance is inadequate, and further theoretical and experimental work is desirable. The most useful source of information would of course be pressure-plotting tests with and without sting, as for the two wings already mentioned.

At any rate in principle, a second reason for the observed pressure differences might be boundary-layer thickening towards the rear of the wing. Unpublished work by Prof. J. C. Cooke, however, indicates that the theoretical effect of this would be much less than the observed discrepancy unless boundary-layer separation were present. In this respect, moreover, the present wing would be expected to behave better than other wings which have been pressure-plotted, rather than worse, as measured, because of the strong favourable pressure gradients predicted by theory.

A third possibility is that of interaction between the trailing-edge shock and the boundary layer, reducing the shock strength and the expansion ahead of the shock compared with theoretical predictions. Unfortunately the boundary-layer behaviour on the wing surface cannot be seen in the schlieren pictures of Fig. 25 because of the sting shroud, but if such interaction occurred one would expect to be able to see either a forward movement of the shock ahead of the trailing edge, or a bifurcated shock with a forward limb ahead of the trailing edge. Neither of these features is apparent in Fig. 25.

The final possibility is that the pressure differences are due simply to theoretical deficiencies. The limitations of slender theory are well known, but in the present case the slender-theory results are quite similar to those from linearized thin-wing theory (Fig. 12) and the latter must also be questioned. One feature of linear thin-wing theory in the present context is the thinness assumption by which the boundary conditions are satisfied in the chord plane rather than on the surface. The errors introduced by this assumption on the present wing, with its faired central body and consequent 'lumpy' cross-sections, Fig. 2, would be expected to be greater than those for earlier wings with simple cross-sections. However, although no results are available without this simplifying assumption, it is generally considered that the errors introduced by it should not be as great as the difference of 0.1 in  $C_p$  implied by Fig. 12a for instance.

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No further possibilities can be suggested, and the choice therefore seems to lie mainly between inadequate sting corrections and inadequate theory—with a general feeling in the latter case that the theory should hardly be wrong to this extent! On the other hand, to attribute the discrepancy entirely to sting effects would involve increasing the assumed sting pressure-field correction by a factor of about  $2\frac{1}{2}$ . For the balance sting, this would mean almost doubling the total corrections of Section 3.1, so that the sting correction for this type of wing would represent over half the zero-lift wave drag, a most unpleasant state of affairs from the experimental viewpoint. It would seem essential, if further sting-mounted-model tests are contemplated on wings with this kind of thickness distribution, that further pressure-plotting evidence should be obtained with and without the sting and also, perhaps, with and without the central faired body of the present model. In addition, further calculations should be made on wings with 'lumpy' cross-sections, with and without the addition of a cylindrical sting shroud at the rear, using various available methods in order to gain further insight into these rear-end effects and the possible effects of sting interference on them.

Finally, it is perhaps worth noting that over the greater part of the wing, where the velocity increments are small, the agreement between theory and experiment is quite good; it is only where theory predicts fairly large velocities, near the trailing edge, that agreement is poor. This suggests that, apart from the questions of sting interference and the simplified boundary conditions of linear thin-wing theory, the source of the disagreement near the trailing edge might lie in the basic assumption of small perturbations, common to both linear and slender theories, and also perhaps in the approximations, different for the two theories, for the direction of propagation of disturbances. To improve the theories in these respects is of course a matter of considerable difficulty, and as a general principle it is therefore desirable that, as far as possible, design solutions should be sought in which the velocity increments are everywhere small.

#### 5.2. Lifting Characteristics.

5.2.1. Pressure distributions, local load and chord load.—Upper-surface and lower-surface chordwise pressure distributions are given in Fig. 14 for incidences of 0 to  $8\frac{1}{2}$  degrees and Mach numbers of  $1 \cdot 4$ ,  $2 \cdot 0$  and  $2 \cdot 8$ . These have been integrated to give loading distributions which will be discussed later, but there are several features of the pressure distributions themselves which may be noted.

The chordwise pressure distributions show the usual effect of flow separation from highly swept leading edges, the upper-surface suctions rising to a peak beneath the coiled leading-edge vortex sheet with a rapid increase of pressure further aft along the chord. The effect is much more marked at the lower Mach numbers; with increase of speed the high-suction region beneath the vortex extends rearward and flattens until by M = 2.8 it is only just visible. Vapour-screen studies on other wings have shown that this is associated with a marked reduction in the height of the vortex sheet above the wing with increase of speed. The oil-flow pictures of Fig. 23 ( $\alpha = 6.4^{\circ}$ ) illustrate the accompanying decrease in scrubbing action of the vortex, and the inward movement of the attachment line of the flow over the top of the vortex sheet, as Mach number increases. The observed movement of the attachment line is shown graphically in Fig. 24, and it can be seen that the position of the attachment line corresponds quite closely to the rearward limit of the region of high suction beneath the vortex from Fig. 14, shown as points in the upper half of Fig. 24. Fig. 24 also gives the position of the secondary separation line, which appears to be constant for all Mach numbers, and of the peak-suction line for Mach numbers of 1.4 and 2.0; at higher speeds there are no well-defined suction peaks.

Fig. 14 shows that inboard and to the rear of the vortex region the chordwise pressure gradients are generally favourable, even at  $8\frac{1}{2}^{\circ}$  incidence. In this area the effect of incidence seems to be simply to produce a roughly constant pressure increment over the whole chord right back to the trailing edge, so that the pressure gradients are practically the same as those due to thickness alone. This is shown more clearly in Fig. 16, giving the pressure increments due to incidence at M = 2 on upper and lower surfaces, for incidences of  $2 \cdot 15^{\circ}$  and  $4 \cdot 25^{\circ}$ . Also shown for comparison are the results which would be given by slender-wing theory if the flow were attached at the leading edge. (Although in one sense such a comparison might seem rather academic since the flow is not in fact attached, it has some practical interest since the cruising incidence will in general be greater than the attachment incidence, and attached-flow slender theory is sometimes used for the part of the loading beyond the attachment condition.) The biggest difference compared with slender theory is at the trailing edge. Here the theory predicts zero load because of the streamwise tips, but in practice the trailing-edge loads are as great as those further forward on the chord, on both upper and lower

surfaces. The distribution to the rear of the vortex region is in fact generally similar to that given by slender theory for a delta wing with no streamwise tip. A full analysis has not been made, but at M = 2, taking the mean\* of the loadings for  $\alpha = 2 \cdot 15^{\circ}$  and  $\alpha = 4 \cdot 25^{\circ}$ , the span of the equivalent delta so far as the loads to the rear of the vortex are concerned would be about  $0 \cdot 22c_0$  (compared with  $0 \cdot 25c_0$  for the actual wing). The additional load near the trailing edge is of course part of the reason for the further aft centre-of-pressure position, compared with slender theory, noted in Section 4.2. Further discussion on this question will be given later when dealing with the distribution of cross-load.

Another interesting feature of Fig. 14 is that, apart from the high suctions on the upper surface under the vortex core, the rest of the loading is by no means equally distributed between upper and lower surfaces as is usually assumed, but is appreciably greater on the lower surface than on the upper surface. On the centre section at  $\alpha = 4 \cdot 25^{\circ}$ , for instance, the ratio of the total chord load on the lower surface to that on the upper surface varies from about  $1 \cdot 4$ , at  $M = 1 \cdot 4$ , to as much as  $1 \cdot 8$  at  $M = 2 \cdot 8$ . The ratio decreases further outboard, as shown in Fig. 17, because of the additional vortex lift developed on the upper surface, but at  $M = 2 \cdot 8$ , where there is little non-linear lift, the lower-surface lift remains greater out to  $0 \cdot 7 \times$  semispan. Fig. 17 also gives the results from attachedflow slender theory, assuming equal lift on both surfaces, and it can be seen that the lower-surface lift is always greater than the theoretical value near the centre of the wing, falling below further outboard. The upper-surface lift, on the other hand, is always less than the theoretical value near the centre of the wing.

Spanwise distributions of the total chord load (i.e. both upper and lower surfaces) are given in Fig. 18 for various Mach numbers and incidences. At M = 2.8, where there is little non-linear lift, the distribution is roughly elliptical, as would be predicted by slender theory, but with a hump near the centre caused by the extra lower-surface lift. As is to be expected at this high speed  $(\beta s_T/c_0 = 0.65)$ , the overall lift is of course appreciably less than the slender-theory value, as noted earlier (Fig. 6). At lower Mach numbers, the effects of the non-linear lift déveloped on the outer sections become apparent, and the spanwise load distributions become rather more rectangular in shape. The number of pressure-plotting stations was insufficient to determine the shape of the distributions on the outer parts of the wing, and the points are therefore left unconnected in Fig. 18.

5.2.2. Cross-load.—Figs. 19 and 20 present some typical spanwise distributions of local load at various chordwise positions, and Figs. 21 and 22 give chordwise variations of cross-load obtained by integrating such distributions. The results from attached-flow slender-wing theory are also shown, and the loads are divided by incidence or by total load to facilitate comparison.

Fig. 19 shows the effects of incidence at a Mach number of  $2 \cdot 0$ . On the inner parts of the wing  $\Delta C_p/\alpha$  is about the same for all incidences, as would be expected, and differs from the slender-theory values at the various chordwise positions in the manner discussed in the previous section. Near the leading edge the values of  $\Delta C_p/\alpha$  at the lowest incidence ( $\alpha = 2 \cdot 15^{\circ}$ ) follow in a qualitative manner the  $\sqrt{(1-\eta^2)}$  trend of slender theory, but with the theoretically infinite leading-edge suctions replaced by finite suction peaks representing the beginning of the effects of the leading-edge vortex system. As can be seen also in the chordwise pressure distributions of Fig. 14, increase of incidence does not produce simply a linear increase of pressures and local loads, which would leave the height

<sup>\*</sup> The consistent difference between the lower-surface values of  $\Delta C_p/\alpha$  for the two incidences is thought to be due to experimental error of the kind discussed in Section 3.2.

and shape of the peak-loading region the same in terms of  $\Delta C_p/\alpha$ ; instead the peak decreases in height and becomes wider. This marked alteration in shape of the peak with increase of incidence at M = 2 takes place in such a way as to leave the integrated cross-load virtually unchanged at each chordwise station, as shown in Fig. 21. As noted earlier, there is not much non-linear overall lift at M = 2; if there had been there would of course have been greater changes in cross-load/ $\alpha$  with incidence.

Fig. 20 shows the effects of Mach number at a constant incidence of  $4 \cdot 25^{\circ}$ , and demonstrates the collapse of the high loading peak near the leading edge with increase of Mach number. By  $M = 2 \cdot 8$  at this incidence the spanwise distribution of local load is similar in shape to that given by attached-flow slender-wing theory, although the general level of load is of course lower corresponding to the smaller overall lift slope compared with slender-wing theory.

It has been noted previously that at M = 2 the overall lift curve displays little non-linear lift in the usual sense of increase of lift slope with incidence, and that the measured lift is in good agreement with that given by linear theory for the equivalent cropped delta. It is perhaps worth remarking that, as discussed above, the actual pressure and load distributions include quite large 'non-linear' contributions in the sense of concentrated loadings under a leading-edge vortex. It happens that these non-linear effects near the leading edge combine with loadings elsewhere on the wing to produce a more or less linear variation of lift with incidence at the higher Mach numbers; the good agreement with linear theory at M = 2 could to this extent be regarded as fortuitous.

Distributions of cross-load divided by incidence for various Mach numbers and incidences are given in Fig. 21a, together with the results from attached-flow slender theory. At M = 1.4 the measured cross-load agrees fairly well with theory over the front two-thirds of the length. Towards the trailing edge, however, as already noted, the loads are very much greater than those given by theory, and this is true at all Mach numbers. Increase of speed leads to a steady reduction in cross-load at all chordwise positions, with little change in general shape. This is shown more clearly in Fig. 21b where the cross-load distributions are made non-dimensional with the total load  $\overline{L}$ , and it can be seen that at  $\alpha = 4.25^{\circ}$  the points for all Mach numbers collapse into a single curve, corresponding to the more or less constant centre-of-pressure position measured in the balance tests (Fig. 8). [There is of course no a priori reason why the cross-loads for different Mach numbers should collapse in this manner. The large variation of the leading-edge vortex lift with Mach number might conceivably have produced variations of cross-load distribution and centre of pressure, and the amount of trailing-edge load could also have varied with Mach number. It so happens that on the present wing the variation of the leading-edge vortex lift with Mach number is roughly the same at all chordwise positions (i.e. quasi-conical), and also the trailing-edge load parameter  $L(1)/\overline{L}$  does not vary significantly with Mach number, so that the shape of the loading curve is unaltered.] The trailing-edge load parameter  $L(1)/\overline{L}$  has the comparatively high value of about 1.75, and compared with attached-flow slender-wing theory there is a shift of load from the front 80% of the length to the rear 20% corresponding to the difference of about  $0.055c_0$  in centre of pressure measured in the balance tests (Fig. 8).

Mention was made in the previous section of the differences between the measured local loads and those from slender-wing theory, Fig. 16. It appears from a comparison of Fig. 16 and Fig. 21b that the general pattern of the local load discrepancies on the centre-line is similar to that shown by the overall cross-loads, the loads in both cases being less than the theoretical near mid-chord and greater near the trailing-edge. This suggests a possible correlation between the two loadings, as

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shown in Fig. 22. The lower half of Fig. 22 gives distributions of  $-\Delta C_p/\alpha$  at the centre-line for Mach numbers of 1.4, 2.0 and 2.8, and compares them with slender-theory values. (Because of pressure measuring inaccuracies as discussed in Section 3.2 the experimental values used are the mean of those for  $\alpha = 2, 4$  and 6 degrees, with transition both fixed and free, for increased accuracy.) In the upper half of Fig. 22 the measured values of cross-load divided by  $\alpha$  are scaled up or down in the ratio of the measured to the theoretical values of  $-\Delta C_p/\alpha$  at the centre-line at each streamwise position, and it can be seen that when this is done the scaled cross-loads collapse quite closely into the curve given by slender theory. In other words, the departure of the measured cross-load from slender theory at any streamwise position is in direct proportion to the departure of the measured centre-line local load from theory. This link between the measured and theoretical cross-load and the measured and theoretical centre-line load is somewhat remarkable in view of the quite different shapes of the spanwise load distributions for different Mach numbers, arising from differences in leading-edge vortex development (Fig. 20). In the absence of separated-flow effects, slender theory would of course predict that the cross-load should be proportional to the local load at the centre-line. The implication of Fig. 22 is that, at any rate on this wing, the same is true even when a large part of the lift is associated with the leading-edge separation vortex, although there is no obvious reason why variations in leading-edge vortex development should be so closely reflected in differences of local load at the centre-line. It may be that the apparent close correlation on the present wing is to some extent accidental. If it were generally true it would mean that the cross-load distribution and centre of pressure could be accurately predicted, even with separation effects, given an improved method of estimating the centre-line load only.

Finally, mention should be made of the implications of the discrepancies between experiment and slender-wing theory on the problem of camber design for trim at cruising conditions. The  $0.05c_0$ discrepancy in supersonic centre of pressure, as such, is not important here, because the design requirement for the camber is not to achieve a given centre-of-pressure position in absolute terms, but simply to produce a  $\Delta C_m$  sufficient to trim the aircraft under cruising conditions at a centre of gravity dictated by low-speed conditions. The requirement is based on the difference between low-speed and high-speed conditions rather than on an absolute centre of pressure. Provided the design method gives the required  $\Delta C_m$ , discrepancies between theoretical and experimental centres of pressure are of no direct consequence. They may be of some significance indirectly, however, since if the plane-wing centre of pressure and load distributions-particularly the latter-differ widely from the slender-theory predictions, there is obviously more reason to doubt whether slender theory will produce the required  $\Delta C_m$  due to camber. The cambered version of the present wing, for instance, was designed to give a trailing-edge load of  $L(1) = 0.5\overline{L}$  according to slender theory, the corresponding plane-wing value being zero. In the event, the plane wing has been found to have  $L(1) = 1.75\overline{L}$  to begin with, and with such a difference on the plane wing the effect of camber on the trailing-edge load could well be quite different from that predicted. When the cambered-wing pressure-plotting results are available it will be interesting to see to what extent the predicted changes in loading due to camber are realized despite the discrepancies on the plane wing.

#### 6. Conclusions.

The main points of interest from the overall force results are as follows:

(i) The difference between the supersonic centre-of-pressure position and the low-speed aerodynamic-centre position at  $C_L = 0.5$  is about  $0.075c_0$ , in good agreement with the figure of  $0.07c_0$  which has been suggested as a camber design requirement.

(ii) The zero-lift wave drag falls with increase of speed in the manner predicted by slender-wing theory, and the values of  $K_0$  are less (by about 0.2) than the slender-theory values. In these respects the results are similar to earlier results on slender wings with Newby or Lord V area distributions and relatively 'smooth' leading-edge planform shapes. At a Mach number of 2.2 the value of  $K_0$  is 0.72.

(iii) The values of the lift-dependent drag factor, K, are in close agreement with the mean curve of Ref. 5 for wings with no streamwise camber. At  $M = 2 \cdot 2$  the value of K at a lift coefficient of  $0 \cdot 1$  is  $1 \cdot 92$ .

(iv) With a typical full-scale drag coefficient of 0.00375 for friction, fin and miscellaneous items, and assuming the same volume coefficient as for the model ( $\tau = 0.0343$ ), the estimated maximum full-scale lift/drag ratio at M = 2.2 is 8.3, excluding engine drag.

The pressure-plotting tests for Mach numbers of 1.4 to 2.8 and incidences up to  $6.4^{\circ}$  show that:

(i) One of the main design objectives, to produce smooth pressure distributions, small velocity increments, and low wave drag due to thickness on a varying-section design more representative of a practical aircraft layout, is successfully achieved.

(ii) At zero lift, the measured pressures over the front two-thirds of the model agree quite well with the predictions of either slender-wing or linear thin-wing theory, but near the trailing edge the high suctions predicted by both theories are not present, the differences being sufficient to account for the lower measured drag compared with theory. The integrated pressure drag agrees well with the wave drag deduced from the balance tests.

(iii) The difference between theory and experiment near the trailing edge is thought to be due either to inadequate sting correction or to inadequate theory. If it is due to inadequate sting correction, it implies that on this wing the sting correction should be roughly doubled; it would then amount to over half the zero-lift wave drag. Further experimental and theoretical work is evidently desirable.

(iv) At incidence, the chordwise pressure gradients are everywhere favourable apart, of course, from the pressure changes through the leading-edge vortex system.

(v) Between the reattachment line and the trailing edge the local load due to incidence at any spanwise station is more or less constant over the whole chord right back to the trailing edge. This is what would be expected on a delta wing with no streamwise tips; the decrease of load to zero at the trailing edge, predicted by slender theory for streamwise tips, does not occur, and the trailing-edge cross-load parameter  $L(1)/\overline{L}$  has the relatively high value of about 1.75.

(vi) Despite large variations in shape of the local load distributions in the leading-edge vortex region with Mach number and incidence, the non-dimensional cross-load distribution  $L(x)/\bar{L}$  hardly varies with Mach number or incidence; changes in the vortex region combine with changes further inboard to leave  $L(x)/\bar{L}$  unaltered, giving a more or less constant centre-of-pressure position for Mach numbers of 1.4 to 2.8 and incidences of between  $1^{\circ}$  and  $6^{\circ}$ . Because of the large trailing-edge load the centre of pressure is about  $0.05c_0$  behind the slender-theory value.

(vii) It appears that at any chordwise position, the departure of the cross-load from the slendertheory value is in almost exact proportion to the departure of the local load at the centre-line from the theoretical value. This apparent link between cross-load and centre-line load is somewhat remarkable in view of the large variation of the leading-edge vortex contribution with Mach number.

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## LIST OF SYMBOLS

A	=	$4s_T^2/P$ , aspect ratio
С		Chord
c <sub>0</sub>		Centre-line chord
ī	=	$P/2s_{T}$ , geometric mean chord
Ē		$\int c^2 dy/P$ , aerodynamic mean chord
$C_D$		Drag coefficient based on $P$
$C_{D0}$		Drag coefficient at zero lift
$C_{DF}$		Overall skin-friction drag coefficient based on P
$C_F$		Skin-friction coefficient per unit wetted area
$(C_F)_c$		Mean value of $C_F$ over local chord length $c$
$(C_F)_{\rm wing}$		Mean value of $C_F$ over wing surface
$C_p$		$(p-p_0)/\frac{1}{2}\rho V_0^2$ , local pressure coefficient
$\Delta C_p$	=	$(C_p)_{\rm u.s.} - (C_p)_{\rm l.s.}$ , local load coefficient $\times (-1)$
$(\Delta C_p)_{ m u.s.}$	=	$(C_p)_{\rm u.s.}(\alpha) - (C_p)_{\rm u.s.}(\alpha = 0)$ , contribution of upper surface to $\Delta C_p$
$G(M_0)$	=	$\left[1 + \sigma^{1/3} \frac{\gamma - 1}{2} M_0^2\right]^{(n-3)/5}$
,		
K	=	$\pi A(C_D - C_{D0})/C_L^2$ , overall lift-dependent drag factor
K K <sub>V</sub>	=	$\pi A(C_D - C_{D0})/C_L^2$ , overall lift-dependent drag factor Vortex drag factor, Section 4.3.2
K $K_{V}$ $K_{W}$	=	$\pi A(C_D - C_{D0})/C_L^2$ , overall lift-dependent drag factor Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2
K $K_{V}$ $K_{W}$ L(x)	II	$\pi A(C_D - C_{D0})/C_L^2$ , overall lift-dependent drag factor Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} - \Delta C_p(x, y) dy$ , cross-load
$K$ $K_{V}$ $K_{W}$ $L(x)$ $L(1, y)$	_	$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} -\Delta C_p(x, y) dx, \text{ total chord load}$
$K$ $K_{V}$ $K_{W}$ $L(x)$ $L(1, y)$ $\bar{L}$		$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} -\Delta C_p(x, y) dx, \text{ total chord load}$ $\int_{0}^{1} L(x) dx, \text{ total load}$
K K <sub>V</sub> K <sub>W</sub> L(x) L(1, y) Ē M, M <sub>0</sub>		$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} -\Delta C_p(x, y) dx, \text{ total chord load}$ $\int_{0}^{1} L(x) dx, \text{ total load}$ Free-stream Mach number
K K <sub>V</sub> K <sub>W</sub> L(x) L(1, y) Ē M, M <sub>0</sub> n	-	$\pi A(C_D - C_{D0})/C_L^2$ , overall lift-dependent drag factor Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy$ , cross-load $\int_{-s(x)}^{T.E.} -\Delta C_p(x, y) dx$ , total chord load $\int_{0}^{1} L(x) dx$ , total load Free-stream Mach number Constant, equation (2), assumed = 0.76
K $K_V$ $K_W$ L(x) L(1, y) $\bar{L}$ $M, M_0$ n p	-	$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} -\Delta C_p(x, y) dx, \text{ total chord load}$ $\int_0^1 L(x) dx, \text{ total load}$ Free-stream Mach number Constant, equation (2), assumed = 0.76 $P/2s_T c_0$
$K$ $K_{V}$ $K_{W}$ $L(x)$ $L(1, y)$ $\bar{L}$ $M, M_{0}$ $n$ $p$ $P$	-	$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} -\Delta C_p(x, y) dx, \text{ total chord load}$ $\int_{0}^{1} L(x) dx, \text{ total load}$ Free-stream Mach number Constant, equation (2), assumed = 0.76 $P/2s_T c_0$ Total planform area
К К <sub>V</sub> К <sub>W</sub> L(x) L(1, y)		$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} -\Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{L.E.}^{T.E.} -\Delta C_p(x, y) dx, \text{ total chord load}$ $\int_0^1 L(x) dx, \text{ total load}$ Free-stream Mach number Constant, equation (2), assumed = 0.76 $P/2s_T c_0$ Total planform area Reynolds number
$K$ $K_{V}$ $K_{W}$ $L(x)$ $L(1, y)$ $\bar{L}$ $M, M_{0}$ $n$ $p$ $P$ $R$ $R_{c}$		$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} - \Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} - \Delta C_p(x, y) dx, \text{ total chord load}$ $\int_0^1 L(x) dx, \text{ total load}$ Free-stream Mach number Constant, equation (2), assumed = 0.76 $P/2s_T c_0$ Total planform area Reynolds number Reynolds number based on local chord
$K$ $K_{V}$ $K_{W}$ $L(x)$ $L(1, y)$ $\bar{L}$ $M, M_{0}$ $n$ $p$ $P$ $R$ $R_{c}$ $R_{c_{0}}$		$\pi A(C_D - C_{D0})/C_L^2, \text{ overall lift-dependent drag factor}$ Vortex drag factor, Section 4.3.2 Lift-dependent wave-drag factor, Section 4.3.2 $\int_{-s(x)}^{s(x)} - \Delta C_p(x, y) dy, \text{ cross-load}$ $\int_{\text{L.E.}}^{\text{T.E.}} - \Delta C_p(x, y) dx, \text{ total chord load}$ $\int_0^1 L(x) dx, \text{ total load}$ Free-stream Mach number Constant, equation (2), assumed = 0.76 $P/2s_T c_0$ Total planform area Reynolds number Reynolds number based on local chord Reynolds number based on centre-line chord

## LIST OF SYMBOLS-continued

$s_T$		Semispan at trailing edge
х		Streamwise distance from apex $\div c_0$
у		Spanwise distance from centre-line
β	=	$\sqrt{(M^2-1)}$
γ	=	1.4, ratio of specific heats
λ	=	$\frac{1}{p}\int_0^1 \left(\frac{c}{c_0}\right)^{4/5} d\eta$
σ		Prandtl number, assumed = $0.72$
au	=	(Volume)/ <i>P</i> <sup>3/2</sup>
η	=	$y s_T$

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## TABLE 1

# Values of $10^3 C_p$ : Transition Free, Small Sting Shroud, $R = 2 \times 10^6/ft$

## (a) $M = 1 \cdot 4$

## α(degrees)

		ļ																
_	$10^3 y/s_T$	$10^{3}x/c_{0}$	-12.86	-8.54	-6·41	-4·27	-3.19	-2.12	1.06	0	0	1.06	2.12	3.19	4.27	6 • 41	8 · 54	12.86
-	0	109 200 300 400 500 600 700 750	183 187 199 192 184 176 151 117	170 121 131 119 109 101 81 73	136 90 101 89 77 69 47 40	115 67 74 58 46 37 15 8	$     \begin{array}{r}       108 \\       60 \\       63 \\       48 \\       34 \\       23 \\       + 1 \\       - 4     \end{array} $	$99 \\ 51 \\ 51 \\ 36 \\ 20 \\ +11 \\ -11 \\ -18$	$     \begin{array}{r}             89 \\             39 \\             24 \\             + 7 \\             - 5 \\             -26 \\             -32 \\         \end{array}     $	823129+12-5-19-38-47	$     \begin{array}{r}       80 \\       29 \\       29 \\       +12 \\       -5 \\       -17 \\       -38 \\       -49 \\     \end{array} $	$74 \\ 24 \\ 20 \\ + 3 \\ -14 \\ -27 \\ -49 \\ -56$	$ \begin{array}{r} 63 \\ 15 \\ + 8 \\ - 9 \\ -26 \\ -41 \\ -62 \\ -71 \\ \end{array} $	$58 \\ 10 \\ + 2 \\ -16 \\ -34 \\ -51 \\ -72 \\ -81$	56 + 5 - 4 - 23 - 43 - 58 - 79 - 90	+50 -7 -14 -36 -55 -74 -97 -105	+36 -26 -34 -55 -76 -94 -117 -128	+12 -59 -71 -99 -124 -147 -169 -176
22	065	148 193 238 283	172 179 188 193	131 128 130 126	113 106 103 99	95 83 76 71	86 71 65 60	77 60 55 48	71 52 45 38	62 41 33 26	60 36 31 24	53 31 21 17	41 19 9 7	34 10 2 2	26 3 7 10	9 12 22 26	9 31 40 43	-216 + 49 - 70 - 78
-	125	204 224 244 265 306 428 469 510 592 673 755 796 837 878 918 959	166 182 188 201 175 209 195 177 172 157 131 121 155 150 131 129	$     \begin{array}{r}       135 \\       136 \\       135 \\       140 \\       107 \\       132 \\       116 \\       104 \\       97 \\       87 \\       69 \\       60 \\       73 \\       56 \\       58 \\       58 \\       \end{array} $	120 116 111 113 80 100 84 70 63 53 37 27 39 41 25 27	$ \begin{array}{r} 103 \\ 95 \\ 88 \\ 86 \\ 48 \\ 68 \\ 52 \\ 39 \\ 28 \\ 21 \\ + 5 \\ - 5 \\ + 6 \\ + 7 \\ - 5 \\ - 4 \end{array} $	$\begin{array}{r} 98\\ 86\\ 77\\ 72\\ 38\\ 58\\ 40\\ 27\\ 17\\ +7\\ -11\\ -19\\ -7\\ -5\\ -17\\ -16\end{array}$	$\begin{array}{r} 88\\ 74\\ 65\\ 62\\ 27\\ 46\\ 26\\ 13\\ +3\\ -7\\ -24\\ -33\\ -21\\ -17\\ -31\\ -28\end{array}$	$\begin{array}{r} 79\\ 64\\ 50\\ 48\\ 17\\ 30\\ +12\\ -2\\ -10\\ -21\\ -38\\ -46\\ -33\\ -31\\ -43\\ -40\\ \end{array}$	$\begin{array}{r} 66\\ 52\\ 36\\ 34\\ 3\\ +15\\ 0\\ -14\\ -24\\ -34\\ -52\\ -60\\ -47\\ -41\\ -55\\ -50\\ \end{array}$	$\begin{array}{r} 62\\ 50\\ 33\\ 2\\ 17\\ +2\\ -12\\ -24\\ -34\\ -52\\ -58\\ -49\\ -43\\ -57\\ -54\end{array}$	54 40 24 +24 -7 +5 -10 -24 -34 -45 -62 -71 -57 -53 -66 -60	$\begin{array}{r} 36\\ 24\\ 9\\ +10\\ +21\\ -7\\ -24\\ -36\\ -48\\ -58\\ -78\\ -84\\ -71\\ -65\\ -79\\ -72\\ \end{array}$	$\begin{array}{r} 21 \\ + 10 \\ - 3 \\ - 2 \\ - 31 \\ - 18 \\ - 32 \\ - 46 \\ - 58 \\ - 68 \\ - 88 \\ - 94 \\ - 81 \\ - 77 \\ - 87 \\ - 82 \end{array}$	$\begin{array}{r} + & 9 \\ 0 \\ - & 14 \\ - & 12 \\ - & 40 \\ - & 26 \\ - & 41 \\ - & 55 \\ - & 67 \\ - & 77 \\ - & 95 \\ - & 101 \\ - & 93 \\ - & 98 \\ - & 94 \\ - & 91 \end{array}$	$\begin{array}{r} -117\\ -12\\ -29\\ -27\\ -57\\ -43\\ -60\\ -72\\ -86\\ -96\\ -114\\ -120\\ -112\\ -107\\ -115\\ -112\\ \end{array}$	$\begin{array}{r} -189 \\ -187 \\ -38 \\ -33 \\ -71 \\ -64 \\ -81 \\ -93 \\ -106 \\ -117 \\ -133 \\ -141 \\ -136 \\ -129 \\ -139 \\ -136 \end{array}$	$\begin{array}{r} -278\\ -377\\ -393\\ -302\\ -146\\ -99\\ -122\\ -134\\ -158\\ -167\\ -185\\ -191\\ -190\\ -183\\ -191\\ -195\\ \end{array}$

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	330	397 412 428 443 473 504 535 566 597 628 690 752 814 876 907 938 969	213 222 218 222 213 208 199 196 194 184 173 155 141 153 148 136 127	$164 \\ 159 \\ 150 \\ 147 \\ 135 \\ 127 \\ 119 \\ 112 \\ 111 \\ 100 \\ 92 \\ 75 \\ 63 \\ 68 \\ 71 \\ 63 \\ 56 \\ 100 \\$	$     \begin{array}{r}       139 \\       127 \\       118 \\       111 \\       99 \\       92 \\       82 \\       77 \\       75 \\       65 \\       56 \\       41 \\       29 \\       32 \\       37 \\       30 \\       23 \\     \end{array} $	$109 \\ 89 \\ 86 \\ 79 \\ 62 \\ 55 \\ 46 \\ 39 \\ 38 \\ 29 \\ 20 \\ + 6 \\ - 4 \\ + 5 \\ - 2 \\ - 7 \\ $	97 81 72 65 48 41 32 27 22 15 + 8 - 6 - 16 - 16 - 7 - 12 - 20	$\begin{array}{c} 83\\ 65\\ 57\\ 48\\ 33\\ 25\\ 15\\ 10\\ +5\\ 0\\ -7\\ -19\\ -30\\ -30\\ -21\\ -26\\ -30\end{array}$	$\begin{array}{r} 62\\ 45\\ 38\\ 29\\ 14\\ +8\\ 0\\ -5\\ -11\\ -17\\ -23\\ -35\\ -45\\ -43\\ -36\\ -40\\ -42\end{array}$	$\begin{array}{r} 38\\ 22\\ +12\\ -2\\ -5\\ -11\\ -16\\ -21\\ -26\\ -31\\ -38\\ -49\\ -57\\ -57\\ -57\\ -50\\ -50\\ -50\\ -54\end{array}$	$ \begin{array}{r} 36 \\ 19 \\ + 9 \\ 0 \\ 0 \\ - 9 \\ - 16 \\ - 21 \\ - 26 \\ - 35 \\ - 45 \\ - 57 \\ - 52 \\ - 54 \\ - 57 \\ - 52 \\ - 54 \\ - 59 \\ \end{array} $	$ \begin{array}{r} 17 \\ + 5 \\ - 2 \\ - 9 \\ - 21 \\ - 24 \\ - 31 \\ - 40 \\ - 45 \\ - 50 \\ - 61 \\ - 71 \\ - 69 \\ - 60 \\ - 62 \\ - 64 \\ \end{array} $	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{r} -130 \\ -109 \\ -36 \\ -27 \\ -48 \\ -53 \\ -60 \\ -63 \\ -67 \\ -72 \\ -74 \\ -82 \\ -93 \\ -93 \\ -86 \\ -84 \\ -86 \end{array}$	$\begin{array}{r} -161 \\ -192 \\ -173 \\ -79 \\ -41 \\ -57 \\ -69 \\ -72 \\ -74 \\ -79 \\ -84 \\ -91 \\ -101 \\ -103 \\ -96 \\ -93 \\ -93 \\ -93 \end{array}$	$\begin{array}{r} -227\\ -247\\ -287\\ -299\\ -230\\ -52\\ -62\\ -76\\ -86\\ -95\\ -102\\ -109\\ -121\\ -122\\ -115\\ -112\\ -114\end{array}$	$\begin{array}{r} -283\\ -295\\ -316\\ -371\\ -378\\ -318\\ -132\\ -84\\ -91\\ -101\\ -119\\ -129\\ -145\\ -148\\ -139\\ -133\\ -136\end{array}$	$\begin{array}{r} -354 \\ -382 \\ -398 \\ -396 \\ -417 \\ -499 \\ -527 \\ -457 \\ -280 \\ -205 \\ -183 \\ -195 \\ -191 \\ -191 \\ -186 \\ -192 \\ \end{array}$
23	550	560 571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	228 226 235 227 218 208 198 199 192 186 171 160 146 152 147 138 126	$     \begin{array}{r}       191 \\       172 \\       170 \\       155 \\       143 \\       130 \\       119 \\       117 \\       109 \\       104 \\       87 \\       78 \\       69 \\       66 \\       67 \\       65 \\       59 \\     \end{array} $	$169 \\ 145 \\ 138 \\ 123 \\ 106 \\ 92 \\ 82 \\ 81 \\ 73 \\ 68 \\ 51 \\ 42 \\ 37 \\ 32 \\ 31 \\ 33 \\ 30$	$ \begin{array}{r} 127\\ 110\\ 105\\ 84\\ 67\\ 53\\ 45\\ 44\\ 34\\ 31\\ 15\\ 8\\ + 3\\ - 2\\ - 3\\ 2\\ 1 \end{array} $	$ \begin{array}{r} 113\\92\\86\\67\\48\\36\\26\\27\\19\\+15\\0\\-6\\-11\\-14\\-19\\-12\\-11\end{array} $	$\begin{array}{r} 94\\72\\55\\.43\\27\\17\\7\\8\\+1\\-2\\-15\\-21\\-24\\-29\\-33\\-24\\-23\end{array}$	$\begin{array}{r} 67\\ 46\\ 31\\ 19\\ +5\\ -5\\ -11\\ -11\\ -18\\ -21\\ -33\\ -38\\ -40\\ -45\\ -46\\ -38\\ -35\end{array}$	$\begin{array}{r} 31 \\ 15 \\ - 7 \\ - 79 \\ - 28 \\ - 35 \\ - 33 \\ - 38 \\ - 41 \\ - 45 \\ - 52 \\ - 52 \\ - 57 \\ - 60 \\ - 51 \\ - 47 \end{array}$	$\begin{array}{r} 31\\ 15\\ +\ 3\\ -\ 7\\ -21\\ -26\\ -31\\ -30\\ -35\\ -41\\ -41\\ -50\\ -54\\ -60\\ -62\\ -57\\ -54\\ \end{array}$	$\begin{array}{r} +10 \\ -9 \\ -14 \\ -29 \\ -40 \\ -46 \\ -53 \\ -49 \\ -52 \\ -55 \\ -64 \\ -69 \\ -66 \\ -69 \\ -72 \\ -63 \\ -59 \end{array}$	$\begin{array}{r} -148 \\ -150 \\ -74 \\ -50 \\ -53 \\ -64 \\ -74 \\ -69 \\ -71 \\ -74 \\ -81 \\ -85 \\ -83 \\ -84 \\ -86 \\ -77 \\ -71 \end{array}$	$\begin{array}{c} -173 \\ -185 \\ -204 \\ -222 \\ -185 \\ -67 \\ -58 \\ -67 \\ -74 \\ -81 \\ -91 \\ -93 \\ -91 \\ -94 \\ -97 \\ -87 \\ -79 \\ -87 \\ -79 \\ \end{array}$	$\begin{array}{r} -206 \\ -215 \\ -223 \\ -242 \\ -268 \\ -261 \\ -179 \\ -60 \\ -48 \\ -69 \\ -91 \\ -98 \\ -100 \\ -103 \\ -105 \\ -96 \\ -89 \end{array}$	$\begin{array}{r} -261 \\ -272 \\ -278 \\ -289 \\ -321 \\ -352 \\ -364 \\ -351 \\ -391 \\ -191 \\ -77 \\ -96 \\ -103 \\ -110 \\ -119 \\ -110 \\ -103 \end{array}$	$\begin{array}{r} -301 \\ -315 \\ -326 \\ -339 \\ -347 \\ -374 \\ -414 \\ -435 \\ -430 \\ -404 \\ -306 \\ -174 \\ -127 \\ -122 \\ -125 \\ -122 \\ -121 \\ \end{array}$	$\begin{array}{r} -381 \\ -390 \\ -395 \\ -410 \\ -447 \\ -455 \\ -447 \\ -452 \\ -464 \\ -473 \\ -521 \\ -525 \\ -463 \\ -384 \\ -355 \\ -314 \\ -292 \end{array}$
_	800	761 774 788 801 814 841 867 894 947 973	184 194 186 187 179 174 156 143 118 99	126 132 118 117 107 99 90 75 48 39	99 100 86 85 75 65 56 44 19 15	$ \begin{array}{r}     66 \\     63 \\     48 \\     48 \\     38 \\     20 \\     +12 \\     -9 \\     -5 \\ \end{array} $	$ \begin{array}{r}     48 \\     44 \\     29 \\     31 \\     22 \\     12 \\     + 6 \\     - 4 \\     -19 \\     -14 \\ \end{array} $	$29 \\ 23 \\ 12 \\ 12 \\ + 3 \\ - 3 \\ - 11 \\ - 19 \\ - 29 \\ - 22$	$ \begin{array}{r} + 5 \\ - 1 \\ - 12 \\ - 9 \\ - 15 \\ - 24 \\ - 28 \\ - 35 \\ - 40 \\ - 33 \\ \end{array} $	$ \begin{array}{r} -29 \\ -30 \\ -38 \\ -35 \\ -38 \\ -45 \\ -47 \\ -52 \\ -52 \\ -46 \\ \end{array} $	$ \begin{array}{r} -26 \\ -28 \\ -34 \\ -35 \\ -38 \\ -43 \\ -43 \\ -54 \\ -57 \\ -48 \\ \end{array} $	$ \begin{array}{r}88 \\57 \\ -63 \\ -57 \\ -62 \\ -63 \\64 \\67 \\64 \\57 \end{array} $	$ \begin{array}{r} -197 \\ -212 \\ -223 \\ -206 \\ -163 \\ -69 \\ -62 \\ -74 \\ -76 \\ -67 \end{array} $	$\begin{array}{r} -224\\ -228\\ -248\\ -262\\ -272\\ -270\\ -217\\ -123\\ -67\\ -60\\ \end{array}$	$\begin{array}{r} -254 \\ -254 \\ -262 \\ -271 \\ -293 \\ -322 \\ -328 \\ -309 \\ -144 \\ -84 \end{array}$	$\begin{array}{r} -302 \\ -310 \\ -312 \\ -311 \\ -317 \\ -342 \\ -380 \\ -395 \\ -388 \\ -352 \end{array}$	$\begin{array}{r} -343 \\ -349 \\ -362 \\ -364 \\ -360 \\ -361 \\ -380 \\ -397 \\ -431 \\ -441 \end{array}$	414 412 422 429 444 473 473 471 459 433 408

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## TABLE 1—continued

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## (b) $M = 1 \cdot 8$

## α(degrees)

			1															
-	$10^{3}y/s_{T}$	$10^{3}x/c_{0}$	-12.74		-6.36		-3.17	-2.11	-1.06	0	0	1.06	2.11	3.17	4.23	6.36	8.49	12.74
	0	100	178	163	133	108	98	88	80	71	72	68	63	55	50	+ 40	+ 27	+ 12
		200	177	117	85	63	53	40	28	26	28	<u>۱8</u>	13	8	+ 3	- 10	- 26	- 45
-		· 300	182	119	85	58	48	40	33	25	27	16	+ 13	+ 5	- 2	- 17	- 31	- 57
		400	174	108	76	53	41	26	18	$+\dot{8}$	9	+ 3	- 2	- 11	- 19	- 36	- 53	- 81
		500	174	107	74	47	33	21	+10	0	+ 1	— 5	- 12	- 20	- 29	- 46	- 61	- 94
		600	160	95	61	33	21	+ 7	- 3	-13	-13	-19	- 25	- 35	- 43	- 60	- 79	-112
		700	146	81	48	19	6	- 6	-16	-28	-26	-34	- 39	- 48	- 56	- 75	95	-128
_		750	135	79	43	16	2	-11	-21	-33	-33	39	- 45	- 53	- 63	- 82	-102	-131
	065	148	174	129	102	84	74	64	59	47	49	43	37	27	17	- 2	- 17	
24		193	179	123	92	69	59.	49	40	29	30	25	18	10	+ 2	- 15	-32	- 38
•		238	179	119	87	62	52	42	34	23	25	18	13	5	- 3	- 20	- 35	- 50
• •		283	176	116	86	61	49	39	29	22	22	14	9	0	- 8	-25	- 38	-63
_	125	204	176	133	111	94	84	74	66	52	56	44	34	19	÷ 7	-109	161	-216
		224	181	133	106	82	71	60	52	42	45	32	23	+ 10	- 2	- 29	-170	-253
		244	179	128	99	74	64	52	40	29	30	20	· 12	0	$-12^{-12}$	- 25	- 96	-268
		265	188	131	97	72	60	50	39	27	29	18	+ 10	Ō	$-10^{-1}$	- 25	- 22	-261
		306	162	104	80	55	40	28	16	8	10	1	- 7	- 17	- 29	- 42	- 54	-174
		428	193	123	91	63	51	36	24	+14	14	+ 6	- 3	- 13	- 21	- 38	- 55	81
		469	181	111	76	49	36	24	12	0	+ 2	5	- 13	- 23	- 32	- 49	- 67	- 97
		510	169	100	66	38	26	13	+ 3	- 9	- 7	-16	22	- 31	- 41	- 58	- 76	-109
		592	159	92	59	30	17	- 5	- 7	-17	-17	-25	- 32	- 42	- 50	- 69	- 88	-119
	1	673	153	89	52	25	$\pm 12$	-2	-13	-23	-23	-32	- 39	- 47	- 57	- 76	- 94	-126
		755	135	73 ·	36	9	- 4	-17	-28	- 39	-38	-47	- 53	- 63	- 71	- 90	-108	-138
		796	127	65	30	3	-10	-23	-34	-45	44	- 50	- 59	- 67	- 77	- 94	-115	-144
		837	132	61	28	1	-12	-26	-36	-46	-43	52	- 61	- 70	- 80	- 98	-117	
		878	137	68	33	+ б	5	-19	29	-39	-36	-45	- 54	- 64	- 73	- 91	-113	
		918	127	58	25	- 2	-15	-27	-37	-47	44	-52	— 59	- 69	- 79	- 95	-117	-151
-		959	127	62	28	+ 1	-12	-24	-34	-44	-42	-50	— 57	- 66	- 76	- 95	-113	-148
			_															

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_	330	397 412 428 443 504 535 566 597 628 690 752 814 876 907 938 969	212 215 212 211 201 194 187 181 177 172 162 145 137 130 132 135 131	$160 \\ 153 \\ 148 \\ 143 \\ 129 \\ 122 \\ 114 \\ 107 \\ 104 \\ -99 \\ 88 \\ 75 \\ 66 \\ 58 \\ 60 \\ 63 \\ 59 \\ 59 \\ 100 \\ $	$     \begin{array}{r}       135 \\       121 \\       113 \\       112 \\       96 \\       85 \\       79 \\       72 \\       68 \\       63 \\       55 \\       41 \\       33 \\       24 \\       23 \\       28 \\       26 \\     \end{array} $	$ \begin{array}{r} 109\\ 91\\ 83\\ 77\\ 62\\ 53\\ 45\\ 40\\ 37\\ 32\\ 23\\ 13\\ +3\\ -4\\ -4\\ -1\\ -3\end{array} $	$\begin{array}{r} 94\\ 74\\ 68\\ 59\\ 47\\ 38\\ 30\\ 25\\ 21\\ 16\\ +9\\ -1\\ -11\\ -17\\ -19\\ -14\\ -16\end{array}$	$78 \\ 59 \\ 51 \\ 44 \\ 30 \\ 23 \\ 15 \\ 10 \\ 6 \\ -14 \\ -23 \\ -31 \\ -28 \\ -2$	$59 \\ 40 \\ 32 \\ 27 \\ 15 \\ + 8 \\ 0 \\ - 4 \\ - 7 \\ -10 \\ -17 \\ -26 \\ -34 \\ -41 \\ -42 \\ -38 \\$	$\begin{array}{r} 39\\ 22\\ 14\\ + 5\\ 0\\ - 7\\ -15\\ -17\\ -19\\ -24\\ -29\\ -36\\ -44\\ -53\\ -54\\ -49\\ -48\end{array}$	$\begin{array}{r} 42\\ 25\\ 15\\ 7\\ + 2\\ - 6\\ - 14\\ - 15\\ - 19\\ - 22\\ - 27\\ - 34\\ - 41\\ - 49\\ - 51\\ - 46\\ - 45\end{array}$	$ \begin{array}{r}     19 \\     + 7 \\     0 \\     - 3 \\     -12 \\     -19 \\     -25 \\     -25 \\     -27 \\     -32 \\     -37 \\     -42 \\     -51 \\     -59 \\     -59 \\     -54 \\     -54 \\   \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{cccc} - 102 \\ - 79 \\ - 42 \\ - 27 \\ - 35 \\ - 44 \\ - 49 \\ - 49 \\ - 52 \\ - 58 \\ - 61 \\ - 71 \\ - 76 \\ - 78 \\ - 73 \\ - 72 \end{array}$	$\begin{array}{c} -131 \\ -143 \\ -127 \\ -84 \\ -37 \\ -48 \\ -56 \\ -57 \\ -59 \\ -62 \\ -66 \\ -71 \\ -81 \\ -86 \\ -83 \\ -82 \\ \end{array}$	$\begin{array}{r} -180 \\ -189 \\ -204 \\ -212 \\ -206 \\ -137 \\ -41 \\ -54 \\ -64 \\ -73 \\ -81 \\ -85 \\ -97 \\ -103 \\ -105 \\ -100 \\ -97 \end{array}$	$\begin{array}{r} -217\\ -226\\ -237\\ -258\\ -273\\ -275\\ -238\\ -115\\ -69\\ -78\\ -92\\ -102\\ -117\\ -122\\ -125\\ -119\\ -119\\ \end{array}$	$\begin{array}{r} -261\\ -271\\ -283\\ -283\\ -295\\ -324\\ -343\\ -343\\ -343\\ -343\\ -343\\ -297\\ -216\\ -161\\ -160\\ -153\\ -156\\ -150\\ -150\\ \end{array}$
- Эл	550	560 571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	241 230 231 218 209 201 191 190 182 174 164 155 147 137 131 133 133	$189 \\ 172 \\ 166 \\ 152 \\ 139 \\ 128 \\ 117 \\ 116 \\ 108 \\ 102 \\ 91 \\ 83 \\ 76 \\ 67 \\ 60 \\ 61 \\ 63 \\ 102 \\ 91 \\ 83 \\ 76 \\ 60 \\ 61 \\ 63 \\ 100 \\$	$\begin{array}{c} 152\\ 135\\ 127\\ 115\\ 100\\ 89\\ 79\\ 78\\ 70\\ 63\\ 54\\ 48\\ 41\\ 32\\ 25\\ 24\\ 26\end{array}$	$124 \\ 105 \\ 90 \\ 80 \\ 63 \\ 57 \\ 43 \\ 44 \\ 36 \\ 32 \\ 20 \\ 16 \\ 13 \\ + 3 \\3 \\ - 5 \\ - 2$	$ \begin{array}{r} 107\\ 86\\ 72\\ 62\\ 47\\ 37\\ 26\\ 19\\ 15\\ 5\\ +1\\ -2\\ -10\\ -17\\ -18\\ -16\\ \end{array} $	$\begin{array}{c} 87 \\ 64 \\ 50 \\ 43 \\ 28 \\ 20 \\ 10 \\ 9 \\ + 4 \\ 0 \\ -110 \\ -12 \\ -16 \\ -24 \\ -29 \\ -30 \\ -29 \end{array}$	$\begin{array}{c} 63 \\ 43 \\ 30 \\ 21 \\ 8 \\ + 3 \\ - 7 \\ - 6 \\ -12 \\ -17 \\ -23 \\ -26 \\ -29 \\ -36 \\ -42 \\ -42 \\ -41 \end{array}$	$\begin{array}{r} 32\\ 16\\ +\ 6\\ 0\\ -14\\ -17\\ -24\\ -23\\ -27\\ -31\\ -37\\ -39\\ -41\\ -47\\ -52\\ -52\\ -51\end{array}$	$\begin{array}{c} 33\\19\\8\\+1\\-12\\-15\\-22\\-19\\-24\\-25\\-34\\-38\\-39\\-46\\-49\\-48\\-49\end{array}$	$ \begin{array}{r} +18 \\ -3 \\ -10 \\ -19 \\ -29 \\ -32 \\ -37 \\ -36 \\ -41 \\ -47 \\ -51 \\ -55 \\ -60 \\ -60 \\ -57 \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r}143 \\151 \\147 \\141 \\108 \\67 \\57 \\55 \\61 \\64 \\69 \\71 \\71 \\74 \\77 \\77 \\76 \end{array}$	$\begin{array}{r} -165 \\ -169 \\ -177 \\ -185 \\ -187 \\ -171 \\ -138 \\ -87 \\ -58 \\ -57 \\ -71 \\ -76 \\ -78 \\ -83 \\ -86 \\ -85 \\ -85 \\ -85 \end{array}$	$\begin{array}{r} -208 \\ -212 \\ -214 \\ -219 \\ -229 \\ -241 \\ -250 \\ -250 \\ -250 \\ -250 \\ -250 \\ -241 \\ -135 \\ -54 \\ -80 \\ -88 \\ -91 \\ -91 \\ -95 \end{array}$	$\begin{array}{r} -238\\ -244\\ -246\\ -251\\ -256\\ -266\\ -285\\ -294\\ -302\\ -302\\ -305\\ -300\\ -252\\ -137\\ -106\\ -104\\ -101\\ -98\end{array}$	275 -280 -280 -283 -298 -310 -312 -317 -325 -323 -333 -333 -342 -334 -318 -308 -298 -280
	800	761 774 788 801 814 841 867 894 947 973	197 195 186 189 179 173 162 149 122 112	138 134 123 122 111 104 95 82 60 52	104 99 88 87 74 68 58 48 29 24	73 67 52 52 40 34 26 16 3 3	54 49 37 35 24 17 11 + 110 - 8	$ \begin{array}{r} 34\\29\\19\\16\\7\\+2\\-6\\-14\\-23\\-18\end{array} $	$ \begin{array}{r} 12 \\ + 9 \\ - 1 \\ - 2 \\ - 11 \\ - 27 \\ - 34 \\ - 28 \\ \end{array} $	$ \begin{array}{r} -16 \\ -20 \\ -23 \\ -24 \\ -32 \\ -32 \\ -36 \\ -41 \\ -45 \\ -37 \end{array} $	$ \begin{array}{r} -13 \\ -16 \\ -21 \\ -22 \\ -30 \\ -30 \\ -30 \\ -34 \\ -39 \\ -42 \\ -37 \end{array} $	$ \begin{array}{r} -51 \\ -43 \\ -48 \\ -44 \\ -48 \\ -48 \\ -49 \\ -52 \\ -53 \\ -45 \\ \end{array} $	$-157 \\ -154 \\ -142 \\ -114 \\ -88 \\ -53 \\ -54 \\ -59 \\ -60 \\ -54$		-195 - 196 - 203 - 209 - 221 - 230 - 231 - 219 - 145 - 57	-232 -230 -236 -236 -244 -252 -269 -285 -293 -288	258 259 266 268 272 269 277 293 324 324	$\begin{array}{r} -291 \\ -287 \\ -293 \\ -292 \\ -297 \\ -308 \\ -320 \\ -327 \\ -330 \\ -323 \end{array}$

## TABLE 1—continued

## (c) $M = 2 \cdot 0$

## $\alpha$ (degrees)

_	$10^3 y/s_T$	$10^{3}x/c_{0}$	-12.68	-8.45	-6·33	-4.22	-3.16	<b>2</b> ·10	-1·05	0	0	1.05	2.10	3.16	4.22	6.33	8.45	12.68
-	0	100 200 300 400 500 600 700 750	152 176 178 165 162 150 145 124	158 118 113 103 101 91 87 85	142 94 87 80 74 65 62 60	112 67 59 51 45 34 31 29	102 59 48 41 35 24 21 17	88     40     35     24     18     + 4     0     5     5	$78 \\ 31 \\ 28 \\ 17 \\ + 9 \\ - 5 \\ - 8 \\ -13$	$75 \\ 23 \\ 21 \\ 8 \\ + 1 \\ -12 \\ -15 \\ -20$	$73 \\ 19 \\ 21 \\ 8 \\ + 1 \\ -22 \\ -17 \\ -27$	$ \begin{array}{r} 68 \\ 14 \\ +13 \\ 0. \\ -8 \\ -22 \\ -25 \\ -34 \end{array} $	$ \begin{array}{r}       63 \\       9 \\       + 6 \\       - 7 \\       - 15 \\       - 27 \\       - 32 \\       - 40 \\ \end{array} $	$57 \\ 8 \\ + 2 \\ - 9 \\ - 20 \\ - 32 \\ - 37 \\ - 42$	$53 + 1 \\ - 1 \\ - 19 \\ - 28 \\ - 42 \\ - 46 \\ - 52$	$\begin{array}{rrrrr} + & 38 \\ - & 9 \\ - & 16 \\ - & 29 \\ - & 40 \\ - & 54 \\ - & 57 \\ - & 64 \end{array}$	$\begin{array}{r} + & 31 \\ - & 18 \\ - & 23 \\ - & 39 \\ - & 50 \\ - & 65 \\ - & 68 \\ - & 73 \end{array}$	$ \begin{array}{r} + 14 \\ - 40 \\ - 50 \\ - 68 \\ - 81 \\ - 95 \\ - 100 \\ - 102 \\ \end{array} $
26	065	148 193 238 283	173 177 177 173	129 124 116 113	111 102 94 88	85 75 65 59	78 65 55 50	63 48 39 35	56 39 32 25	49 34 24 18	48 31 24 18	41 22 15 8	36 19 9 3	27 10 3 2	15 2 7 11	0 14 19 23	9 24 27 31	142 48 46 55
-	125	204 224 244 265 306 428 469 510 592 673 755 796 837 878 918 959	$178 \\ 184 \\ 180 \\ 187 \\ 161 \\ 181 \\ 166 \\ 159 \\ 153 \\ 145 \\ 129 \\ 124 \\ 127 \\ 135 \\ 128 \\ 127 \\ 127 \\ 135 \\ 128 \\ 127 \\ 127 \\ 127 \\ 127 \\ 127 \\ 128 \\ 127 \\ 127 \\ 127 \\ 127 \\ 128 \\ 127 \\ 127 \\ 127 \\ 127 \\ 127 \\ 128 \\ 127 $	135 133 129 128 106 116 105 100 92 87 78 73 64 72 67 67	$ \begin{array}{c} 120\\ 114\\ 105\\ 104\\ 86\\ 90\\ 78\\ 74\\ 66\\ 61\\ 52\\ 48\\ 39\\ 47\\ 43\\ 42\\ \end{array} $	96 87 77 73 57 60 47 42 36 29 20 17 8 16 11 11	90776763454839322419 $+$ 5 - 2 + 6 2 2	73 60 48 46 28 31 20 15 + $50-12-15-19-10-16-16$	$\begin{array}{r} 64\\ 53\\ 39\\ 37\\ 18\\ 21\\ 11\\ +\\ 5\\ -\\ 3\\ -\\ 8\\ -21\\ -25\\ -29\\ -21\\ -25\\ -25\\ -25\\ \end{array}$	$\begin{array}{r} 56\\ 46\\ 31\\ 29\\ 13\\ 14\\ +\ 4\\ -\ 2\\ -10\\ -17\\ -28\\ -31\\ -34\\ -28\\ -30\\ -32\\ \end{array}$	54 44 29 27 9 14 + 4 - 2 - 10 - 19 - 33 - 36 - 38 - 32 - 37 - 35	$\begin{array}{r} 42\\ 29\\ 17\\ +15\\ -1\\ +2\\ -8\\ -12\\ -22\\ -29\\ -41\\ -42\\ -46\\ -38\\ -42\\ -43\end{array}$	$\begin{array}{r} 35\\ 22\\ 12\\ +9\\ -4\\ -3\\ -13\\ -17\\ -27\\ -36\\ -46\\ -46\\ -51\\ -45\\ -47\\ -49\\ \end{array}$	$\begin{array}{r} 21 \\ + 10 \\ 0 \\ - 2 \\ - 15 \\ - 13 \\ - 21 \\ - 26 \\ - 34 \\ - 41 \\ - 51 \\ - 55 \\ - 58 \\ - 50 \\ - 57 \\ - 56 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	84 27 27 27 40 35 43 58 58 58 75 78 78 84 76 79 79	$-117 \\ -102 \\ - 75 \\ - 32 \\ - 44 \\ - 46 \\ - 54 \\ - 60 \\ - 68 \\ - 73 \\ - 88 \\ - 94 \\ - 88 \\ - 90 \\ - 90 \\ - 90$	$\begin{array}{r}175 \\ -193 \\ -198 \\ -195 \\ -172 \\ -69 \\ -86 \\ -92 \\ -99 \\ -106 \\ -113 \\ -114 \\ -125 \\ -120 \\ -122 \\ -122 \end{array}$

	330	397 412 428 443 504 535 566 597 628 690 752 814 876 907 938 969	$\begin{array}{c} 207\\ 206\\ 205\\ 204\\ 192\\ 185\\ 179\\ 174\\ 169\\ 162\\ 154\\ 141\\ 134\\ 127\\ 127\\ 127\\ 131\\ 128 \end{array}$	$158 \\ 148 \\ 144 \\ 138 \\ 126 \\ 117 \\ 111 \\ 106 \\ 99 \\ 93 \\ 86 \\ 76 \\ 69 \\ 64 \\ 64 \\ 66 \\ 63 \\ 81 \\ 82 \\ 83 \\ 86 \\ 76 \\ 64 \\ 64 \\ 66 \\ 63 \\ 83 \\ 83 \\ 84 \\ 84 \\ 84 \\ 84 \\ 84 \\ 8$	$     \begin{array}{r}       135 \\       122 \\       117 \\       109 \\       97 \\       88 \\       81 \\       77 \\       69 \\       64 \\       59 \\       49 \\       42 \\       37 \\       36 \\       40 \\       38 \\     \end{array} $	$108 \\ 90 \\ 83 \\ 73 \\ 63 \\ 52 \\ 45 \\ 43 \\ 38 \\ 31 \\ 27 \\ 18 \\ 13 \\ 6 \\ 6 \\ 8 \\ 7 \\ 18 \\ 13 \\ 6 \\ 7 \\ 18 \\ 13 \\ 6 \\ 7 \\ 18 \\ 13 \\ 7 \\ 18 \\ 13 \\ 6 \\ 7 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 $	97787163514135312619158+ 1- 4- 4- 4- 2- 3	76 56 50 43 31 22 14 11 6 + 1 - 4 - 9 -17 -22 -23 -21 -22	59 42 33 29 15 8 + 2 - 1 - 6 - 9 - 14 - 19 - 26 - 31 - 33 - 31 - 30	$\begin{array}{r} 44 \\ 29 \\ 20 \\ 10 \\ + 7 \\ 0 \\ - 6 \\ - 10 \\ - 13 \\ - 16 \\ - 21 \\ - 24 \\ - 31 \\ - 38 \\ - 40 \\ - 36 \\ - 35 \end{array}$	$\begin{array}{r} 44\\ 27\\ 21\\ 12\\ + 9\\ 0\\ - 6\\ - 8\\ - 15\\ - 18\\ - 22\\ - 28\\ - 36\\ - 43\\ - 44\\ - 41\\ - 40\end{array}$	$ \begin{array}{r} 18 \\ + 5 \\ - 1 \\ - 7 \\ - 12 \\ - 19 \\ - 25 \\ - 25 \\ - 26 \\ - 32 \\ - 34 \\ - 38 \\ - 44 \\ - 51 \\ - 50 \\ - 50 \\ - 47 \\ \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -124 \\ -123 \\ -101 \\ -70 \\ -43 \\ -52 \\ -52 \\ -52 \\ -55 \\ -59 \\ -60 \\ -62 \\ -70 \\ -74 \\ -74 \\ -74 \\ -73 \end{array}$	$\begin{array}{r} -161 \\ -167 \\ -173 \\ -174 \\ -171 \\ -140 \\ -66 \\ -45 \\ -59 \\ -68 \\ -74 \\ -84 \\ -87 \\ -88 \\ -87 \\ -88 \\ -87 \end{array}$	$-187 \\ -191 \\ -195 \\ -203 \\ -213 \\ -207 \\ -185 \\ -139 \\ -68 \\ -64 \\ -75 \\ -80 \\ -92 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -96 \\ -97 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -97 \\ -96 \\ -97 \\ -9$	$\begin{array}{r} -221\\ -227\\ -231\\ -236\\ -242\\ -246\\ -271\\ -264\\ -271\\ -254\\ -208\\ -156\\ -140\\ -128\\ -131\\ -126\\ +27\end{array}$	
27 .	550	560 571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	229 226 227 215 203 196 183 186 176 171 162 154 149 138 131 130 129	$179 \\ 170 \\ 164 \\ 150 \\ 137 \\ 128 \\ 116 \\ 114 \\ 107 \\ 103 \\ 92 \\ 86 \\ 81 \\ 74 \\ 70 \\ 69 \\ 66 \\ 100 \\$	$     \begin{array}{r}       155\\       143\\       135\\       120\\       104\\       99\\       86\\       84\\       78\\       72\\       63\\       59\\       54\\       47\\       43\\       44\\       42     \end{array} $	$123 \\ 108 \\ 93 \\ 82 \\ 65 \\ 60 \\ 50 \\ 48 \\ 41 \\ 36 \\ 29 \\ 25 \\ 22 \\ 14 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10$	$\begin{array}{c} 110\\ 92\\ 77\\ 67\\ 52\\ 46\\ 35\\ 34\\ 27\\ 25\\ 15\\ 12\\ 10\\ + 2\\ 0\\ - 1\\ - 2\end{array}$	$\begin{array}{r} 84\\ 67\\ 52\\ 43\\ 30\\ 24\\ 13\\ 11\\ 5\\ + 2\\ - 5\\ - 9\\ - 9\\ - 9\\ - 16\\ - 19\\ - 19\\ - 21\end{array}$	$\begin{array}{r} 64\\ 46\\ 33\\ 26\\ 11\\ +9\\ -1\\ -3\\ -9\\ -11\\ -17\\ -19\\ -19\\ -26\\ -29\\ -30\\ -29\end{array}$	$\begin{array}{r} 38\\ 26\\ 14\\ +8\\ -6\\ -8\\ -15\\ -15\\ -15\\ -23\\ -24\\ -29\\ -29\\ -35\\ -36\\ -36\\ -38\end{array}$	$\begin{array}{r} 38\\ 26\\ 14\\ +8\\ -6\\ -7\\ -13\\ -15\\ -21\\ -23\\ -29\\ -31\\ -38\\ -41\\ -40\\ -39\end{array}$	$ \begin{array}{r} 1 \\ + 2 \\ - 6 \\ - 16 \\ - 26 \\ - 27 \\ - 33 \\ - 34 \\ - 38 \\ - 38 \\ - 41 \\ - 44 \\ - 43 \\ - 49 \\ - 49 \\ - 49 \\ - 48 \\ - 50 \\ \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -126\\ -126\\ -108\\ -103\\ -83\\ -56\\ -52\\ -52\\ -52\\ -57\\ -57\\ -60\\ -60\\ -58\\ -62\\ -63\\ -64\\ -62\\ \end{array}$	$\begin{array}{c} -151 \\ -153 \\ -158 \\ -161 \\ -158 \\ -140 \\ -119 \\ -90 \\ -65 \\ -57 \\ -61 \\ -67 \\ -73 \\ -72 \\ -72 \\ -72 \\ -72 \\ -72 \end{array}$	$\begin{array}{r} -178 \\ -180 \\ -182 \\ -185 \\ -192 \\ -193 \\ -194 \\ -191 \\ -191 \\ -187 \\ -164 \\ -57 \\ -60 \\ -73 \\ -73 \\ -76 \\ -77 \end{array}$	$\begin{array}{r} -192 \\ -220 \\ -196 \\ -201 \\ -204 \\ -210 \\ -214 \\ -216 \\ -220 \\ -219 \\ -212 \\ -173 \\ -138 \\ -86 \\ -80 \\ -76 \\ -77 \end{array}$	$\begin{array}{r} -225\\ -226\\ -228\\ -231\\ -238\\ -242\\ -245\\ -247\\ -253\\ -257\\ -257\\ -259\\ -261\\ -253\\ -242\\ -234\\ -235\\ -222\end{array}$	-
-	800	761 774 788 801 814 841 867 894 947 973	200 197 188 189 173 175 163 155 129 117	144 135 127 127 111 110 102 93 71 65	115 106 98 98 83 81 73 64 46 41	79 73 62 60 44 45 37 30 15 14	64 56 49 45 30 30 24 16 5 3	37 30 23 19 6 8 + 1 - 6 -14 -14	$ \begin{array}{r} 16\\13\\6\\+3\\-6\\-12\\-18\\-25\\-22\end{array} $	$ \begin{array}{r} - & 6 \\ - & 9 \\ - & 14 \\ - & 15 \\ - & 24 \\ - & 19 \\ - & 24 \\ - & 28 \\ - & 32 \\ - & 29 \end{array} $	$ \begin{array}{r} - 8 \\ -11 \\ -14 \\ -28 \\ -21 \\ -26 \\ -37 \\ -36 \\ -31 \end{array} $	$ \begin{array}{r}47 \\ -40 \\ -42 \\ -38 \\ -48 \\ -40 \\ -43 \\ -45 \\ -48 \\ -42 \\ \end{array} $	$ \begin{array}{r} -116 \\ -104 \\ -94 \\ -76 \\ -67 \\ -45 \\ -50 \\ -52 \\ -53 \\ -48 \end{array} $	$ \begin{array}{r} -156 \\ -156 \\ -159 \\ -153 \\ -149 \\ -130 \\ -109 \\ -76 \\ -51 \\ -48 \end{array} $	$-175 \\ -176 \\ -182 \\ -185 \\ -196 \\ -190 \\ -188 \\ -187 \\ -145 \\ -85 \\ -$	$-197 \\ -197 \\ -200 \\ -202 \\ -212 \\ -211 \\ -217 \\ -221 \\ -222 \\ -208 \\ $	$\begin{array}{r} -209\\ -209\\ -212\\ -214\\ -222\\ -219\\ -224\\ -231\\ -239\\ -232\end{array}$	$\begin{array}{r} -238 \\ -236 \\ -240 \\ -238 \\ -247 \\ -247 \\ -253 \\ -254 \\ -258 \\ -253 \end{array}$	-

## TABLE 1—continued

## (*d*) $M = 2 \cdot 4$

## α(degrees)

	$10^{3}y/s_{T}$	$10^{3}x/c_{0}$	-12.56	-8·37	-6.28	-4.18	-3·14	-2.09	-1.05	0	0	1.05	2.09	3.14	4·18	6.28	8.37	12.56
-	0	100 200 300 400 500 600 700 750	159 165 171 157 149 132 120 89	153 113 109 99 91 81 79 73	130 93 88 78 70 62 59 57	107 72 64 60 46 38 37 39	89 53 44 38 28 18 17 15	81 42 39 27 17 11 8 3	72 30 31 20 +10 0 - 3 - 4	67 26 24 14 + 5 - 5 - 8 - 10	$ \begin{array}{r} 65\\23\\19\\+9\\-1\\-9\\-15\\-15\end{array} $	$58 \\ 19 \\ 15 \\ + 4 \\ - 6 \\ -16 \\ -22 \\ -22$	$51 \\ 10 \\ + 6 \\ - 5 \\ - 15 \\ - 27 \\ - 31 \\ - 33$	45 8 + 3 - 9 - 19 - 29 - 36 - 35	$\begin{array}{r} 42 \\ + & 3 \\ - & 4 \\ - & 18 \\ - & 28 \\ - & 36 \\ - & 44 \\ - & 42 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrr} + & 21 \\ - & 19 \\ - & 28 \\ - & 39 \\ - & 51 \\ - & 59 \\ - & 65 \\ - & 65 \end{array}$	$\begin{array}{rrrrr} + & 6 \\ - & 33 \\ - & 42 \\ - & 55 \\ - & 67 \\ - & 73 \\ - & 79 \\ - & 76 \end{array}$
28	065	148 193 238 283	165 163 163 164	125 119 112 108	107 100 92 86	89 80 71 64	72 60 51 48	65 52 40 39	56 41 36 30	50 38 29 24	47 34 23 21	38 27 18 12	29 16 7 3	23 11 4 1	16 + 4 - 4 - 10	+ 5 - 5 - 13 - 17	14 25 30 35	- 82 - 66 - 38 - 46
-	125	204 224 265 306 428 469 510 592 673 755 796 837 878 918 959	171 184 175 179 158 176 156 148 136 119 98 96 110 117 109 111	131 130 125 125 107 109 97 92 83 78 67 63 51 57 57 55	$ \begin{array}{c} 117\\ 110\\ 105\\ 103\\ 86\\ 86\\ 73\\ 71\\ 62\\ 56\\ 49\\ 45\\ 29\\ 37\\ 37\\ 35\\ \end{array} $	99 91 82 80 64 59 50 47 38 34 27 25 7 15 14 15	$ \begin{array}{r} 84\\ 72\\ 63\\ 62\\ 46\\ 41\\ 30\\ 27\\ 20\\ 13\\ 5\\ + 2\\ - 9\\ - 3\\ - 5\\ - 3\\ \end{array} $	73 65 54 39 33 24 18 11 + 2 - 4 - 5 - 18 - 12 - 12 - 14	$\begin{array}{r} 66\\ 56\\ 45\\ 41\\ 28\\ 21\\ 12\\ + 7\\ 0\\ - 7\\ -14\\ -18\\ -27\\ -21\\ -22\\ -22\end{array}$	$\begin{array}{r} 60\\ 48\\ 38\\ 34\\ 21\\ 14\\ +2\\ -5\\ -13\\ -22\\ -23\\ -32\\ -26\\ -28\\ -28\end{array}$	55 45 34 29 17 12 + 3 - 2 - 9 - 18 - 27 - 29 - 36 - 30 - 31 - 31	$\begin{array}{r} 46\\ 34\\ 23\\ 22\\ 6\\ +1\\ -8\\ -11\\ -18\\ -25\\ -34\\ -36\\ -43\\ -37\\ -40\\ -37\end{array}$	$\begin{array}{r} 31\\ 20\\ 11\\ + 9\\ - 3\\ - 8\\ - 17\\ - 21\\ - 29\\ - 36\\ - 45\\ - 46\\ - 52\\ - 46\\ - 52\\ - 47\\ - 49\\ - 47\end{array}$	$\begin{array}{r} 26\\13\\5\\+\\4\\-\\8\\-\\13\\-\\22\\-\\25\\-\\32\\-\\39\\-\\48\\-\\50\\-\\57\\-\\51\\-\\53\\-\\51\end{array}$	$\begin{array}{r} 17\\ + 2\\ - 7\\ - 9\\ - 17\\ - 22\\ - 28\\ - 32\\ - 39\\ - 46\\ - 53\\ - 55\\ - 62\\ - 58\\ - 60\\ - 60\\ \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	99 93 73 52 42 45 55 57 63 70 77 80 89 85 85 83	$\begin{array}{r} -124 \\ -131 \\ -122 \\ -118 \\ -121 \\ -67 \\ -72 \\ -73 \\ -79 \\ -84 \\ -89 \\ -91 \\ -105 \\ -101 \\ -101 \\ -99 \end{array}$

• •	330	397 412 428 443 473 504 535 566 597 628 690 752 814 876 907 938 969	207 206 205 201 188 177 167 164 155 149 143 128 121 112 106 108 109	$158 \\ 148 \\ 140 \\ 132 \\ 123 \\ 110 \\ 100 \\ 97 \\ 89 \\ 86 \\ 78 \\ 69 \\ 61 \\ 54 \\ 50 \\ 52 \\ 53 \\ 53 \\ 53 \\ 51 \\ 52 \\ 53 \\ 51 \\ 51 \\ 52 \\ 53 \\ 53 \\ 51 \\ 51 \\ 51 \\ 52 \\ 53 \\ 53 \\ 51 \\ 51 \\ 51 \\ 51 \\ 51 \\ 51$	137 123 113 103 92 80 73 70 62 59 52 45 38 33 28 31 30	113 94 84 74 63 53 46 43 37 34 27 22 16 11 8 9 8	95 76 66 58 45 33 28 24 17 15 9 + 4 - 2 - 9 - 12 - 11 - 12	82 65 51 43 34 22 17 14 8 + 6 0 - 4 - 11 - 18 - 21 - 20 - 19	$\begin{array}{r} 67\\ 47\\ 35\\ 29\\ 18\\ 11\\ 5\\ +3\\ -3\\ -6\\ -11\\ -14\\ -20\\ -27\\ -30\\ -29\\ -30\end{array}$	$\begin{array}{r} 49\\ 32\\ 22\\ 14\\ +9\\ 0\\ -6\\ -8\\ -12\\ -15\\ -20\\ -27\\ -34\\ -37\\ -36\\ -35\\ \end{array}$	$\begin{array}{r} 48\\ 29\\ 21\\ 11\\ +5\\ -2\\ -8\\ -8\\ -13\\ -17\\ -20\\ -23\\ -29\\ -38\\ -39\\ -38\\ -39\end{array}$	$\begin{array}{c} 24\\ 11\\ +\ 4\\ -\ 9\\ -\ 16\\ -\ 21\\ -\ 22\\ -\ 26\\ -\ 28\\ -\ 31\\ -\ 32\\ -\ 38\\ -\ 45\\ -\ 48\\ -\ 47\\ -\ 48\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c} -130\\ -132\\ -128\\ -123\\ -116\\ -107\\ -88\\ -69\\ -56\\ -61\\ -61\\ -70\\ -75\\ -76\\ -75\\ -76\\ -75\\ -76\end{array}$	$\begin{array}{r} -157 \\ -159 \\ -158 \\ -159 \\ -161 \\ -161 \\ -161 \\ -158 \\ -151 \\ -113 \\ -66 \\ -70 \\ -82 \\ -89 \\ -90 \\ -89 \\ -90 \\ -89 \\ -92 \\ \end{array}$	$\begin{array}{c} -173 \\ -173 \\ -174 \\ -175 \\ -179 \\ -182 \\ -183 \\ -180 \\ -189 \\ -178 \\ -178 \\ -138 \\ -138 \\ -113 \\ -111 \\ -110 \end{array}$
29	550	560 571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	216 223 220 207 191 184 174 173 164 160 148 143 132 124 119 117 110	$171 \\ 167 \\ 156 \\ 144 \\ 126 \\ 119 \\ 109 \\ 106 \\ 98 \\ 93 \\ 85 \\ 78 \\ 74 \\ 66 \\ 63 \\ 61 \\ 60 \\ 100 \\ 1$	171 140 129 117 99 94 84 81 71 66 58 52 51 43 40 37 38	168 111 99 86 68 63 55 50 42 39 31 27 25 19 16 14 16	$ \begin{array}{r} 157\\ 88\\ 75\\ 63\\ 44\\ 40\\ 32\\ 28\\ 22\\ 19\\ 11\\ 5\\ -1\\ -2\\ -5\\ -4\\ \end{array} $	$ \begin{array}{r} 149\\73\\59\\50\\32\\29\\19\\15\\9\\6\\+2\\-4\\-7\\-12\\-11\\-14\\-16\end{array} $	$\begin{array}{c} 76 \\ 53 \\ 39 \\ 31 \\ 15 \\ 13 \\ 5 \\ + 1 \\ - 5 \\ - 8 \\ - 13 \\ - 16 \\ - 18 \\ - 22 \\ - 23 \\ - 24 \\ - 23 \end{array}$	$\begin{array}{r} 49\\ 33\\ 22\\ 15\\ +3\\ 0\\ -6\\ -10\\ -16\\ -17\\ -22\\ -25\\ -25\\ -30\\ -31\\ -31\\ -29\end{array}$	$\begin{array}{r} 42\\ 28\\ 17\\ +10\\ -3\\ -4\\ -12\\ -13\\ -20\\ -22\\ -25\\ -29\\ -31\\ -35\\ -34\\ -35\\ -34\end{array}$	$ \begin{array}{r} 19\\12\\+3\\-6\\-17\\-18\\-26\\-32\\-33\\-36\\-40\\-38\\-42\\-43\\-42\\-41\end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{r} -117\\ -120\\ -113\\ -104\\ -92\\ -80\\ -76\\ -70\\ -71\\ -69\\ -66\\ -68\\ -66\\ -67\\ -66\\ -65\\ -66\\ -65\\ -66\end{array}$	$\begin{array}{r} -135\\ -138\\ -135\\ -135\\ -131\\ -123\\ -122\\ -121\\ -123\\ -112\\ -123\\ -119\\ -118\\ -107\\ -91\\ -74\\ -66\\ -62\\ -64\\ \end{array}$	$\begin{array}{r} -155 \\ -160 \\ -158 \\ -160 \\ -157 \\ -158 \\ -158 \\ -158 \\ -161 \\ -162 \\ -163 \\ -161 \\ -152 \\ -146 \\ -139 \\ -132 \\ -113 \end{array}$	$\begin{array}{r} -167\\ -171\\ -172\\ -172\\ -172\\ -172\\ -172\\ -172\\ -172\\ -178\\ -179\\ -182\\ -177\\ -178\\ -179\\ -182\\ -177\\ -174\\ -170\\ -169\\ -155\end{array}$
	800	761 774 788 801 814 841 867 894 947 973	196 188 182 180 162 165 150 140 121 114	136 128 118 118 106 102 94 86 69 65	111 103 93 79 79 71 62 47 45	82 76 64 50 52 42 35 24 24	59 53 43 41 26 28 20 12 4 4 4	$\begin{array}{r} 42 \\ 36 \\ 28 \\ 24 \\ 12 \\ 14 \\ - 1 \\ - 7 \\ - 5 \end{array}$	242010+10- 3+ 1- 7-13-20-16	$ \begin{array}{r}     4 \\     + 2 \\     - 6 \\     - 17 \\     - 12 \\     - 16 \\     - 22 \\     - 27 \\     - 23 \\ \end{array} $	$ \begin{array}{r} - 3 \\ - 5 \\ - 12 \\ - 24 \\ - 17 \\ - 22 \\ - 28 \\ - 32 \\ - 27 \\ \end{array} $	$ \begin{array}{r} -21 \\ -23 \\ -30 \\ -28 \\ -37 \\ -32 \\ -34 \\ -39 \\ -41 \\ -36 \end{array} $	$ \begin{array}{r}112 \\ -87 \\ -69 \\ -54 \\ -58 \\ -47 \\ -52 \\ -54 \\ -54 \\ -54 \\ -48 \end{array} $	$ \begin{array}{r} -133 \\ -116 \\ -104 \\ -92 \\ -90 \\ -71 \\ -62 \\ -60 \\ -57 \\ -52 \end{array} $	$-153 \\ -146 \\ -142 \\ -131 \\ -129 \\ -115 \\ -105 \\ -97 \\ -79 \\ -63$	$-158 \\ -154 \\ -155 \\ -151 \\ -154 \\ -144 \\ -141 \\ -139 \\ -132 \\ -123$	$\begin{array}{r} -173 \\ -170 \\ -173 \\ -171 \\ -175 \\ -167 \\ -168 \\ -167 \\ -170 \\ -163 \end{array}$	180 177 180 178 178 177 178 179 172

## TABLE 1—continued

## (e) M = 2.8

## α(degrees)

$10^{3}y/s_{T}$	$10^{3}x/c_{0}$	-12.44	-8·30	-6.23	-4·15	$-3 \cdot 11$	-2.07	-1·04	0	0	1.04	2.07	3.11	4.15	6 · 23	8.30	12.44
0	100 200 300 400 500 600 700 750	157 156 156 143 138 123 113 88	151 115 107 100 95 90 88 82	129 91 85 77 70 66 64 64	106 70 62 55 48 43 43 43 47	94 56 48 42 35 31 29 31	87 40 36 30 23 17 15 15	73 32 31 24 15 9 7 7	$ \begin{array}{r} 67 \\ 25 \\ 21 \\ 10 \\ 3 \\ + 2 \\ - 2 \\ - 6 \end{array} $	$ \begin{array}{r} 65\\ 21\\ 17\\ 8\\ +1\\ -2\\ -4\\8\end{array} $	$ \begin{array}{r} 62\\ 21\\ 17\\ 8\\ +1\\ -4\\ -8\\ -8\end{array} $	$56 \\ 15 \\ 11 \\ + 2 \\ - 5 \\ - 10 \\ - 14 \\ - 14$	$50 \\ 11 \\ + 7 \\ - 3 \\ - 11 \\ - 16 \\ - 20 \\ - 20$	$ \begin{array}{r}     44 \\     + 5 \\     - 1 \\     - 11 \\     - 18 \\     - 24 \\     - 24 \\     - 30 \\ \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} + & 28 \\ - & 14 \\ - & 20 \\ - & 31 \\ - & 38 \\ - & 41 \\ - & 45 \\ - & 45 \end{array}$	$\begin{array}{rrrrr} + & 17 \\ - & 22 \\ - & 30 \\ - & 42 \\ - & 49 \\ - & 53 \\ - & 56 \\ - & 55 \end{array}$
065 30	148 193 238 283	161 155 155 152	127 122 114 109	104 98 90 83	84 77 69 62	75 63 55 50	61 49 41 38	55 41 37 30	45 37 24 22	41 33 24 18	39 29 22 16	33 22 14 9	26 16 8 5	14 6 0 3	$\begin{array}{c} 0 \\ - & 6 \\ - & 14 \\ - & 17 \end{array}$	12 17 23 25	56 50 47 36
125	204 224 244 265 306 428 469 510 592 673 755 796 837 878 918 959	168 180 169 171 152 162 148 140 129 112 91 88 104 109 101 103	136 131 127 127 107 99 96 90 84 75 73 59 64 64 64	$ \begin{array}{c} 117\\108\\104\\104\\85\\82\\73\\73\\65\\61\\55\\55\\36\\40\\42\\42\\42\end{array} $	97 88 80 78 64 58 50 49 43 39 34 33 12 17 21 19	85 75 67 65 52 45 36 36 36 29 24 20 18 2 5 7 7 7	$ \begin{array}{r} 73\\63\\53\\53\\38\\29\\24\\22\\16\\10\\4\\+4\\-9\\-7\\-7\\-7\\-5\end{array}$	$\begin{array}{r} 67\\ 57\\ 47\\ 45\\ 29\\ 21\\ 16\\ 14\\ 8\\ + 2\\ - 4\\ - 4\\ - 17\\ - 14\\ - 13\\ - 13\end{array}$	54 47 35 31 21 11 9 + 4 0 - 8 -11 -12 -27 -22 -20 -24	52 43 33 29 17 9 5 + 2 - 4 - 12 - 17 - 16 - 29 - 24 - 22 - 24	52 39 29 26 13 6 + 1 - 2 - 6 - 14 - 19 - 20 - 31 - 26 - 24	$\begin{array}{r} 38\\ 27\\ 18\\ 16\\ + 5\\ 0\\ - 5\\ - 9\\ - 14\\ - 20\\ - 25\\ - 25\\ - 37\\ - 34\\ - 32\\ - 32\end{array}$	$\begin{array}{r} 28\\18\\10\\+6\\-3\\-8\\-13\\-8\\-13\\-20\\-25\\-31\\-31\\-45\\-40\\-40\\-38\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$

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	330	397           412           428           443           473           504           535           566           597           628           690           752           814           876           907           938           969	209 204 201 194 188 175 166 162 158 150 142 128 116 104 99 100 101	156 141 136 129 120 106 99 91 87 87 83 73 67 61 58 59 56	$132 \\ 116 \\ 109 \\ 100 \\ 90 \\ 79 \\ 74 \\ 72 \\ 64 \\ 60 \\ 57 \\ 49 \\ 43 \\ 38 \\ 35 \\ 36 \\ 33 \\ 33 \\ 33 \\ 33 \\ 33 \\ 33$	111. 92 83 73 65 53 46 46 38 35 34 26 20 16 13 14 11	99 78 69 51 40 35 35 27 23 22 14 8 2 1 4 8 2 1 0 0	83 63 54 45 37 26 21 15 9 8 + 2 - 4 - 9 - 11 - 13 - 14	$\begin{array}{r} 67\\ 47\\ 38\\ 31\\ 23\\ 14\\ 9\\ 9\\ +3\\ -1\\ -2\\ -7\\ -11\\ -17\\ -18\\ -21\\ -20\\ \end{array}$	$50 \\ 31 \\ 24 \\ 16 \\ 10 \\ + 2 \\ - 3 \\ - 7 \\ -11 \\ -11 \\ -15 \\ -19 \\ -25 \\ -28 \\ -29 \\ -28$	$\begin{array}{r} 46\\ 29\\ 20\\ 12\\ + 8\\ - 2\\ - 5\\ - 5\\ - 11\\ - 13\\ - 13\\ - 17\\ - 21\\ - 27\\ - 30\\ - 29\\ - 30\end{array}$	$\begin{array}{r} 32\\ 18\\ 13\\ +4\\ -2\\ -7\\ -11\\ -11\\ -16\\ -18\\ -19\\ -21\\ -25\\ -31\\ -32\\ -33\\ -34 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{r} -108 \\ -105 \\ -93 \\ -88 \\ -80 \\ -75 \\ -69 \\ -65 \\ -65 \\ -65 \\ -54 \\ -58 \\ -62 \\ -63 \\ -64 \\ -64 \end{array}$	$\begin{array}{c} -122\\ -122\\ -120\\ -117\\ -113\\ -100\\ -108\\ -100\\ -104\\ -102\\ -89\\ -67\\ -69\\ -67\\ -69\\ -69\\ -70\end{array}$	$\begin{array}{c} -131\\ -132\\ -129\\ -128\\ -128\\ -128\\ -128\\ -128\\ -128\\ -127\\ -127\\ -127\\ -127\\ -120\\ -104\\ -106\\ -102\\ -100\\ -97\\ -95\end{array}$
22		560 571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	186 229 221 211 193 186 174 172 163 156 147 136 126 119 114 115 106	189 174 164 152 135 127 117 113 104 99 88 81 81 74 73 69 71	$187 \\ 147 \\ 136 \\ 121 \\ 105 \\ 98 \\ 89 \\ 84 \\ 75 \\ 72 \\ 63 \\ 53 \\ 55 \\ 48 \\ 47 \\ 44 \\ 47 \\ 44 \\ 47 \\ 100 \\ $	$184 \\ 117 \\ 103 \\ 93 \\ 74 \\ 69 \\ 60 \\ 56 \\ 47 \\ 44 \\ 37 \\ 30 \\ 30 \\ 25 \\ 24 \\ 20 \\ 24$	$176 \\ 100 \\ 86 \\ 76 \\ 58 \\ 53 \\ 42 \\ 41 \\ 32 \\ 29 \\ 22 \\ 16 \\ 16 \\ 9 \\ 10 \\ 7 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 $	$ \begin{array}{r} 107\\80\\68\\58\\40\\35\\27\\23\\14\\13\\8\\0\\+2\\-5\\-6\\-7\\-4\end{array} $	$\begin{array}{r} 83\\62\\52\\44\\29\\22\\13\\11\\4\\-7\\-7\\-7\\-14\\-14\\-15\\-11\end{array}$	$\begin{array}{r} 43\\ 31\\ 23\\ 13\\ 8\\ +1\\ 0\\ -7\\ -11\\ -14\\ -19\\ -21\\ -24\\ -24\\ -25\\ -25\end{array}$	$50 \\ 35 \\ 25 \\ 17 \\ 7 \\ + 4 \\ - 3 \\ - 4 \\ - 11 \\ - 15 \\ - 16 \\ - 23 \\ - 26 \\ - 26 \\ - 27 \\ $	$\begin{array}{c} 41\\ 25\\ 17\\ +9\\ -1\\ -6\\ -11\\ -10\\ -17\\ -16\\ -24\\ -27\\ -25\\ -30\\ -29\\ -31\\ -25\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} -106\\ -109\\ -106\\ -96\\ -88\\ -84\\ -80\\ -83\\ -81\\ -78\\ -78\\ -78\\ -77\\ -72\\ \end{array}$	$\begin{array}{r} -117\\ -121\\ -117\\ -119\\ -108\\ -103\\ -108\\ -103\\ -106\\ -104\\ -105\\ -108\\ -102\\ -106\\ -103\\ -104\\ -99\end{array}$	$\begin{array}{r} -123\\ -124\\ -123\\ -125\\ -123\\ -120\\ -119\\ -111\\ -122\\ -119\\ -120\\ -124\\ -118\\ -119\\ -118\\ -122\\ -114\end{array}$
	800	761 774 788 801 814 841 867 894 947 973	199 189 181 180 161 164 149 136 122 116	146 138 128 129 114 115 106 97 82 78	119 111 99 85 87 77 70 57 55	89 83 71 72 57 58 51 42 31 33	71 67 56 40 42 36 27 18 20	54 48 38 36 22 26 18 9 2 4	$ \begin{array}{r} 38\\32\\24\\25\\13\\14\\+6\\-3\\-6\\-4\end{array} $	$ \begin{array}{r} 15 \\ 9 \\ 5 \\ -3 \\ -9 \\ -16 \\ -20 \\ -12 \end{array} $	$ \begin{array}{r} 11 \\ 5 \\ + 1 \\ - 1 \\ - 11 \\ - 7 \\ - 13 \\ - 18 \\ - 22 \\ - 16 \\ \end{array} $	$ \begin{array}{r} -1 \\ -7 \\ -7 \\ -7 \\ -17 \\ -11 \\ -15 \\ -22 \\ -26 \\ -20 \\ \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{r} -114 \\ -101 \\ -99 \\ -87 \\ -70 \\ -64 \\ -63 \\ -59 \\ -51 \\ \end{array} $	$-132 \\ -126 \\ -128 \\ -119 \\ -119 \\ -102 \\ -95 \\ -92 \\ -84 \\ -72$	$\begin{array}{r} -139 \\ -133 \\ -135 \\ -131 \\ -133 \\ -118 \\ -116 \\ -113 \\ -111 \\ -97 \end{array}$	$-139 \\ -133 \\ -137 \\ -133 \\ -134 \\ -126 \\ -124 \\ -125 \\ -122 \\ -109$

 $\frac{31}{31}$ 

## TABLE 2

Values of  $10^3 C_p$ : Transition Free, Small Sting Shroud,  $R = 1 \times 10^6/ft$ 

## $M = 2 \cdot 0$

α(degrees)

$10^3 y/s_T$	$10^{3}x/c_{0}$	-8.22	-6.16	-4·11	-2.05	0	2.05	· 4·11	6.16	8.22
0	100     200     300     400     500     600     700     750	072 104 104 89 83 76 65 48	72 93 90 75 70 66 58 48	68 62 55 44 42 32 24 20	103 51 44 29 30 19 8 4	95332615+ 9- 5- 16- 10	$ \begin{array}{r}                                     $	$ \begin{array}{r} 77 \\ + & 6 \\ - & 1 \\ - & 12 \\ - & 21 \\ - & 32 \\ - & 43 \\ - & 39 \end{array} $	+ 62 - 11 - 18 - 36 - 42 - 53 - 68 - 61	+ 63 8 - 18 - 36 - 46 - 54 - 65
065	148 193 238 283	108 101 101 102	104 98 91 89	79 66 60 61	73 55 45 46	51 34 27 25	34 20 14 11	20 7 0 1	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
125	204 224 244 265 306 428 469 510 592 673 755 796 837 878 918	$ \begin{array}{r} 119\\ 118\\ 115\\ 100\\ 88\\ 85\\ 79\\ 78\\ 68\\ 45\\ 41\\ 55\\ 63\\ 50\\ \end{array} $	$ \begin{array}{c} 115\\ 108\\ 104\\ 104\\ 87\\ 74\\ 72\\ 69\\ 64\\ 61\\ 42\\ 37\\ 38\\ 50\\ 39\\ \end{array} $	90 79 73 70 55 44 41 35 30 23 11 7 5 12 2	$\begin{array}{c} 81\\ 69\\ 59\\ 55\\ 41\\ 39\\ 29\\ 22\\ 17\\ 7\\ -2\\ -7\\ -12\\ -1\\ -11\\ -11\end{array}$	$59 \\ 45 \\ 34 \\ 36 \\ 16 \\ 14 \\ + 8 \\ - 2 \\ - 7 \\ - 10 \\ - 22 \\ - 21 \\ - 29 \\ - 21 \\ - 32 \\ -$	$\begin{array}{c} 38\\ 24\\ 14\\ +14\\ -1\\ -6\\ -9\\ -15\\ -24\\ -27\\ -36\\ -41\\ -49\\ -42\\ -52\\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$

(89022)

330 - 9 -123-167-183397 153 129 104 84 42 -----178-187412 142 114 86 62 24 - 10 -107-190428 77 53 18 - 16 - 76 -178136 109 -191 - 50 42 7 - 20 -168443 128 98 63 -191 24 - 43 -151473 118 91 56 35 +3 \_\_\_\_ 29 - 49 -118-182504 48 29 5 109 82 -----\_ 535 104 80 45 23 \_ 4 \_\_\_\_ 31 - 51 - 80 23 --- 59 -126 566 73 39 8 - 31 - 51 ------ 74 -- 56 32 13 - 15 - 35 - 54 - 63 - 597 94 66 628 87 60 26 9 - 18 -- 42 - 58 - 69 - 74 - 71 9 - 39 - 59 690 79 59 25 - 19 - 75 - 77 752 49 2 - 26 - 42 - 59 69 15 +814 45 11 2 - 29 \_ 46 \*\*\*\*\* 65 — 84 - 85 66 -- 12 - 92 35 + 1 - 36 - 56 - 72 - 94 876 52 - 71 - 90 - 94 907 53 36 - 1 - 15 - 35 - 55 - 88 - 88 938 52 38 + 1- 12 - 36 - 53 - 69 - 89 - 17 - 37 - 73 - 88 969 51 34 0 - 54 550 93 47 - 65 -176--- 181 560 -135164 157 118 --- 74 -184-186571 156 138 100 70 28 -143- 25 -185582 148 130 88 61 20 -138-179 -18851 9 -----25 -141 -186 593 137 117 79 +— -198 616 124 103 62 34 -----1 35 -131 -193 -110-194 28 — 3 34 -189639 111 91 56 \_ -19545 23 - 11 --- 42 --- 94 -186661 107 87 -19091 47 21 - 10 - 37 — 73 -181684 108 -196 38 15 - 19 - 42 - 69 -180707 99 75 - 61 --- 172 -191 729 94 73 35 16 - 18 — 45 -151-184 774 81 61 23 3 24 - 47 - 63 +\_\_\_\_ - 91 -15855 18 2 - 29 -- 49 --- 69 819 76 --11372 55 18 \_ 2 - 26 - 46 - 62 - 60 864 — 77 8 - 32 - 52 - 71 - 76 43 9 910 60 ----- 73 - 76 3 - 34 ----54 - 70 932 54 40 - 10 - 75 --- 37 — 53 - 73 - 82 955 55 38 4 - 13 - 78 55 - 16 - 33 - 53 - 65 - 81 977 38 5 761 2 -202-20474 -118-166800 133 115 46 \_ - 99 -201\_ -196744 128 111 69 38 4 -204788 57 32 ----9 - 87 -166-202119 102 -205 27 \_ 8 - 72 -161-203801 117 97 55 -212 814 96 79 38 16 - 19 - 66 -168-210-205-21182 41 18 -- 16 - 43 -156841 99 -152-21793 72 35 9 - 19 - 42 ---211 867 894 77 60 22 3 - 28 -- 48 -145-214-223+-225 - 31 - 51 -110-216 47 10 3 947 61 — -203---215 - 27 - 44 - 70 973 57 44 10 ----3

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С

## TABLE 3

Values of  $10^3 C_p$ : Transition Fixed, Large Sting Shroud,  $R = 2 \times 10^6/ft$ 

(a) M = 1.4

(b)  $M = 1 \cdot 8$ 

∝(degrees)

α(degrees)

$10^3 y/s_T$	$10^{3}x/c_{0}$	-6.41	-4·27	-2·12	0	2.12	4.27	6.41		-6.36	-4.23	-2·11	0	2.11	4.23	6.36
0	100 200 300 400 500 600	89 84 97 78 71 59	91 , 66 71 52 42 30	91 47 49 28 14 3	$72 \\ 31 \\ 30 \\ + 8 \\ - 8 \\ - 21$	$57 \\ 14 \\ + 9 \\ - 11 \\ - 27 \\ - 42$	+36 - 1 - 8 - 28 - 45 - 62	+36 - 17 - 21 - 47 - 64 - 71	<b>-</b>	76 66 79 65 65 52	80 51 60 45 43 30	80 36 40 25 21 8	$69 \\ 20 \\ 22 \\ + 5 \\ 0 \\ - 12$	$59 \\ 11 \\ + 12 \\ - 8 \\ - 14 \\ - 27$	+ 49 - 1 - 4 - 24 - 31 - 45	+ 39 - 12 - 17 - 37 - 44 - 61
065	148 193 238 283	115 101 95 91	98 81 73 67	81 62 50 45	64 43 30 25	43 23 9 6	$+ 23 \\ 0 \\ 9 \\ - 13$	$\begin{array}{r} 0 \\ - 20 \\ - 30 \\ - 32 \end{array}$	_	99 84 77 75	86 69 60 57	71 52 40 37	54 34 22 18	38 19 8 5		-1 -14 -22 -25
125	204 224 244 265 306 428 469 510 592 673 755 796 837 878 918 959	134 110 99 103 74 93 78 64 53 50 40 33 35 28 14 14	122 93 76 79 48 64 47 35 24 21 14 6 - 3 - 13 - 15	$ \begin{array}{r} 106\\ 72\\ 55\\ 24\\ 38\\ 21\\ + 7\\ - 3\\ - 8\\ - 15\\ - 21\\ - 22\\ - 29\\ - 39\\ - 39\end{array} $	$\begin{array}{r} 88\\ 50\\ 28\\ 31\\ -\\ -\\ 14\\ -\\ 3\\ -\\ 17\\ -\\ 29\\ -\\ 32\\ -\\ 40\\ -\\ 45\\ -\\ 46\\ -\\ 49\\ -\\ 59\\ -\\ 59\end{array}$	$59 \\ 23 \\ 2 \\ + 7 \\ - 20 \\ - 8 \\ - 23^{\circ} \\ - 35 \\ - 49 \\ - 54 \\ - 61 \\ - 68 \\ - 66 \\ - 71 \\ - 80 \\ - 78 \\ - 78 \\ - 78 \\ - 78 \\ - 80 \\ - 78 \\ - 80 \\ - 78 \\ - 80 \\ - 78 \\ - 80 $	$\begin{array}{r} + 28 \\ - 6 \\ - 25 \\ - 18 \\ - 44 \\ - 29 \\ - 45 \\ - 58 \\ - 71 \\ - 78 \\ - 85 \\ - 90 \\ - 88 \\ - 95 \\ - 102 \\ - 98 \end{array}$	$\begin{array}{r} -105\\ -25\\ -46\\ -39\\ -64\\ -51\\ -66\\ -78\\ -93\\ -100\\ -109\\ -114\\ -112\\ -119\\ -104\\ -122\\ \end{array}$	-	117 98 84 88 69 83 71 59 49 40 33 28 36 28 18 18	$ \begin{array}{r} 108 \\ 79 \\ 66 \\ 68 \\ 48 \\ 56 \\ 46 \\ 26 \\ 21 \\ 19 \\ 13 \\ 9 \\ + 1 \\ - 6 \\ - 4 \end{array} $	$\begin{array}{r} 93\\61\\46\\27\\34\\23\\14\\-2\\-3\\-9\\-14\\-22\\-27\\-27\\-27\end{array}$	$\begin{array}{r} 73\\ 39\\ 24\\ 25\\ 9\\ 12\\ + 3\\ - 8\\ - 18\\ - 24\\ - 24\\ - 27\\ - 33\\ - 41\\ - 46\\ - 47\end{array}$	$50 \\ 18 \\ 6 \\ + 6 \\ - 9 \\ - 6 \\ - 16 \\ - 24 \\ - 34 \\ - 41 \\ - 43 \\ - 43 \\ - 51 \\ - 58 \\ - 65 \\ - 62 $	$\begin{array}{r} + 18 \\ - 8 \\ - 18 \\ - 17 \\ - 31 \\ - 24 \\ - 36 \\ - 43 \\ - 53 \\ - 63 \\ - 63 \\ - 66 \\ - 71 \\ - 76 \\ - 83 \\ - 81 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$

330	397 412 428 443 504 535 566 597 628 690 752 814 876 907 938 969	184 137 116 108 93 87 78 70 64 60 48 41 28 28 28 28 28 19 14	$ \begin{array}{r} 161\\ 106\\ 86\\ 77\\ 58\\ 53\\ 44\\ 36\\ 28\\ 28\\ 17\\ + 12\\ - 3\\ - 3\\ - 3\\ - 10\\ - 13\\ \end{array} $	$128 \\ 72 \\ 51 \\ 41 \\ 24 \\ 21 \\ 12 \\ + 6 \\ - 3 \\ - 5 \\ - 15 \\ - 18 \\ - 30 \\ - 30 \\ - 30 \\ - 30 \\ - 35 \\ - 37 \\ - $	$\begin{array}{r} 89\\ 31\\ 17\\ + 7\\ - 8\\ - 12\\ - 17\\ - 25\\ - 32\\ - 32\\ - 41\\ - 42\\ - 54\\ - 54\\ - 54\\ - 52\\ - 58\\ - 58\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	-155 - 172 - 169 - 92 - 49 - 60 - 70 - 75 - 83 - 89 - 88 - 98 - 100 - 99 - 90 - 100 - 90 - 9	$\begin{array}{r} -222\\ -235\\ -276\\ -296\\ -252\\ -66\\ -63\\ -95\\ -99\\ -109\\ -109\\ -122\\ -122\\ -122\\ -122\\ -122\\ -122\\ -122\\ -122\\ -122\\ \end{array}$		176 134 111 103 89 81 75 68 61 59 51 43 35 29 26 23 21	$ \begin{array}{r} 149\\ 101\\ \cdot 80\\ 71\\ 58\\ 50\\ 43\\ 36\\ 31\\ 30\\ 20\\ 14\\ 6\\ + 1\\ - 1\\ - 4\\ - 6\\ \end{array} $	$\begin{array}{c} 117\\ 70\\ 50\\ 42\\ 29\\ 20\\ 13\\ 9\\ 4\\ + & 4\\ - & 6\\ - & 11\\ - & 17\\ - & 22\\ - & 24\\ - & 26\\ - & 27\end{array}$	$\begin{array}{r} 82\\ 32\\ 15\\ + 9\\ - 1\\ - 6\\ - 13\\ - 16\\ - 19\\ - 21\\ - 28\\ - 31\\ - 37\\ - 41\\ - 44\\ - 46\\ - 46\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -129 \\ -132 \\ -80 \\ -44 \\ -53 \\ -59 \\ -61 \\ -65 \\ -65 \\ -70 \\ -71 \\ -79 \\ -80 \\ -81 \\ -83 \\ -83 \\ -83 \end{array}$	-174 - 182 - 201 - 207 - 204 - 145 - 56 - 70 - 75 - 83 - 85 - 96 - 98 - 100 - 100
550	571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	144 127 117 98 86 72 72 66 60 49 41 37 30 25 23 16	$ \begin{array}{r} 115 \\ 91 \\ 81 \\ 62 \\ 50 \\ 37 \\ 37 \\ 30 \\ 25 \\ 14 \\ 11 \\ + 4 \\ - 1 \\ - 4 \\ - 6 \\ - 10 \\ \end{array} $	$\begin{array}{r} 76\\ 50\\ 40\\ 23\\ +\ 11\\ -\ 1\\ +\ 1\\ -\ 6\\ -\ 11\\ -\ 18\\ -\ 22\\ -\ 23\\ -\ 30\\ -\ 32\\ -\ 33\\ -\ 33\end{array}$	$\begin{array}{r} 24 \\ + 2 \\ - 6 \\ - 22 \\ - 29 \\ - 39 \\ - 35 \\ - 40 \\ - 51 \\ - 52 \\ - 51 \\ - 52 \\ - 51 \\ - 54 \\ - 56 \\ - 54 \\ - 54 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -221\\ -226\\ -243\\ -273\\ -267\\ -190\\ -81\\ -54\\ -74\\ -93\\ -97\\ -95\\ -98\\ -100\\ -95\\ -97\end{array}$	$\begin{array}{r} -283\\ -286\\ -295\\ -325\\ -358\\ -375\\ -366\\ -318\\ -218\\ -83\\ -97\\ -105\\ -112\\ -117\\ -114\\ -114\end{array}$	-	$ \begin{array}{r} 129\\120\\112\\94\\84\\71\\70\\65\\56\\48\\46\\38\\30\\26\\25\\20\end{array} $	$ \begin{array}{r} 101\\ 88\\ 78\\ 63\\ 51\\ 41\\ 38\\ 33\\ 26\\ 18\\ 14\\ 13\\ 5\\ + 1\\ 0\\ - 2 \end{array} $	$\begin{array}{c} 66\\ 51\\ 45\\ 26\\ 19\\ 10\\ 6\\ + 3\\ - 4\\ - 9\\ - 12\\ - 12\\ - 12\\ - 18\\ - 22\\ - 24\\ - 25\end{array}$	$ \begin{array}{r} 11\\ 10\\ + 3\\ - 13\\ - 16\\ - 24\\ - 26\\ - 29\\ - 34\\ - 36\\ - 39\\ - 39\\ - 43\\ - 44\\ - 44\\ - 47\\ \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -173 \\ -176 \\ -185 \\ -190 \\ -178 \\ -146 \\ -98 \\ -59 \\ -59 \\ -59 \\ -74 \\ -80 \\ -78 \\ -81 \\ -81 \\ -81 \\ -83 \\ \end{array}$	$\begin{array}{r} -212\\ -213\\ -217\\ -229\\ -239\\ -245\\ -245\\ -245\\ -245\\ -245\\ -61\\ -78\\ -88\\ -88\\ -88\\ -93\\ \end{array}$
800	761 774 788 801 814 841 867 894 947 973	120 91 83 79 70 60 52 41 18 11	$ \begin{array}{r} 86 \\ 55 \\ 49 \\ 45 \\ 36 \\ 28 \\ 20 \\ + 12 \\ - 6 \\ - 6 \\ \end{array} $	$ \begin{array}{r}     45 \\     16 \\     8 \\     + 4 \\     - 1 \\     - 8 \\     - 14 \\     - 18 \\     - 28 \\     - 23 \\ \end{array} $	- 13 - 35 - 40 - 38 - 42 - 45 - 47 - 47 - 49 - 47 - 42	$-177 \\ -199 \\ -211 \\ -207 \\ -179 \\ -80 \\ -55 \\ -66 \\ -68 \\ -61 \\ -61$	$\begin{array}{r} -247 \\ -260 \\ -264 \\ -269 \\ -288 \\ -318 \\ -332 \\ -313 \\ -144 \\ -85 \end{array}$	$\begin{array}{r} -301 \\ -318 \\ -320 \\ -320 \\ -324 \\ -344 \\ 392 \\ -418 \\ -419 \\ -382 \end{array}$	-	$ \begin{array}{r} 112\\90\\82\\75\\68\\60\\45\\41\\26\\20\end{array} $	81 61 52 47 39 30 22 16 3 3	$\begin{array}{r} 43\\ 26\\ 17\\ 15\\ 7\\ +1\\ -7\\ -11\\ -19\\ -15\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$-150 \\ -150 \\ -141 \\ -119 \\ -95 \\ -57 \\ -57 \\ -61 \\ -61 \\ -52$	$\begin{array}{r} -196 \\ -198 \\ -203 \\ -206 \\ -210 \\ -225 \\ -230 \\ -225 \\ -156 \\ -63 \end{array}$	228 228 235 235 237 247 263 276 277 270

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## TABLE 3—continued

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(c)	Μ	=	2.	0
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α(degrees)

(d)  $M = 2 \cdot 4$  $\alpha$ (degrees) -

$10^{3}y/s_{T}$	$10^{3}x/c_{0}$	-6.33	-4·22	-2.10	0	2.10	4.22	6.33	-6.28	-4·18	-2.09	0	2.09	4.18	6·28	
0	100	74	76 52	76	64 13	51 -+ 3	+ 39 - 10	+ 31 - 20	 74 70	74 54	77	68 18	58 9	+ 44	+ 35 - 14	-
	300	78	56	31	+ 12	, <u>0</u>	-15	- 23	76	55	33	17	+ 6	- 10	-20	
	400	63	12	19	- 1	- 13	- 31	- 42	64	42	23	+ 3	8	- 24	- 36	
'	500	64	12	17	- 3	- 17	- 35	- 49	61	38	17	- 1	- 12	- 30	— 41	
	600	53	31	6	- 16	- 30	- 50	62	48	32	7	- 13	- 24	— 36	- 49	
065	148	102	87	65	45	31	+ 9	- 9	 98	84	62	44	32	16	- 6	-
	193	88	70	46	26	+ 13	- 7	- 21	87	73	48	28	16	+ 3	— 13	
	238	79	58	34	14	0	<u> </u>	- 32	76	57	37	19	5	- 11	- 26	
	283	76	54	31	11	- 1	. – 21	- 33	 76	57	35	17	5	- 11	- 26	
125	204	119	107	86	64	42	+ 10	- 77	120	102	84	65	43	+ 15	— 57	
	224	102	80	55	31	13	- 17	- 38	98	82	57	35	17	- 4	- 29	
	244	88	68	41	20	+ 3	- 26	— 39	89	71	48	26	10	- 11	— 31	
	265	89	67	39	17	0	— 25	- 40	88	68	43	22	+ 8	- 16	- 34	
	306	72	48	23	1	- 11	·— 36	- 48	73	57	32	10	- 4	-20	- 38	
	428	78	53	25	+ 3	- 11	- 32	- 44	73	51	25	+ 3	- 11	- 25	40	
	469	69	44	17	- 5	- 17	- 40	- 54	59	42	15	- 5	- 17	- 32	- 46	
	510	62	38	11	- 11	-24	- 48	- 59	- 57	39	12	- 7	20	- 34	- 49	
	592	51	28	+ 3	- 19	- 34	- 56	- 68	46	28	÷ 5	-10	- 27	- 41	- 5/	
	673	42	22	- 5	- 27	- 40	- 62	- 76	30	20	- 3	- 23	- 33	- 50	- 04	
	755	40	25	- 1	- 24	- 38	- 61	- 73	35	27	0	- 20	- 32	- 45	- 01	
	796	37	22	- 3	- 27	- 37	- 62	- 74	33	24	- 1	- 21	- 33	- 40	- 02	
	837	43	18	- 11	- 32	- 40	- 68	- 79	32	14	- 13	- 31	- 43	- 5/	- 12	
	878	35	11	- 10	- 3/	49	73	- 84	20	9	- 10	34	- 4/	01	- /5	
	918	28	0	- 21	- 42	- 53	- 70	80	21	1	- 20	- 38 27	- 50	- 01	- 73 70	
	959	25	5	-22	- 42	- 57	- 77	- 91	22	4	19	- 37	- 49	- 00	- 78	

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330	397 412 428 443 504 535 566 597 628 690 752 814 876 907 938 969	$168 \\ 128 \\ 106 \\ 100 \\ 88 \\ 81 \\ 74 \\ 70 \\ 62 \\ 59 \\ 51 \\ 46 \\ 40 \\ 36 \\ 33 \\ 31 \\ 30$	140 98 79 70 58 51 44 40 31 29 22 18 13 11 8 6 3	103 63 44 36 25 17 12 8 + 1 - 1 - 8 - 11 - 15 - 17 - 19 - 21 - 24	$\begin{array}{r} 44\\ 26\\ 9\\ + 4\\ - 6\\ - 13\\ - 17\\ - 21\\ - 26\\ - 31\\ - 32\\ - 37\\ - 39\\ - 41\\ - 44\\ - 46\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c}127 \\118 \\ -107 \\76 \\ -53 \\56 \\60 \\63 \\66 \\67 \\70 \\70 \\76 \\76 \\78 \\78 \\79 \end{array}$	$-162 \\ -169 \\ -180 \\ -182 \\ -175 \\ -144 \\ -79 \\ -53 \\ -66 \\ -72 \\ -80 \\ -78 \\ -88 \\ -89 \\ -89 \\ -91$	$     \begin{array}{r}       159\\       125\\       106\\       99\\       83\\       74\\       68\\       60\\       53\\       51\\       43\\       37\\       31\\       28\\       26\\       23\\       21     \end{array} $	134 99 79 68 59 47 41 37 30 29 22 18 13 9 7 7 5	$ \begin{array}{r} 101\\61\\44\\35\\25\\15\\11\\7\\2\\+1\\-6\\-7\\-12\\-16\\-18\\-20\\-22\end{array} $	$\begin{array}{r} 47\\ 24\\ 13\\ + 7\\ - 2\\ - 10\\ - 14\\ - 18\\ - 22\\ - 22\\ - 22\\ - 22\\ - 23\\ - 33\\ - 36\\ - 38\\ - 39\\ - 39\\ - 39\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c} -135\\ -137\\ -137\\ -136\\ -125\\ -113\\ -96\\ -77\\ -65\\ -65\\ -65\\ -65\\ -75\\ -77\\ -77\\ -77\\ -77\\ -77\\ -79\end{array}$
550	571 582 593 616 639 661 684 707 729 774 819 864 910 932 945 977	129 121 112 95 87 74 70 67 60 54 48 45 39 39 35 29	98 91 79 62 53 44 40 37 30 25 20 22 14 12 10 8	58 50 42 23 18 8 7 + 2 - 3 - 8 - 12 - 10 - 16 - 17 - 20	$ \begin{array}{r} 11 \\ + 5 \\ 0 \\ - 14 \\ - 19 \\ - 25 \\ - 27 \\ - 30 \\ - 34 \\ - 37 \\ - 39 \\ - 37 \\ - 41 \\ - 40 \\ - 40 \\ - 42 \end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -161 \\ -163 \\ -166 \\ -163 \\ -151 \\ -120 \\ -101 \\ -72 \\ -65 \\ -71 \\ -78 \\ -76 \\ -80 \\ -77 \\ -77 \\ -77 \\ -77 \end{array}$	$\begin{array}{r} -190\\ -191\\ -195\\ -200\\ -203\\ -205\\ -201\\ -201\\ -200\\ -174\\ -59\\ -66\\ -80\\ -77\\ -78\\ -84\end{array}$	$123 \\ 116 \\ 107 \\ 89 \\ 82 \\ 72 \\ 66 \\ 61 \\ 56 \\ 49 \\ 41 \\ 40 \\ 33 \\ 33 \\ 31 \\ 29$	98 90 77 60 57 45 42 36 31 125 19 17 12 13 11. 6	$\begin{array}{r} 59\\ 50\\ 42\\ 25\\ 21\\ 11\\ 8\\ + 4\\ - 1\\ - 7\\ - 11\\ - 10\\ - 15\\ - 14\\ - 16\\ - 16\end{array}$	$ \begin{array}{r} 18\\11\\+6\\-7\\-11\\-19\\-21\\-24\\-28\\-30\\-36\\-33\\-38\\-37\\-37\\-37\\-37\end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -120\\ -107\\ -101\\ -93\\ -84\\ -82\\ -76\\ -76\\ -76\\ -76\\ -69\\ -72\\ -69\\ -72\\ -67\\ -66\\ -69\end{array}$	$\begin{array}{r} -150 \\ -148 \\ -148 \\ -145 \\ -139 \\ -141 \\ -139 \\ -139 \\ -139 \\ -132 \\ -123 \\ -105 \\ -86 \\ -73 \\ -67 \\ -69 \end{array}$
800	761 774 788 801 814 841 867 894 947 973	112 94 88 83 75 67 56 50 35 30	79 65 58 54 46 39 31 23 12 10	$ \begin{array}{r} 35\\27\\17\\16\\9\\+5\\-3\\-9\\-17\\-13\end{array} $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -136\\ -126\\ -115\\ -99\\ -81\\ -57\\ -55\\ -58\\ -57\\ -52\\ \end{array}$	$-183 \\ -183 \\ -187 \\ -189 \\ -188 \\ -193 \\ -192 \\ -185 \\ -154 \\ -91$	$\begin{array}{r} -206 \\ -205 \\ -209 \\ -209 \\ -210 \\ -215 \\ -222 \\ -227 \\ -228 \\ -216 \end{array}$	100 91 83 81 73 66 57 48 34 31	70 63 57 51 46 40 30 27 13 15	$\begin{array}{r} 36\\ 29\\ 21\\ 19\\ 12\\ 9\\ + 3\\ - 4\\ - 12\\ - 12\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrr}106 \\90 \\74 \\58 \\50 \\46 \\49 \\52 \\53 \\48 \end{array}$	$-148 \\ -142 \\ -142 \\ -131 \\ -118 \\ -114 \\ -109 \\ -104 \\ -87 \\ -71$	$-165 \\ -164 \\ -167 \\ -165 \\ -161 \\ -158 \\ -159 \\ -155 \\ -153 \\ -144$

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## TABLE 3—continued

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## (e) $M = 2 \cdot 8$

## α(degrees)

$10^3 y/s_T$	$10^{3}x/c_{0}$	-6.23	-4·15	-2.07	0	2.07	4·15	6.23
0	100	65	65	67	63	49	41	+ 35
	200	69	49	37	27	5	+ 1	- 11
	300	70	52	36	24	+ 2	- 6	- 16
	400	60	40	24	12	- 10	- 18	-28
	500	57	37	21	9	- 13	- 23	- 31
	600	48	30	14	2	- 20	- 24	- 38
065	148	96	78	62	52	26	20	- 2
	193	82	64	50	38	+ 12	+ 6	- 12
	238	72	54	24	24	0	- 8	- 22
	283	70	50	34	20	- 2	- 8	-22
125	204	111	99	. 83	67	39	19	- 37
	224	98	74	58	42	14	+ 2	- 24
	244	88	70	52	36	8.	4	- 24
	265	85	63	_45	29	+ 1	- 11	- 27
	306	72	52	34	20	- 6	- 14	- 34
	428	68	44	26	12	- 12	- 20	36
	469	59	35	19	3	19	- 25	- 41
	510	56	36	20	+ 6	- 18	- 24	- 40
	592	48	30	· 12	. 0	- 24	30	- 46
	673	37	21	7	- 5.	- 31	- 37	- 51
	755	36	24	10	- 2	- 26	- 30	- 48
	796	35	23	+ 11	- 1	- 25	- 31	- 47
	837	36	12	- 4	- 18	- 40	- 46	- 62
	878	30	10	- 6	- 22	- 44	- 50	- 64
	918	26	8	- 8	- 20	- 42	— 46	- 64
	959	25	7	- 7	- 21	- 43	— 55	- 65

	330	397 412 428 443 473 504 535 566 597 628 690 752 814 876 907 938 969	150 122 104 94 84 75 68 64 58 55 49 42 37 30 30 28 26	$     \begin{array}{r}       122 \\       90 \\       75 \\       64 \\       54 \\       43 \\       38 \\       30 \\       27 \\       23 \\       18 \\       13 \\       10 \\       8 \\       6 \\       6     \end{array} $	$\begin{array}{c} 94\\ 63\\ 47\\ 38\\ 28\\ 21\\ 16\\ 16\\ 16\\ 8\\ 7\\ +3\\ 0\\ -7\\ -8\\ -8\\ -8\\ -10\\ -10\end{array}$	$53 \\ 321 \\ 12 \\ + 6 \\ - 1 \\ - 2 \\ - 4 \\ - 12 \\ - 11 \\ - 13 \\ - 21 \\ - 22 \\ - 22 \\ - 24 \\ - 24$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} -114 \\ -110 \\ -100 \\ -95 \\ -87 \\ -84 \\ -77 \\ -71 \\ -73 \\ -68 \\ -68 \\ -68 \\ -66 \\ -66 \\ -66 \\ -66 \\ -66 \end{array}$
39	550	571 582 593 616 639 661 684 707 729 774 819 864 910 932 955 977	127 121 111 92 86 75 71 65 59 53 44 39 32 35 33 31	99 91 81 64 56 47 43 37 33 25 18 19 12 13 11 13	$\begin{array}{c} 72 \\ 63 \\ 53 \\ 38 \\ 32 \\ 23 \\ 19 \\ 13 \\ 11 \\ + 5 \\ - 2 \\ - 1 \\ - 6 \\ - 5 \\ - 7 \\ - 3 \end{array}$	$\begin{array}{r} 38\\ 33\\ 25\\ 14\\ + 8\\ - 1\\ - 3\\ - 9\\ - 11\\ - 15\\ - 20\\ - 17\\ - 22\\ - 21\\ - 21\\ - 21\\ - 19\end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{r} -113 \\ -110 \\ -108 \\ -99 \\ -91 \\ -90 \\ -86 \\ -88 \\ -86 \\ -88 \\ -86 \\ -88 \\ -86 \\ -89 \\ -82 \\ -82 \\ -82 \\ -82 \\ -82 \\ -76 \\ \end{array} $
	800	761 774 788 801 814 841 867 894 947 973	101 95 88 84 76 71 60 50 39 37	73 71 60 58 50 47 36 30 19 19	49 47 34 34 28 23 16 10 1 3	$ \begin{array}{r}     13 \\     15 \\     8 \\     8 \\     4 \\     + 1 \\     - 4 \\     - 12 \\     - 12 \\     - 13 \\ \end{array} $	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{r} -106 \\ - 88 \\ - 91 \\ - 85 \\ - 79 \\ - 69 \\ - 62 \\ - 58 \\ - 59 \\ - 51 \\ \end{array} $	$\begin{array}{r} -136 \\ -124 \\ -129 \\ -127 \\ -119 \\ -106 \\ -99 \\ -93 \\ -88 \\ -80 \end{array}$



FIG. 1. General arrangement of model.



FIG. 2. Planform and cross-section shapes.



FIG. 3. Chordwise section shapes.





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FIG. 5. Lift curves with model inverted, and effective downwash.

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FIG. 6. Variation of  $C_L/\alpha$  with Mach number. ( $C_L = 0$  and  $C_L = 0.075.$ )





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![](_page_44_Figure_1.jpeg)

![](_page_44_Figure_2.jpeg)

![](_page_45_Figure_0.jpeg)

![](_page_45_Figure_1.jpeg)

![](_page_45_Figure_2.jpeg)

![](_page_45_Figure_3.jpeg)

![](_page_46_Figure_0.jpeg)

FIG. 12. Chordwise pressure distributions at  $\alpha = 0$ .

![](_page_47_Figure_0.jpeg)

FIG. 12. Chordwise pressure distributions at  $\alpha = 0$ .

![](_page_48_Figure_0.jpeg)

![](_page_48_Figure_1.jpeg)

![](_page_49_Figure_0.jpeg)

![](_page_49_Figure_1.jpeg)

![](_page_50_Figure_0.jpeg)

![](_page_50_Figure_1.jpeg)

FIG. 14b. Chordwise pressure distributions at various incidences.

![](_page_51_Figure_0.jpeg)

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FIG. 14c. Chordwise pressure distributions at various incidences.

![](_page_51_Figure_3.jpeg)

Fig. 15. Effect of transition fixing and larger sting shroud on pressure distributions at M = 2.

![](_page_52_Figure_0.jpeg)

FIG. 16. Surface pressure increments due to lift.

![](_page_53_Figure_0.jpeg)

FIG. 17. Contributions of upper and lower surfaces to total chord load at  $\alpha = 4.25^{\circ}$ .

![](_page_54_Figure_0.jpeg)

FIG. 18. Spanwise distributions of chord load at various Mach numbers and incidences.

![](_page_55_Figure_0.jpeg)

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![](_page_55_Figure_1.jpeg)

![](_page_55_Figure_2.jpeg)

FIG. 20. Spanwise distributions of  $\Delta C_p/\alpha$  at various  $x/C_0$ : variation with Mach number at  $\alpha \sim 4.25^{\circ}$ .

![](_page_56_Figure_0.jpeg)

![](_page_56_Figure_1.jpeg)

![](_page_56_Figure_2.jpeg)

![](_page_56_Figure_3.jpeg)

![](_page_56_Figure_4.jpeg)

![](_page_57_Picture_0.jpeg)

 $M = 1 \cdot 4.$ 

![](_page_57_Picture_2.jpeg)

![](_page_57_Figure_3.jpeg)

![](_page_57_Figure_4.jpeg)

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![](_page_58_Picture_0.jpeg)

 $M = 2 \cdot 4.$ 

![](_page_58_Figure_2.jpeg)

![](_page_58_Figure_3.jpeg)

FIG. 23—continued. Oil-flow pictures at  $\alpha = 6 \cdot 4^{\circ}$ .

![](_page_59_Figure_0.jpeg)

FIG. 24. Attachment lines, etc., at various Mach numbers,  $\alpha = 6 \cdot 4^{\circ}$ .

![](_page_60_Picture_0.jpeg)

 $M = 2 \cdot 0.$ 

![](_page_60_Picture_2.jpeg)

![](_page_60_Figure_3.jpeg)

FIG. 25. Schlieren pictures at zero incidence.

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